

Advanced Short-Term Actuarial Mathematics Exam

SPRING 2023

The ASTAM Exam is a three-hour exam consisting of 60 points of written-answer questions. The exam will be taken at Prometric testing centers. The written-answer questions will be displayed on the computer and answered in a paper answer booklet to be provided and collected by Prometric. An Excel workbook will be available for calculations, but the workbook will not be submitted for grading. A formula sheet will be available on the computer. Paper versions of the exam and formula sheet will not be provided. Candidates will be provided with a scratchpad.

Knowledge of the FAM Exam material is assumed for the ASTAM Exam.

[Exam Registration](#)

Candidates may register online or with an application.

[Introductory Study Note](#)

The Introductory Study Note has a complete listing of all study notes as well as errata and other important information.

[Past Exams](#)

Past STAM Exams are available on the SOA website. There are no past ASTAM Exams.

[Updates](#)

Candidates should be sure to check the Updates page on the exam home page periodically for additional corrections or notices.

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1. Topic: Severity Models (12-22%)

Learning Objectives

The Candidate will understand, interpret, and be able to perform calculations with commonly used severity distributions, including extreme value distributions.

Learning Outcomes

The Candidate will be able to:

- a) Describe how changes in the parameters affect the distributions.
- b) Create new distributions by multiplication by a constant, raising to a power, exponentiation, mixing and splicing.
- c) Understand and interpret the characteristics of severity distributions.
- d) Compare two distributions based on various characteristics of their tails, including moments, ratios of moments, limiting tail behavior, hazard rate functions, and mean excess functions.
- e) Understand the derivation and characteristics of the Generalized Extreme Value and the Generalized Pareto distributions.
- f) Apply the Generalized Extreme Value and the Generalized Pareto distributions to the estimation of tail measures and probabilities.

2. Topic: Aggregate Models (12-22%)

Learning Objectives

The Candidate will understand, interpret, and be able to perform calculations with aggregate models.

Learning Outcomes

The Candidate will be able to:

- a) Use convolution and recursive formulas to derive probability and distribution functions for aggregate claims distributions with $(a,b,0)$ or $(a,b,1)$ frequency, and with discrete severity distributions.
- b) Derive the discretized version of a continuous distribution using the method of rounding and local moment matching.
- c) Perform calculations for sums of compound Poisson models.

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| 3. Topic: Coverage Modifications (6-12%) |
| Learning Objectives |
| The Candidate will understand, interpret, and be able to perform calculations with respect to coverage modifications. |
| Learning Outcomes |
| The Candidate will be able to: <ul style="list-style-type: none">a) Evaluate the effects of the following coverage modifications: deductibles, policy limits, maximum covered loss, coinsurance, and stop loss reinsurance.b) Calculate and interpret loss elimination ratios, increased limits factors, and deductible factors.c) Evaluate and interpret the effects of inflation on losses. |

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| 4. Topic: Construction and Selection of Parametric Models (12-22%) |
| Learning Objectives |
| The Candidate will understand and be able to construct and estimate parameters for parametric models. |
| Learning Outcomes |
| The Candidate will be able to: <ul style="list-style-type: none">a) Estimate the parameters for frequency and severity distributions by maximum likelihood.b) Estimate the variance of the estimators and construct normal and non-normal confidence intervals.c) Use the delta method to estimate the variance of the maximum likelihood estimator of a function of the parameter(s).d) Estimate the parameters for severity, frequency, and aggregate distributions using Bayesian Estimation.e) Perform model selection using:<ul style="list-style-type: none">• Graphical procedures.• Hypothesis tests, including Kolmogorov-Smirnov, Chi-square goodness-of-fit, and Likelihood ratio (LRT) tests.• Score-based approaches, including Schwarz Bayesian Criterion (SBC), Bayesian Information Criterion (BIC), and Akaike Information Criterion (AIC). |

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| 5. Topic: Credibility (12-20%) |
| Learning Objectives |
| The Candidate will understand and be able to estimate losses using credibility procedures. |
| Learning Outcomes |
| The Candidate will be able to: <ul style="list-style-type: none">a) Explain and apply Bayesian (greatest accuracy) credibility.b) Apply Bühlmann and Bühlmann-Straub models and understand their relationship to Bayesian models.c) Explain and apply empirical Bayesian estimation in the nonparametric and semiparametric cases. |

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| 6. Topic: Reserving for Short-Term Insurance Coverages (12-20%) |
| Learning Objectives |
| The Candidate will be able to calculate reserves for short-term insurance coverages. |
| Learning Outcomes |
| The Candidate will be able to: <ul style="list-style-type: none">a) Understand, interpret, and apply techniques for estimating outstanding claims, using the following methods:<ul style="list-style-type: none">• Expected Loss Ratio• Chain-Ladder• Bornhuetter-Ferguson• Bayesian• Frequency and Severityb) Understand, interpret, and apply the following statistical models and assumptions used for outstanding claims reserves:<ul style="list-style-type: none">• Mack's model• Poisson model• Overdispersed Poisson model |

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7. Topic: Pricing for Short-Term Insurance Coverages (4-12%)

Learning Objectives

The Candidate will be able to calculate premiums for short-term insurance coverages.

Learning Outcomes

The Candidate will be able to:

- a) Calculate projected losses using trend analysis.
- b) Calculate overall average rates and rate changes using the loss cost and loss ratio methods.
- c) Calculate risk classification differential changes, including balancing back.

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Resources

- *Loss Models: From Data to Decisions*, (Fifth Edition), 2019, by Klugman, S.A., Panjer, H.H. and Willmot, G.E., Wiley, ISBN: 978-1-119-52378-9
 - Chapter 3 (Sections 4.2-4.6)
 - Chapter 5 (Sections 1, 2)
 - Chapter 8
 - Chapter 9 (Sections 3.1-2, 4 (Theorem 9.7 & Example 9.9 only), 5, 6 (except 6.1), 7)
 - Chapter 11 (Sections 5-7)
 - Chapter 12 (Section 4)
 - Chapter 13
 - Chapter 15 (except Section 4.2)
 - Chapter 17
 - Chapter 18
- *Introduction to Ratemaking and Loss Reserving for Property and Casualty Insurance* (Fifth Edition), 2022, by Brown and Lennox, ACTEX, ISBN: 978-1-64756-787-3 [Candidates may also use Fourth Edition, 2015, (same chapters) ACTEX, ISBN: 978-1625424747]
 - Chapter 4 (Section 8)
 - Chapter 5 (Sections 3, 4)
- [ASTAM-21-23: Outstanding Claims Reserves](#), 2022, Hardy, M.R.
- [ASTAM-22-23: Chapter 5 of Quantitative Enterprise Risk Management](#), 2022, by Hardy, M.R. and Saunders, D. Cambridge University Press, ISBN : 978-1009098465
- [Notation and Terminology used on Exam ASTAM](#)
- [ASTAM Formula Sheet](#)
- [Sample questions and solutions](#)
- [Corrections and Comments for Loss Models, Fifth Edition](#)

Note: The text and any study notes will not be available with the examination. An electronic copy of the formula sheet will be available with the exam.