# The Effect of Global Warming On Discounting Methodology 

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## Stern Review: The Economics of Climate Change

- October 30, 2006
- Sir Nicholas Stern, head of UK government economics service
- Headlines: If nothing is done to arrest it, the expected value of the present value of the future effects of global warming could be equivalent to a $20 \%$ decline in world real GDP per capita, starting now and lasting forever. Such a decline in GDP would be a catastrophe equivalent to all the wars and great depressions of the twentieth century combined.
- Fine print: The study actually concluded that the expected value is in a range of $5 \%$ to $20 \%$ decline in world real GDP per capita, but the $20 \%$ possibility should be taken seriously.
- Prescription: We can avoid it if we start immediately to sacrifice $1 \%$ of world real GDP per capita annually to arrest warming. A no-brainer. (Fine print: mainstream studies range from $0 \%$ to $5 \%$ ).


## Yikes! What Are the Numbers?

EXPECTED VALUE OF REDUCTION IN WORLD REAL GDPPER CAPITA CAUSED BY GLOBAL WARMING

| Typical* |  |  | $2.2 \%$ |
| :--- | :---: | :---: | ---: |
| add Catastrophes* | $0.2 \%$ | $0.9 \%$ | $5.3 \%$ |
| add Feedbacks* |  |  | $7.3 \%$ |
| add non-Market Effects* |  | $2.9 \%$ | $13.8 \%$ |
| add new Sensitivity Est.** | $1.3 \%$ | $5.9 \%$ | $24.4 \%$ |

source: *buried in the text on pages 155 and 156 **buried in the text on page 156, science not solid yet

## How Certain Are The Numbers?

| RANGE OF VALUE OF REDUCTION IN WORLD REAL GDP PER |  |  |  |
| :--- | :---: | :---: | :---: |
| CAPITA CAUSED BY GLOBAL WARMING IN 2200 | \& BEYOND |  |  |
| Model | $\mathbf{5 \%}$ (ile | Mean | $\mathbf{9 5 \%}$-ile |
| Typical Models* |  | $2.2 \%$ |  |
| add Catastrophes* | $0.6 \%$ | $5.3 \%$ | $13.4 \%$ |
| add Feedbacks* | $0.9 \%$ | $7.3 \%$ | $17.9 \%$ |
| add non-Market Effects* | $2.9 \%$ | $13.8 \%$ | $35.2 \%$ |
| add new Sensitivity Est.** |  | $24.4 \%$ |  |

sources: *buried in the text on pages 155 and 156 **buried in the text on page 156, science not solid yet

## What Are The Present Values?

Balanced Growth Equivalent (BGE): The reduction in world GDP per capita applied now and in all future years that would produce the same present value

| RANGE OF BGE OF REDUCTION IN ALL FUTURE WORLD |  |  |  |
| :--- | :---: | :---: | ---: |
| REAL GDP PER CAPITA CAUSED BY GLOBAL | WARMING |  |  |
| Model | 5\%-ile | Mean | $\mathbf{9 5 \%}$-ile |
| Typical Models | $0.3 \%$ | $2.1 \%$ | $5.9 \%$ |
| add Catastrophes | $0.6 \%$ | $5.0 \%$ | $12.3 \%$ |
| add Feedbacks | $0.9 \%$ | $6.9 \%$ | $16.5 \%$ |
| add non-Market Effects | $2.7 \%$ | $14.4 \%$ | $32.6 \%$ |
| add new Sensitivity Est. | not given |  |  |
| recommended upper bound* | $20 \%$ |  |  |

sources: chart on page 163 *judgmental, text on page 164

## Schematically

## World GDP Over Centuries

—— Warming —— No Warming ——Arrest Warming ——BGE of Warming

## What Kind of Present Values Are Those?

| Range of value of reduction in world real gdp per CAPITA CAUSED BY GLOBAL WARMING IN 2200 \& BEYOND |  |  |  |
| :---: | :---: | :---: | :---: |
| Model | 5\%-ile | Mean | 95\%-ile |
| Typical Models |  | 2.2\% |  |
| add Catastrophes | 0.6\% | 5.3\% | 13.4\% |
| add Feedbacks | 0.9\% | 7.3\% | 17.9\% |
| add non-Market Effects | 2.9\% | 13.8\% | 35.2\% |
| add new Sensitivity Est. |  | 24.4\% |  |
| RANGE OF BGE OF REDUCTION IN ALL FUTURE WORLD |  |  |  |
|  |  |  |  |
| Model | 5\%-ile | Mean | 95\%-ile |
| Typical Models | 0.3\% | 2.1\% | 5.9\% |
| add Catastrophes | 0.6\% | 5.0\% | 12.3\% |
| add Feedbacks | 0.9\% | 6.9\% | 16.5\% |
| add non-Market Effects | 2.7\% | 14.4\% | 32.6\% |
| add new Sensitivity Est. |  | not give |  |

## Partial Explanation (from commentators)

- They discounted at only $\delta=0.1 \%$ per year
- Then why aren't the effects proportional?
- And how can a BGE be higher than every one of the future values?
- They used an inappropriate elasticity of marginal utility $\eta=1$
- This has the effect of valuing equal percentage changes in wealth equally whether for paupers or millionaires
- $1.3 \%$ baseline annual growth in world real GDP per capita makes a lot more future millionaires and a lot fewer future paupers, so they are valuing a reduction in future caviar supplies equally with a reduction in current bread supplies


## Stern Review Explanation

- Why discount at only $\delta=0.1 \%$ per year?
- We have no ethical right to value our welfare above that of our great-great-great-great-great grandchildren just because we are alive and they are not. The ethical pure discount rate is $0 \%$. But there is some chance that we won't have any great-great-great-great-great grandchildren at all (asteroids, epidemics, etc. might make the human race extinct) so we can discount for that probability. Make it $0.1 \%$ per year, even though that's probably too big
- What does the elasticity of marginal utility (whatever that is) have to do with present values?
- Financial discounting works by examining the marginal effect on the welfare of the world from a small change in circumstances. If the circumstances you are evaluating change the world entirely, then you cannot use a technique grounded in marginal effects. Instead sum up all future welfare effects (discounted only for the probability of human extinction) of the circumstances you are evaluating.


## Stern Review Explanation

- But why use that $\eta=1$ value in calculating future welfare?
- Not much of an answer was given. Essentially, they claimed that the empirical economics literature doesn't clearly support any other value as being implied by current interest rates. They didn't even mention an ethical dimension to this question (valuing future caviar shortages the same as bread shortages today).


## Financial Discounting Is Only For Marginal Effects?

PV of Welfare $=$ utility of consumption $\times$ pure time preference

$$
\begin{aligned}
W(0) & =\int_{0}^{\infty} U(C(t)) e^{-\delta t} d t \\
\Delta W(0) & =\int_{0}^{\infty} \Delta C(t) \frac{d U}{d C}(C(t)) e^{-\delta t} d t \\
& =\int_{0}^{\infty} \Delta C(t) e^{\int_{0}^{t}\left(\frac{d}{d s} \ln \left[\frac{d U}{d C}(C(s))\right]-\delta\right) d s} d t
\end{aligned}
$$

so discount rate at $s$ is $=-\frac{d}{d s} \ln \left[\frac{d U}{d C}(C(s))\right]+\delta$
for simplicity let $\frac{d U}{d C}(C)=C^{-\eta}$ for some $\eta \geq 1$ and you get
discount rate at $s$ is $=\eta \frac{\frac{d C}{d s}(s)}{C(s)}+\delta$ for marginal $\Delta C(t), t \geq s$
$\eta=$ the elasticity of marginal utility

## So Financial Discounting Depends On The Economic Path

Discount rate at $s$ is $=\eta \frac{\frac{d C}{d s}(s)}{C(s)}+\delta$ for marginal $\Delta C(t), t \geq s$

- In a faster growing economy, you discount at a higher rate
- In a negatively growing economy $\left(\frac{d C}{d s}(s)<0\right)$, you might even discount at a negative rate! (if $-\eta \frac{\frac{d C}{d s}(s)}{C(s)} \geq \delta$ )
- This is not unlikely if $\delta$ has been chosen quite small!
- But what if you are discounting a disturbance to the entire economic path?
- $C(s) \longrightarrow C^{\prime}(s)$ for all $s$
- Do I use $\frac{d C}{d s}(s)$ or $\frac{d C^{\prime}}{d s}(s)$ to determine my discount rate?
- Stern Review says you give up discounting financial values and instead go back to $W(0)=\int_{0}^{\infty} U(C(t)) e^{-\delta t} d t$


## Stern Review: You Can't Discount Financial Values

- If you can't discount how do you get a present value?
- Well, they never actually calculate present values of financial variables, only of welfare.
- If $W(0)=\int_{0}^{\infty} U(C(t)) e^{-\delta t} d t=\int_{0}^{\infty} U\left(C^{\prime}(t)\right) e^{-\delta t} d t=W^{\prime}(0)$ then
say that $C(t)$ and $C^{\prime}(t)$ have "the same present value"
- $C(t)$ might represent the BGE path at a lower growth rate than a world without global warming; $C^{\prime}(t)$ might represent the path of the world with global warming
- Notice that the BGE path won't have any negative value of $\frac{d C}{d s}(s)$; a Monte Carlo generated global warming path has a high likelihood of $\frac{d C^{\prime}}{d s}(s)<0$ for long stretches of time.
- All the present value assertions in the Stern Review come about in this way.
- Why does that matter? We're not discounting financial values anymore, we're only discounting welfare.


## But We Are Discounting Financial Values!

- Let $C(t)$ be the BGE path at a lower growth rate than the world without global warming and $C^{\prime}(t)$ be a Monte Carlo generated global warming path.
- At each $t$ let $\Delta C(t)=C(t)-C^{\prime}(t)$ and define $C(t, p)$ for $0 \leq p \leq 1$ by $\frac{\partial C(t, p)}{\partial p}=\Delta C(t)$. Use $C(t, p)$ to define $W(0, p)$ and then $\Delta W(0)=\int_{0}^{1} \frac{\partial W}{\partial p}(0, p) d p$. Now

$$
\begin{aligned}
\Delta W(0) & =\int_{0}^{1} \int_{0}^{\infty} \frac{\partial c(t, p)}{\partial p} \frac{d U}{d C}(C(t, p)) e^{-\delta t} d t d p \\
& =\int_{0}^{\infty} \Delta C(t) \int_{0}^{1} e^{-\int_{0}^{t}\left(\eta \frac{\frac{\partial C}{\partial s}(s, p)}{C(s, p)}+\delta\right) d s} d p d t
\end{aligned}
$$

## The Implicit Discount Rate In Stern

$$
-\frac{d}{d t} \ln \int_{0}^{1} e^{-\int_{0}^{t}\left(\eta \frac{\partial C}{\frac{\partial \mathcal{S}}{\partial(s, p)}(s, p)}+\delta\right) d s} d p
$$

- If $\frac{\partial C}{\partial s}(s, p) \leq 0$ for a significant range of $p$, which will be the case when $\frac{d C^{\prime}}{d s}(s) \leq 0$, and if $\delta$ is small, then this implicit discount rate in Stern's modeling can be negative.
- This discounting at a negative interest rate for stretches of time in some of the Monte Carlo runs is especially pernicious because he approximates $\int_{\text {year } 2200}^{\infty}$ by a simple growing perpetuity on each Monte Carlo path.
- Well, that's the Stern Review methodology. What about their choices for the values of $\delta$ and $\eta$ ?


## Comparitive Values of Parameters - BGE Decline Due To

 Warming for Typical Models plus Cats, Feedback \& Non-Market Effects| $\eta$ | 1.5 | 1.0 | 1.5 | 1.0 | yr 2200 | 1.0 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $\delta$ | 1.5 | 1.5 | 0.1 | 0.0 |  | 0.1 |
| $5 \%$-ile | $0.6 \%$ | $0.8 \%$ | $2.0 \%$ | $3.2 \%$ | $2.9 \%$ | $2.7 \%$ |
| mean | $2.8 \%$ | $4.2 \%$ | $10.2 \%$ | $16.9 \%$ | $13.8 \%$ | $\mathbf{1 4 . 4} \%$ |
| $95 \%$-ile | $6.8 \%$ | $10.1 \%$ | $20.0 \%$ | $38.4 \%$ | $35.2 \%$ | $32.6 \%$ |
| judgmental | $4 \%$ | $6 \%$ | $13 \%$ | $24 \%$ |  | $20 \%$ |

source
conclusion

JB Annex Annex JB
p. 156
p. 163
too low too low too low good! rats! well,OK

- Stern couldn't get the answer he wanted with $\eta>1$ or $\delta>0$, but then had to dial $\delta$ up just a bit in order avoid looking ridiculous. Unfortunately, at $\delta=0.1$ there are still some ridiculous data points


## Speaking of Ethics

- The baseline growth rate in real per capita GDP assumed in Stern's modeling is $1.3 \%$ per annum.
- With world GDP per capita of $\$ 7,600$ in 2006 (Stern) that means that without global warming world real per capita GDP in 2200 would be $\$ 93,121$.
- A $13.8 \%$ decline in 2200 world real GDP per capita caused by global warming would leave it at $\$ 80,270$.
- How much should the poverty end of today's $\$ 7,600$ average be expected to pay to keep that unfortunate average citizen in 2200 from having to live on only $\$ 80,270$ instead of $\$ 93,121$ ?
- By setting $\eta=1$ most of that decline from $\$ 93,121$ to $\$ 80,270$ is reflected today. Tommorow's caviar shortage is equated to today's bread shortages.
- Should we really believe even a low growth rate like $1.3 \%$ as lasting forever?


## A Few More Thoughts

- Maybe the social consequences of a falling GDP (chaotic and violent unrest, organized warfare, etc.) are the same whether it's falling from a high level to a slightly less high level or from a low level to a slightly lower level?
- In that case, maybe it makes sense to discount future values at a negative interest rate when valuing income that would arrive in the midst of such dire circumstances? (Assuming you've properly discounted for the probability of arrival, given such dire circumstances)
- In that case, maybe it makes sense to discount the value of that future decline at a negative interest rate when deciding what it is worth spending today in order to avert/ameliorate the decline?
- But regardless, these aren't your father's present values! It is a distinct methodological departure. There's a lot to learn from it, but it seems troublesome that the results were summarized as simply "present value" comparisons.

