



SOCIETY OF ACTUARIES

Article from:

# ARCH 2013.1 Proceedings

August 1- 4, 2012

Yu Lin, Xiaoming Liu

## Dynamic Population Structure with Stochastic Mortality and Fertility Rates

*Yu Lin<sup>1</sup> and Xiaoming Liu<sup>2</sup>*

<sup>1</sup>University of Western Ontario, London, Canada; [ylin287@uwo.ca](mailto:ylin287@uwo.ca)

<sup>2</sup>University of Western Ontario, London, Canada; [xliu@stats.uwo.ca](mailto:xliu@stats.uwo.ca)

The impact of a stochastic population structure on the labour force stability is very important for pension risk management and investigated in this study. We propose a stochastic population structure model based on the Leslie matrix, in which we use a Lee-Carter model framework to describe the future mortality and fertility changes. This population structure model is then combined with investment return models to examine the impact of a Defined Contribution (DC) pension systems on the labour force stability, if the population follows the current changing patterns in mortality and fertility rates. U.S. population data from 1933-2008 is used to validate the population projection and dependency ratio (the ratio of retirees to workers) is calculated to illustrate the labour force stability over time.