

Quantitative Finance and Investment – Core Exam

Spring/Fall 2016

Important Exam Information:

Exam Registration Candidates may register online or with an application.

Order Study Notes
Study notes are part of the required syllabus and are not available electronically but may be purchased through the online store.

Introductory Study Note
The Introductory Study Note has a complete listing of all study

notes as well as errata and other important information.

Case Study There is no case study for this examination.

<u>Past Exams</u> Past Exams from 2000 - present are available on the SOA website.

Formula Package A Formula Package will be provided with the exam. Please see the

Introductory Study Note for more information.

<u>Table</u> A cumulative normal distribution table will be provided with the

exam.

<u>Updates</u> Candidates should be sure to check the Updates page on the exam

home page periodically for additional corrections or notices.

1. Topic: Stochastic Calculus

Learning Objectives

The candidate will understand the fundamentals of stochastic calculus as they apply to option pricing

Learning Outcomes

The Candidate will be able to:

- a) Understand and apply concepts of probability and statistics important in mathematical finance
- b) Understand the importance of the no-arbitrage condition in asset pricing
- c) Understand Ito integral and stochastic differential equations
- d) Understand and apply Ito's Lemma
- e) Understand and apply Jensen's Inequality
- f) Demonstrate understanding of option pricing techniques and theory for equity and interest rate derivatives.
- g) Demonstrate understanding of the differences and implications of real-world versus risk-neutral probability measures.
- h) Define and apply the concepts of martingale, market price of risk and measures in single and multiple state variable contexts.
- i) Understand and apply Girsanov's theorem in changing measures.
- j) Understand the Black Scholes Merton PDE (partial differential equation).

- An Introduction to the Mathematics of Financial Derivatives, Neftci, Hirsa, 3rd Edition, 2014
 - o Ch. 1-15
- Frequently Asked Questions in Quantitative Finance, Wilmott, Paul, 2nd Edition, 2009
 - o Ch. 2: Q23, Q25, Q26, Q36, Q37, Q60
 - o Ch. 6
- Paul Wilmott Introduces Quantitative Finance, Wilmott, Paul, 2nd Edition
 - o Ch. 6

2. Topic: Option Pricing and Hedging

Learning Objectives

- The candidate will understand how to apply the fundamental theory underlying the standard models for pricing financial derivatives
- The candidate will understand the implications for option pricing when markets do not satisfy the common assumptions used in option pricing theory such as market completeness, bounded variation, perfect liquidity, etc.
- The candidate will understand how to evaluate situations associated with derivatives and hedging activities.

Learning Outcomes

The Candidate will be able to:

- a) Identify limitations of the Black-Scholes pricing formula
- b) Compare and contrast the various kinds of volatility, (eg actual, realized, implied, forward, etc)
- c) Compare and contrast various approaches for setting volatility assumptions in hedging.
- d) Understand the different approaches to hedging.
- e) Understand how to delta hedge and the interplay between hedging assumptions and hedging outcomes.
- f) Appreciate how hedge strategies may go awry.
- g) Describe and explain some approaches for relaxing the assumptions used in the Black-Scholes formula.

- Paul Wilmott Introduces Quantitative Finance, Wilmott, Paul, 2nd Edition, 2007
 - o Ch. 2 (Background only) Ch. 8, 10, 26
- Frequently Asked Questions in Quantitative Finance, Wilmott, Paul, 2nd Edition, 2009
 - o Ch. 2: Q38, Q39, Q53
- QFIC-102-13: Current Issues: Options What Does An Option Pricing Model Tell Us About Option Prices?
- QFIC-103-13: How to Use the Holes in Black-Scholes
- QFIC-104-13: Chapter 3 of The Known, the Unknown, and the Unknowable in Financial Risk Management: Measurement and Theory Advancing Practice
- QFIC-105-13: Section IX of Carr Peter, FAQ's in Option Pricing Theory Which volatility should one hedge at historical or implied?" (pp. 26-28)

3. Topic: Interest Rate Models

Learning Objectives

The candidate will understand the quantitative tools and techniques for modelling the term structure of interest rates and pricing interest rate derivatives.

Learning Outcomes

The Candidate will be able to:

- a) Understand and apply the concepts of risk-neutral measure, forward measure, normalization, and the market price of risk, in the pricing of interest rate derivatives.
- b) Apply the models to pricecommon interest sensitive instruments including: callable bonds, , bond options, caps, floors, swaptions, caption, floortions
- c) Understand and apply popular one-factor interest rate models including Vasicek, Cox-Ross_Ingersoll, Hull-White, Ho-Lee, Black-Derman_Toy, Black-Karasinski
- d) Understand the concept of calibration and describe the issues related to calibration, including yield curve fitting.
- e) Understand and differentiate between the classical approach to interest rate modelling and the HJM modelling approach, including the basic philosophy, arbitrage conditions, assumptions, and practical implementations
- f) Understand and apply the HJM and BGM/Libor Market model.

- Paul Wilmott Introduces Quantitative Finance, Wilmott, Paul, 2nd Edition,2007
 - o Ch. 16-19
- An Introduction to the Mathematics of Financial Derivatives, Hirsa and Neftci, 3rd Edition, 2014
 - o Ch. 16-19

4. Topic: Volatility

Learning Objectives

The candidate will understand the concept of volatility and some basic models of it

Learning Outcomes

The Candidate will be able to:

- a) Compare and contrast the various kinds of volatility, (eg actual, realized, implied, forward, etc)
- b) Understand and apply various techniques for analyzing conditional heteroscedastic models including ARCH and GARCH

- Paul Wilmott Introduces Quantitative Finance, Wilmott, Paul, 2nd Edition, 2007
 - o Ch 9.5-9.7
- Analysis of Financial Time Series, Tsay, 3rd Edition, 2010
 - Chapters 1–2 (background only)
 - o Ch. 3 Conditional Heteroscedastic Models (3.1–3.8) 3.14
- QFIC-109-15: Chapter 9 of Risk Management and Financial Institutions, Hull, 2nd Edition

5. Topic: Fixed Income Portfolio Management

Learning Objectives

The candidate will understand and identify the variety of fixed instruments available for portfolio management.

This section deals with fixed income securities. As the name implies the cash flow is often predictable, however there are various risks that affect cash flows of these instruments. In general candidates should be able to identify the cash flow pattern and the factors affecting cash flow for commonly available fixed income securities. Candidates should be comfortable using various interest rate risk quantification measures in the valuation and managing of investment portfolios; Candidates should also understand various strategies of managing the portfolio against given benchmark.

Learning Outcomes

The Candidate will be able to:

- a) Explain the cash flow characteristics and pricing of Treasury securities.
- b) Demonstrate an understanding of par yield curves, spot curves, and forward curves and their relationship to traded security prices; and understanding of bootstrapping and interpolation.
- c) Demonstrate an understanding of the different characteristics, including credit quality, of securities issued by government agencies or government-sponsored enterprises.
- d) Evaluate features of municipal bonds including the role of rating agencies.
- e) Describe the cash flow of various corporate bonds considering underlying risks such as interest rate, credit and event risks.
- f) Demonstrate an understanding of the characteristics of leveraged loans.
- g) Demonstrate an understanding of cash flow pattern and underlying drivers and risks of agency and non-agency mortgage-backed securities, commercial mortgage-backed securities, and collateralized mortgage obligations.
- h) Demonstrate an understanding of the characteristics and mechanics of fixed income ETFs.;
- i) Construct and manage portfolios of fixed income securities using the following broad categories:
 - a. Managing funds against a target return
 - b. Managing funds against liabilities

- The Handbook of Fixed Income Securities, Fabozzi, Frank, 8th Edition, 2012
 - o Ch. 1,2 and 9 (background only), Ch.10-13, 17-18, 21, 24-26, 31-32
- Managing Investment Portfolios: A Dynamic Process, Maginn & Tuttle, 3rd Edition, 2007
 - o Ch. 6, Fixed Income Portfolio Management
- Paul Wilmott Introduces Quantitative Finance, Wilmott, Paul, 2nd Edition, 2007
 - o Ch. 14

6. Topic: Equities

Learning Objectives

The candidate will understand the variety of equity investments and strategies available for portfolio management.

Learning Outcomes

The Candidate will be able to:

- a) Explain the nature and role of equity investments within portfolios that may include other asset classes.
- b) Demonstrate an understanding of the basic concepts surrounding passive, active, and semi active (enhanced index) equity investing, including managing exposures.
- c) Explain the basic active equity selection strategies including value, growth and combination approaches.
- d) Demonstrate an understanding of equity indices and their construction, including distinguishing among the weighting schemes and their biases.
- e) Identify methods for establishing passive exposure to an equity market;
- f) Compare techniques for characterizing investment style of an investor;
- g) Recommend and justify, in a risk–return framework, the optimal portfolio allocations to a group of investment managers;
- h) Describe the core-satellite approach to portfolio construction with a completeness fund to control overall risk exposures;
- i) Explain alpha and beta separation as an approach to active management and demonstrate the use of portable alpha;
- j) Describe the process of identifying, selecting, and contracting with equity managers.

- Managing Investment Portfolios: A Dynamic Process, Maginn & Tuttle, 3rd Edition, 2007
 - o Ch. 7 Equity Portfolio Management
- QFIC-110-15: Liquidity as an Investment Style

7. Topic: Investment Policy

Learning Objectives

The candidate will understand how to develop an investment policy including governance for institutional investors and financial intermediaries.

Learning Outcomes

The Candidate will be able to:

- a) Explain how investment policies and strategies can manage risk and create value.
- b) Identify a fiduciary's obligations and explain how they apply in managing portfolios.
- c) Determine how a client's objectives, needs and constraints affect investment strategy and portfolio construction. Include capital, funding objectives, risk appetite and risk-return trade-off, tax, accounting considerations and constraints such as regulators, rating agencies, and liquidity.
- d) Incorporate financial and non-financial risks into an investment policy, including currency, credit, spread, liquidity, interest rate, equity, insurance product, operational, legal and political risks.

- Managing Investment Portfolios: A Dynamic Process, Maginn & Tuttle, 3rd Edition, 2007
 - o Ch. 1 & 3
- QFIC-108-13: Managing your Advisor: A Guide to Getting the Most Out of the Portfolio Management Process

8. Topic: Asset Allocation

Learning Objectives

The candidate will understand the theory and techniques of portfolio asset allocation.

Learning Outcomes

The Candidate will be able to:

- a) Explain the impact of asset allocation, relative to various investor goals and constraints.
- b) Propose and critique asset allocation strategies.
- c) Evaluate the significance of liabilities in the allocation of assets.
- d) Incorporate risk management principles in investment policy and strategy, including asset allocation
- e) Understand and apply the concept of risk factors in the context of asset allocation.

- Managing Investment Portfolios: A Dynamic Process, Maginn & Tuttle, 3rd Edition
 - o Ch. 5
- QFIC-106-13: Chapter 10 of Modern Investment Management: An Equilibrium Approach
- QFIC-107-13: Revisiting the Role of Insurance Company ALM within a Risk Management Framework
- QFIC-111-16: Stop Playing With Your Optimizer
- QFIC-112-16: Risk Factors as Building Blocks for Portfolio Diversification: The Chemistry of Asset Allocation