
SOCIETY OF ACTUARIES
Enterprise Risk Management – General Insurance Extension

Exam ERM-GI

Date: Friday, April 28, 2017

Time: 8:30 a.m. – 12:45 p.m.

INSTRUCTIONS TO CANDIDATES

General Instructions

1. This examination has a total of 80 points.

This exam consists of 9 questions, numbered 1 through 9.

The points for each question are indicated at the beginning of the question. Questions 8 and 9 pertain to the extension readings and/or the Case Study, which is enclosed inside the front cover of this exam booklet.

2. Failure to stop writing after time is called will result in the disqualification of your answers or further disciplinary action.
3. While every attempt is made to avoid defective questions, sometimes they do occur. If you believe a question is defective, the supervisor or proctor cannot give you any guidance beyond the instructions on the exam booklet.

Written-Answer Instructions

1. Write your candidate number at the top of each sheet. Your name must not appear.
2. Write on only one side of a sheet. Start each question on a fresh sheet. On each sheet, write the number of the question that you are answering. Do not answer more than one question on a single sheet.
3. The answer should be confined to the question as set.
4. When you are asked to calculate, show all your work including any applicable formulas.
5. When you finish, insert all your written-answer sheets into the Essay Answer Envelope. Be sure to hand in all your answer sheets because they cannot be accepted later. Seal the envelope and write your candidate number in the space provided on the outside of the envelope. Check the appropriate box to indicate Exam ERM-GI.
6. Be sure your written-answer envelope is signed because if it is not, your examination will not be graded.

Tournez le cahier d'examen pour la version française.

CASE STUDY INSTRUCTIONS

The case study will be used as a basis for some examination questions. Be sure to answer the question asked by referring to the case study. For example, when asked for advantages of a particular plan design to a company referenced in the case study, your response should be limited to that company. Other advantages should not be listed, as they are extraneous to the question and will result in no additional credit. Further, if they conflict with the applicable advantages, no credit will be given.

****BEGINNING OF EXAMINATION****

1. (10 points) DML is a large life insurance company and is due to report its economic capital (EC) to the regulators. DML currently offers three main products:

- **Single premium immediate annuity (SPIA)**
 - Level payments are guaranteed for life.
 - The current mortality assumption is based on DML's experience, but the experience data are not fully credible.
 - One set of assumptions is used for the entire block.
- **5-year deferred annuity**
 - The credited rate is guaranteed for the term of the contract.
 - The death benefit is equal to the book value of the account.
 - There are no surrender charges after 2 years.
- **Participating whole life insurance**
 - This product provides a level death benefit plus accrued dividend.
 - The dividend is based on the difference between actual rates of mortality and interest versus rates assumed in the contract.
 - There is currently no more room to pass adverse experience to policyholders.
 - This product is sold in three different countries but the mortality assumption is based on the DML's experience in its home country.

The assets supporting the DML liabilities are corporate bonds with an average duration of 10 years. The liability duration is 17 years.

(a) (2 points) Describe two important considerations for measuring and modeling each of the following risks for DML:

- Mortality risk
- Interest rate risk.

(b) (5 points)

(i) Explain how mortality and interest rate risks interact within each of DML's three main products as well as across products. Use examples to illustrate your response.

(ii) Describe the following approaches to aggregate EC:

- Correlation
- Copulas
- Multivariate methods

(iii) Recommend an appropriate capital aggregation approach for determining the DML's EC. Justify your answer.

1. Continued

(c) (*3 points*) You are reviewing DML's model governance procedures. All you found was evidence of the following three activities:

- Model output should be validated by comparing the projected premiums and benefits from the EC model with those from the cash flow testing model for a set of ten random policies.
- All individual risk factors should be validated independently and in aggregate.
- Comprehensive documentation of model output should exist to support model validation.

(i) Evaluate how each of these activities adhere to core model validation principles.

(ii) Recommend steps that DML should implement to enhance its model governance procedures.

- 2.** (8 points) You are an actuarial student at CMP Financial, an insurance company specializing in fire indemnity insurance. CMP Financial has a stop-loss reinsurance agreement with XYZ Re that reimburses aggregate monthly claims in excess of \$130,000. CMP Financial receives an experience refund at the end of any calendar year in which no reimbursements are paid by XYZ Re.

Your boss, Stan, asks for your assistance with modeling aggregate monthly claims activity. Stan would like you to analyze claims using a Generalized Pareto Distribution (GPD).

In addition to providing summary statistics for historical aggregate monthly claim amounts for the block, Stan has also calculated estimates for the GPD parameters at various threshold percentiles.

Average Aggregate Monthly Claim = \$12,200

Standard Deviation of Aggregate Monthly Claim = \$53,000

Percentile	Aggregate Monthly Claim Amount in \$ million	ξ	β
90 th	0.095	0.12	0.05
91 st	0.100	0.13	0.05
92 nd	0.104	0.13	0.05
93 rd	0.110	0.15	0.04
94 th	0.115	0.15	0.04
95 th	0.123	0.14	0.04
96 th	0.134	0.14	0.04
97 th	0.147	0.14	0.04

GPD's cumulative distribution function is

$$F(x) = 1 - \left(1 + \xi \frac{x-u}{\beta}\right)^{-\frac{1}{\xi}}, x \geq u$$

(a) (2 points)

- (i) Explain considerations when selecting a threshold value for parameterizing a GPD.
- (ii) Recommend an appropriate threshold level. Justify your response.

2. Continued

- (b) (*3 points*) Assume that aggregate monthly claim amounts are independent of prior months' claim activity. Consider the following two claim models.
- I. The GPD model using the threshold you recommended in part (a)
 - II. A normal approximation
- Calculate the probabilities, for each claim model, that:
- (i) No claim reimbursement will be made in a given month.
 - (ii) CMP will receive the experience refund at the end of the upcoming calendar year.
- (c) (*3 points*) Stan is currently preparing cash flow projections for the upcoming calendar year and would like to incorporate the results of your analysis.
- (i) Explain why the GPD model more appropriately reflects the true likelihood of payment of the experience refund.
 - (ii) Describe two shortcomings of the normal approximation in the context of modeling CMP's aggregate claim distribution.

- 3.** (12 points) You are a new CERA hired by the finance department of Protection Partners (PP), a clearinghouse that trades derivatives and other financial instruments. PP has maintained an AA rating ever since its inception. You are analyzing a new credit derivative issued by XEN Bank that PP wishes to offer.

You are given:

- The annual risk free rate is 5%

ABC Bond

- Issued in \$100 notional amount increments
- 3 year term
- Pays 15% annual coupons
- If the bond defaults, no coupon is paid, and the bondholder immediately receives whatever principal is recovered, terminating the bond contract.
- The probabilities of default are:
 - 5% in each of years 1 and 2
 - 10% in year 3
- The recovery rates given default are:
 - 0% with probability 50%
 - 50% with probability 30%
 - 75% with probability 20%

ABC Credit Derivative

- The derivative is on ABC bonds
- Each \$100 ABC Credit Derivative backs \$100 in ABC bonds
- When an ABC bond defaults, the ABC Credit Derivative will
 - Immediately pay the defaulted coupon
 - Pay any future coupons at their normal due date
 - Pay the unrecovered principal (with no adjustment for interest) at the planned ABC bond maturity.

- (a) (2.5 points) Determine the price of the ABC Credit Derivative at issue assuming no taxes or profit margin. Show your work.

3. Continued

- (b) (*3.5 points*)
- (i) Describe how each of the following credit enhancers mitigates credit risk.
- I. Collateral
 - II. Netting Agreement
 - III. Walkaway features
- (ii) Explain whether the credit enhancers listed above are appropriate for the purchaser of the ABC Credit Derivative contract to use with PP.
- (c) (*3.5 points*)
- (i) Define Potential Future Exposure (PFE) and Expected Positive Exposure (EPE).
- (ii) Identify which of PFE or EPE is more appropriate for capital purposes.
- (iii) From PP's perspective:
Determine the PFE to PP from the ABC Credit Derivative assuming a 100% confidence level and a 0% interest rate. Explain your reasoning.
- (iv) From the ABC Credit Derivative owner's perspective:
Determine the PFE from the ABC Credit Derivative assuming a 100% confidence level and a 0% interest rate. Explain your reasoning.
- (d) (*1.5 points*) PP is putting together a brochure to help with understanding the ABC Credit Derivative. You have been asked to draft the answer to the following question in the brochure:
- “Q: For this product, you list a value for the Potential Future Exposure that is very different from the Expected Positive Exposure. Which value should matter more to an investor?”
- Prepare an answer to this question indicating which one is more important.
- (e) (*1 point*) Other than minimizing their credit exposure to ABC, explain how ABC bondholders could benefit from owning the ABC Credit Derivative.

- 4.** (9 points) You are given the following capital information on company XYZ for its three lines of business.

Line of Business	Stand-Alone Capital (\$ million)
Annuities	20
Life	6
Auto	14

A matrix for the risk correlation between lines of business is provided below.

	Annuities	Life	Auto
Annuities	1	0.8	0.4
Life	0.8	1	0.5
Auto	0.4	0.5	1

- (a) (2 points) Demonstrate that the diversification benefit for XYZ is \$6.35 million. Assume that risks within lines of business are normally distributed.
- (b) (4 points) Calculate the capital allocation using the following two methods:
- I. Pro-rata
 - II. Discrete marginal contribution
- (c) (3 points)
- (i) Compare the following capital allocation approaches:
- I. Standalone
 - II. Pro-rata
 - III. Discrete marginal contribution
- (ii) Recommend a capital allocation method for XYZ. Justify your response.

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5. (7 points) You are asked to calculate economical capital (EC) for the Long Term Care (LTC) business of the XYZ Insurance Company. This block of business has the following characteristics:

- Level premium for life
- Policy pays certain qualified expenses incurred to assist with activities of daily living
- Liability duration is approximately 40 years at issue
- Supporting assets are invested in government securities and high-yield corporate bonds
- Interest rate swaps and options are used to manage interest rate risk
- Economic Liability is based on best estimate assumptions.

(a) (2 points) You are evaluating the following risk categories as related to the LTC business:

- I. Insurance Risk
- II. Credit Risk
- III. Market Risk

- (i) Describe the specific risks in each of above categories.
- (ii) Rank the risks. Justify your response.

(b) (2 points) XYZ uses the deterministic stress tests to calculate EC.

Describe how you would select shocks for a deterministic stress test.

5. Continued

(c) (3 points) XYZ uses the following deterministic shocks:

- +/- 1% parallel shift in interest rates
- +/- 20% in lapse rates in all durations
- 10% increase in claims

XYZ's Chief Risk Officer (CRO) commented that:

- I. Interest rate shock may not capture the inherent interest risk in this line of business.
 - II. The shock design seems overly simplistic to reflect all the material risks.
-
- (i) Explain the CRO's concerns.
 - (ii) Provide recommendations to address the CRO's concerns.

- 6.** (8 points) LMN Insurance Company, a BBB-rated insurer, plans to expand into a new market. The CFO of LMN is exploring the possibility of securing additional capital using Special Purpose Vehicles (SPV) to fund the expansion. The CFO thinks that the current financing rates are too high for what he thinks is a very low risk venture.

Major rating agencies recently changed LMN's credit rating outlook to negative.

LMN holds high-quality commercial real estate investments in a fast-growing city. This accounts for more than half of its asset portfolio.

The CFO suggests using the real estate portfolio to collateralize the bonds issued by an SPV to finance the expansion.

- (a) (0.5 point) Define an SPV.
- (b) (3 points) Illustrate how LMN can structure this SPV to obtain financing.
- (c) (2 points) Identify four of the key risks and four of the key benefits of the SPV transaction for LMN.
- (d) (1 point) Recommend whether LMN should proceed with the SPV transaction based on your response to (c). Justify your response.
- (e) (1.5 points) Describe three other strategic considerations that LMN would need to address prior to initiating the SPV transaction.

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- 7.** (6 points) XYZ is an insurance company that sells life insurance and hurricane insurance. In order to grow, XYZ is investigating selling a new tornado insurance product. For hurricane and tornado insurance combined, XYZ is willing to absorb a loss of \$100 million, which is 10% of expected company-wide profits.

The CFO has asked you to quantify the risk of offering the tornado insurance. An outside consultant provided you with the sales data from several other companies that sell tornado insurance. The data for one company is shown below.

Date	Sales in Millions
Jan. 2010	15.34
Feb. 2011	18.23
Mar. 2012	18.23
Apr. 2013	18.23
May 2014	99.99
Jun. 2015	19.74

- (a) (3 points) You are reviewing ASOP 23 prior to performing your work.
- Describe concerns you have with the data you have been provided.
 - Identify two key data-related disclosures that you would include as part of your actuarial report on the profitability of the tornado insurance.

7. Continued

Your colleague has estimated the 90% VaR for hurricane product's losses over 5 years to be \$60 million; and the corresponding CTE to be \$90 million.

Your calculations for the tornado product's losses show a 90% VaR over 5 years of \$75 million, with a corresponding CTE of \$120 million.

- (b) *(1.5 points)* Explain whether VaR or CTE is the more appropriate risk measure to use in this situation.
- (c) *(1.5 points)* The CFO has directed you to use the 90% VaR measure with complete independence between hurricane and the tornado products.

Recommend whether or not XYZ should offer the tornado product. Justify your response.

***Questions 8-9 pertain to the Case Study and/or extension readings.
Each question should be answered independently***

- 8.** (11 points) You are a newly appointed regulator in Atlantis. Atlantis wants to modernize its regulatory framework.

You are looking at a sample block of Personal Auto (PA) policies to compare the regulatory capital requirements under the following three jurisdictions:

- I. United States
- II. Canada
- III. European Union

You have made the following assumptions for the sample block (in \$millions):

Assets Invested in Risk Free Government Bonds	800
Discounted Best Estimate on Unpaid Claims (Best Estimate Liability)	250
Undiscounted Best Estimate on Unpaid Claims	270
Cost-of-Capital Risk Margin under Solvency II	18
Assumed Margin for Claims Development under the Canadian Valuation Framework	10%
Net Written Premium	350
Unearned Premium Reserve	175
Premium Liability Reflecting the Future Economic Profit in the Year which the Business was Written	143
Deferred Policy Acquisition Expense (as a percentage of Net Written Premium)	8%

- (a) (5 points)

- (i) Calculate the amount of available capital under the three jurisdictions above (I, II, and III).
- (ii) Provide reasons why available capital differs among the three capital frameworks.

8. Continued

- (b) (2 points) You have calculated components of the regulatory capital requirement for the sample block under the RBC, MCT, and Solvency II regimes, as follows:

(Amounts in \$millions)

	Premium Risk	Reserve Risk
Regime A	50	40
Regime B	105	100
Regime C	15	25

	Catastrophe Risk
Regime D	55
Regime E	0
Regime F	2

Identify the regime associated with each of the following:

(i) A, B and C

(ii) D, E and F

Explain your rationale.

- (c) (2 points) Describe the impact increasing interest rates would have on available capital, required capital, and free capital for each framework (US, Canada, European Union). Justify your response.
- (d) (1 point) You have calculated the Minimum Capital Requirement (MCR) for the sample block to be \$100 million and have set the MCR to be equal to 40% of the total Solvency Capital Requirement.

Calculate the amount of free capital under Solvency II. Show your work.

- (e) (1 point) Your boss proposes that Atlantis should use the Canadian statutory accounting framework for assets and liabilities on the balance sheet with Solvency II for regulatory capital.

Critique this proposal.

***Questions 8-9 pertain to the Case Study and/or extension readings.
Each question should be answered independently***

- 9.** (9 points) Each year Pryde provides portfolio information to its reinsurance broker for the modeling of its catastrophe (CAT) risks. Based on the modeling results for a 1-in-250 return period, Pryde determines the amount of catastrophe reinsurance it needs to purchase.

This year the broker used a new version of the CAT model for earthquake risks. Pryde's senior management is concerned about the accuracy of the results under this new version and decides to initiate a review of the model.

- (a) (1 point) Describe the components of the CAT earthquake model that Pryde should review.
- (b) (2 points) Upon reviewing the model, Pryde realizes the following portfolio information had not been provided to the broker before he ran the model:
- I. Exposure data for each risk on a postal code level. Previously the data was provided on a county or regional level.
 - II. Under the insurance policy sold by Pryde, Pryde will not pay the first \$20,000 loss amount to the policyholder in an earthquake event (e.g. if the loss is \$15,000, Pryde will not pay anything and the policyholder has to bear all; if the loss is \$100,000, Pryde will pay \$80,000).
 - III. Many policies were written on a loss limit basis and subsequently the loss limits were recorded in the system (e.g. a risk has a Total Sum Insured of \$3,000,000, but the insurance policy only indemnifies the losses up to \$2,000,000).
 - IV. Big Re and Pryde have negotiated a reduction in the per occurrence annual limit from \$7,500,000 to \$3,500,000 upon renewal of the reinsurance.

Assess the marginal impact of including each piece of information on the 1-in-250 return period modeling result of Pryde prior to reinsurance recoveries from Bigger Re. Justify your answers.

9. Continued

- (c) (*1.5 points*) Pryde's senior management has reviewed the CAT model results for both hurricanes and earthquakes and has expressed the following concerns:
- I. A severe hurricane that occurred last year has only caused loss amounts of \$10M to Pryde. According to the media, this was a 1-in-250 year event. It appears that our CAT risk may be overestimated.
 - II. According to the broker, this new version of the earthquake model took into consideration volcanic eruptions and tsunamis. Currently Pryde's Homeowners policy does not cover tsunami, though its Auto policy does. It seems that the CAT risk may be further driven up by this new version.

Prepare a response addressing the two concerns raised by Pryde's Senior Management.

- (d) (*3 points*) Recommend an action plan that Pryde can take to address concerns with the model results. Your recommendation should contain at least three actions addressing the concerns above.
- (e) (*1.5 points*) In 2012, Hawthorne had estimated standalone economic capital for catastrophe risk at \$41,800,000. Since that time, Pryde has increased that amount to \$45,000,000. Archie Daniels, CFO, has said that with the current reinsurance coverage in place it would not be possible for net losses to reach that amount.
- (i) Describe situations where Pryde's net losses after all reinsurance recoveries over a one-year period could equal or exceed \$45,000,000.
 - (ii) As indicated above, the per occurrence aggregate limit for Big Re will be reduced to \$3,500,000 from \$7,500,000.

Suggest changes to its other reinsurance programs such that Pryde could maintain its standalone economic capital for CAT risk unchanged.

****END OF EXAMINATION****

USE THIS PAGE FOR YOUR SCRATCH WORK