

**November, 2001- Course 8P  
Society of Actuaries**

**\*\*BEGINNING OF EXAMINATION\*\***

- 1.** (8 points) A new Company has established a contributory pension plan on January 1, 2001. You are given:

**Plan Provisions**

Retirement benefit:	The greater of: (i) 2% of career average earnings, or (ii) actuarial equivalent of 200% of employee contributions accumulated at the fund rate of return
Normal form of payment:	5 years certain and life thereafter, payable monthly in advance
Normal retirement age:	65
Employee contributions:	4% of annual earnings, payable at the beginning of the year
Termination or death benefit:	Lump sum payment of 200% of employee contributions accumulated at the fund rate of return
Actuarial equivalence:	At valuation assumptions

**Actuarial Assumptions and Methods**

Interest rate:	6.5% per annum						
Retirement age:	65						
Salary increases:	4.0% per annum						
Termination rates:	<table><thead><tr><th><u>Attained Age</u></th><th><u>Year-end rates</u></th></tr></thead><tbody><tr><td>Up to 34</td><td>10%</td></tr><tr><td>35 and over</td><td>0%</td></tr></tbody></table>	<u>Attained Age</u>	<u>Year-end rates</u>	Up to 34	10%	35 and over	0%
<u>Attained Age</u>	<u>Year-end rates</u>						
Up to 34	10%						
35 and over	0%						
Other pre-retirement decrements:	None						
Actuarial cost method:	Unit Credit						
Actuarial value of assets:	Market value						

$$\ddot{a}_{65:\overline{5}|}^{(12)} = 10.4$$



**1. (CONTINUED)**

**Participant Data**

	<u>Group J</u>	<u>Group K</u>
Number of employees	30	30
Age at 1/1/2001	30	50
2001 earnings per employee	\$40,000	\$60,000

- (a) Calculate the employer normal cost for 2001.
- (b) The employer contributes the employer normal cost on January 1, 2001. The fund earns 8% during 2001. At December 31, 2001, 6 employees in Group J terminate and 1 Group K employee dies.

Determine the plan's assets and accrued liability at January 1, 2002.

- (c) Calculate the gains and losses by source for 2001.

Show all work.

2. (4 points) The CEO of ABC Company will receive a pension on retirement at age 65.

You are given the following as at January 1, 2001:

CEO's Age:	50
CEO's Service:	10 years
CEO's Salary:	\$300,000 per annum
Pension Benefit:	2% of final year's salary times years of service
Form of Payment:	Life only, payable monthly in advance

The pension is paid from a basic plan and a supplemental executive plan. The maximum annual pension payable under the Basic Plan is \$2,000 times years of service. The remainder is paid from the Supplemental Plan. ABC pre-funds the CEO's entire pension.

**Actuarial Assumptions and Method**

	<u>Basic Plan</u>	<u>Supplemental Plan</u>
Interest rate:	8% per annum	6% per annum
Salary scale:	5% per annum	5% per annum
Normal retirement age:	65	65
Pre-retirement decrements:	None	None
Actuarial Cost Method:	Projected Unit Credit (prorated on service)	Entry Age Normal (level % of pay)
$\ddot{a}_{65}^{(12)}$	9.0	11.0

- (a) Calculate the normal cost for the Basic Plan at January 1, 2001.
- (b) Calculate the normal cost for the Supplemental Plan at January 1, 2001.

Show all work.

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3. (8 points) You are the actuary for a company that sponsors a non-contributory defined benefit pension plan.

You are given:

**Plan Provisions**

Retirement benefit:	\$20 per month, per year of service
Normal form of pension:	Life only, payable monthly in advance
Normal retirement age:	60
Early retirement reduction:	5% per year that retirement precedes age 60
Other ancillary benefits:	None

**Actuarial Assumptions and Method**

Interest rate:	7.0% per annum
Retirement rates:	10% per annum, at the beginning of each year, from age 57 through 59; 100% at age 60
Pre-retirement decrements:	None
Actuarial cost method:	Unit Credit

$$\ddot{a}_{57}^{(12)} = 10.0$$

$$\ddot{a}_{58}^{(12)} = 9.0$$

$$\ddot{a}_{59}^{(12)} = 8.0$$

$$\ddot{a}_{60}^{(12)} = 7.0$$

**Financial Information**

Assets at January 1, 2001:	\$100,000
2001 employer contribution:	None
Fund rate of return in 2001:	2%

**Participant Data as at January 1, 2001**

<u>Member</u>	<u>Age</u>	<u>Service</u>
Jean	57	25
Kelly	58	29

**3. (CONTINUED)**

- (a) Calculate the unfunded accrued liability and normal cost as at January 1, 2001.
- (b) On December 31, 2001, Kelly retires. On December 31, 2001, Pat transfers into the plan at age 45 and \$10,000 is transferred to recognize 10 years of Pat's prior service.

Calculate the unfunded accrued liability as at January 1, 2002.

- (c) Calculate the gains and losses by source for 2001.

Show all work.

4. (4 points) You are the actuary for a company that sponsors a defined benefit pension plan.

You are given:

**Plan Provisions**

Retirement benefit:	\$30 per month, per year of service
Normal form of payment:	Five years certain and life thereafter, payable monthly in advance
Optional form of payment:	Actuarially equivalent 75% joint and survivor annuity
Normal retirement age:	65
Early retirement reduction:	Actuarial equivalence
Other ancillary benefits:	None
Actuarial equivalence:	Based on valuation assumptions

**Actuarial Assumptions and Method**

Interest rate:	7.0% per annum
Retirement age:	65
Pre-retirement decrements:	None
Actuarial cost method:	Entry Age Normal

<u>Member</u>	<u>Spouse</u>	<u>Member: Spouse</u>
$\ddot{a}_{60}^{(12)} = 10.8387$	$\ddot{a}_{57}^{(12)} = 12.5296$	$\ddot{a}_{60:57}^{(12)} = 9.7460$
$\ddot{a}_{65}^{(12)} = 9.7004$	$\ddot{a}_{62}^{(12)} = 11.6834$	$\ddot{a}_{65:62}^{(12)} = 8.5126$
$\ddot{a}_{70}^{(12)} = 8.4642$	$\ddot{a}_{67}^{(12)} = 10.6379$	$\ddot{a}_{70:67}^{(12)} = 7.1863$
${}_5P_{60} = 0.9446$		
${}_5P_{65} = 0.9039$		

The following member retires on January 1, 2001:

	<u>Data as at January 1, 2001</u>
Member's age:	60
Spouse's age:	57
Years of service:	35



**4. (CONTINUED)**

- (a) Calculate the experience gain or loss on January 1, 2001 caused by the retirement of the member.
- (b) Calculate the member's pension under the optional form of payment.

Show all work.

5. (6 points) Your client sponsors a non-contributory defined benefit pension plan.

You are given:

**Plan Provisions**

Retirement benefit:	1.5% of career average earnings
Normal form of payment:	Life only, payable monthly in advance
Normal retirement age:	65
Earliest retirement age:	55
Early retirement reduction:	3% per year that retirement precedes age 65

**Actuarial Assumptions**

Interest rate:	6.5% per annum
Salary increase rate:	4.0% per annum
Retirement age:	60
Pre-retirement decrements:	None
Actuarial value of assets:	Market value

$$\ddot{a}_{60}^{(12)} = 11.4$$

Assets at January 1, 2001 equal the January 1, 2001 Unit Credit accrued liability.

**Participant data as at January 1, 2001**

<u>Members</u>	<u>Age</u>	<u>Service (Years)</u>	<u>2001 Earnings</u>	<u>Accrued Benefit</u>
J	41	11	\$50,000	\$6,000
K	53	18	60,000	12,000

- (a) Determine the normal cost under the Frozen Initial Liability method given that this method was adopted on January 1, 2001.
- (b) Determine the normal cost under the Individual Aggregate cost method, assuming that assets allocated to each member equal their respective Unit Credit accrued liability.

Show all work.

**\*\*END OF EXAMINATION\*\***