#### **2019 Predictive Analytics Symposium**

Session 24: B/I - How Can an Actuary Become a Data Scientist?

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# How Actuary can become Data Scientist

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RGA

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### Agenda

- What actuary already knew
- What actuary may not know
- Basic models beyond OLS
  - Generalized Linear Model
  - Decision tree & more
  - Clustering & more
- What is next?
- Conclusion, Q & A



### What actuary already knew

- Are you familiar with the following terms?
  - Ordinary Least Square (OLS)
  - Time Series
- Linear regression model

 $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_n X_n + \varepsilon = \Sigma_i \beta_i X_i + \varepsilon = \overline{X} \overline{\beta} + \varepsilon$ 

- Y target variable,  $X_i$  predictor variable,  $\varepsilon$  error term/noise
- $\beta_i$  parameters to be estimated
- Underlying Assumptions for a valid LM
  - Y: homogeneity, representative of population, independence between observations
  - X: fixed, error-free
  - Normality,  $\varepsilon \sim N(0,\sigma^2)$
  - (linearity)





#### **Ordinary Least Squares**

if normal distribution

Ordinary Least Squares(OLS)

 $\hat{\beta} = \arg\min(RSS) = \arg\min(\Sigma_i(\hat{y}_i - y_i)^2) = \arg\min(\Sigma_i(\Sigma_i\beta_iX_{ii} - y_i)^2)$ 

For a simple regression •

 $\widehat{\beta_1} = (\Sigma x_i y_i - \frac{1}{n} \Sigma x_i \Sigma y_i) / (\Sigma x_i^2 - \frac{1}{n} (\Sigma x_i)^2), \quad \widehat{\beta_0} = \overline{y} - \widehat{\beta_1} \overline{x}$ 

- Identical to Maximum likelihood estimator
  - More robust and consistent approach

 $\hat{\beta} = \arg \max(L(X, Y, \beta)) = \arg \min(-\ln(L(X, Y, \beta))) = \arg \min(\Sigma_i (y_i - \hat{y}_i(\mu_i))^2)$ 

 $\succ$  Use adj  $R^2$  to compare fitness of models

- $1 = \frac{RSS}{TSS} + \frac{ESS}{TSS}$  portion that has been explained by OLS model portion of TSS for the error

Define  $R^2 = \frac{RSS}{TSS} = 1 - \frac{ESS}{TSS} = \frac{\sum_i (Y_i - \widehat{Y}_i)^2}{\sum_i (Y_i - \overline{Y})^2}$ , but it is biased Adjusted  $R^2 = 1 - \frac{ESS}{TSS} * \frac{n-1}{n-k} = 1 - (1-R^2) * \frac{n-1}{n-k}$ 



### Why actuary did not use OLS

- Processes are inherently linear, or can be well-approximated by LM
- Effectiveness & Completeness
  - OLS makes very efficient use of the data; good results with relatively small data sets
  - Identical to maximum likelihood estimation
- Easy to understand and communicate
  - theory is well-understood; Results are easy to communicate
- Great! but wait …
- There are several issues with OLS
  - Validation of assumptions Normal w/ constant  $\sigma^2$ , independent, homogeneous
  - Unbounded data, non-negative value
- > How about insurance application? Distribution of data, variance structure
  - Binomial for rate (mortality/lapse/UW, etc.),  $\sigma^2 \sim r(1-r)$
  - Poisson for claim count, ~ mean
- OLS may not be applicable in insurance, but you know lots about modeling

### What actuary may not know



#### Machine Learning & Statistical Techniques

- Generalized Linear Model (GLM)
- Random Forest
- XG-boost machine
- Gradient Boosting
- Ada Boosting
- Support vector machine
- Ensemble method
- Survey Data Analysis
- Genetic Algorithms
- Sentiment Analysis
- Markov chain Monte Carlo (MCMC)
- Optimization Methods
- Feature engineering

- Decision Trees (CART/MARS)
- Neural Networks / Deep learning
- Bayesian Analysis
- Classification/Association
- Analysis of Variance
- Mixed Models
- Categorical Data Analysis
- Multivariate Analysis
- Survival Analysis
- Cluster Analysis (e.g. K-Means)
- Non-Parametric Analysis
- Text mining



# **PM terminology**

Supervised vs. Unsupervised	<ul> <li>Supervised: estimate expected value of Y given values of X</li> <li>Example: OLS/LM, GLM, Cox, NN, etc.</li> <li>Unsupervised: find interesting patterns amongst X; no target Y</li> <li>Example: Clustering, Correlation / Principal Components</li> </ul>
Classification vs. Regression	<ul> <li>Classification: segment observations into 2 or more categories</li> <li>Example: fraud vs. legitimate, lapsed vs. retained, UW class</li> <li>Regression: predict a continuous amount,</li> <li>Example: dollars of loss for a policy, ultimate size of claim</li> </ul>
Parametric vs. Non-Parametric	<ul> <li>Parametric Statistics: probabilistic model of data</li> <li>Example: Poisson Regression(claims count), Gamma (claim amount)</li> <li>Non-Parametric Statistics: no probability model specified</li> <li>Example: classification trees, NN</li> </ul>



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### **Generalized Linear Model**

#### Generalized Linear Model(GLM)

- Major focus of PM in insurance industry
- Include most distributions related to insurance
- Great flexibility in variance structure
- OLS model is a special case of GLM
- (Relatively) Easy to understand and communicate
- Multiplicative model intuitive & consistent with insurance practice

#### 3 components

- Random component
- Systematic component
- link function



# **Generalized Linear Model**

Random component

Observations  $Y_1, \ldots, Y_n$  are independent w/ density from the exponential family  $(y_i\theta_i - b(\theta_i))$ 

$$f_i(y_i;\theta_i,\phi) = exp\left\{\frac{y_i \sigma_i - b(\sigma_i)}{a_i(\phi)} + c(y_i,\phi)\right\}$$

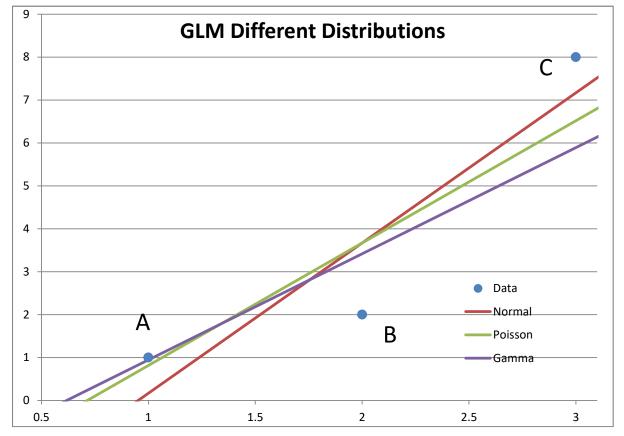
From maximum likelihood theory,

$$E(Y) = \mu = b'(\theta), \quad var(Y) = b''(\theta)a(\phi) = a(\phi)V(\mu)$$

- Each distribution is specified in terms of mean & variance
- Variance is a function of mean

	Normal	Poisson	Binomial	Gamma	InverseGaussia n
Name	$N(\mu, \sigma^2)$	$P(\mu)$	$B(m,\pi)/m$	$G(\mu, \nu)$	$IG(\mu,\sigma^2)$
Range	$(-\infty,+\infty)$	(0,+∞)	(0,1)	(0,+∞)	(0,+∞)
$b(\theta)$	$\theta^2$	$e^{ heta}$	In(1+e <sup>θ</sup> )	$-\ln(-\theta)$	$-(-2\theta)^{1/2}$
$\mu( heta)$	heta	$e^{ heta}$	$e^{\theta}/(1+e^{\theta})$	$-1/\theta$	$(-2\theta)^{-1/2}$
$V(\mu)$	1	μ	$\mu(1-\mu)$	$\mu^2$	$\mu^3$

### Why distribution will affect results



#### Variance of different distributions

- Gaussian, constant
- Poisson, ~ mean
- ➢ Gamma, ∼ mean^2



# **Generalized Linear Model**

### > Systematic component A linear predictor $\eta_i = \sum_j x_{ij}\beta_j = X\beta$ for observation *i*

#### link function

 $\eta_i = g(\mu_i)$ , random & systematic are connected by a smooth & invertible function

	Identity	Log	Logit	Reciprocal
$g(\mu_i)$	x	$\ln(x)$	$\ln(\frac{x}{1-x})$	1/x
$g^{-1}(\eta_i)$	x	e <sup>x</sup>	$\frac{e^x}{1+e^x}$	1/x

Log is unique in insurance application s.t. all parameters are multiplicative

- $y = \exp(\sum_j x_{ij}\beta_j) = \prod_j \exp(x_{ij}\beta_j) = \prod_j \exp(\beta_j)^{x_{ij}} = \prod_j f_j^{x_{ij}}$
- Consistent with most insurance practices
- Intuitively easy to understand and communicate



### **Generalized Linear Model**

- > Solve for parameters ( $\beta$ ) by maximum likelihood
  - Closed form for small data and simple model
  - Iterative numerical techniques for large data set & complex model
    - $\beta_{n+1} = \beta_n H^{-1} \cdot s$ , similar to Newton's method  $x_{n+1} = x_n f(x_n)/f'(x_n)$
  - Use statistical analysis application, such as *R*
- Compare OSL and GLM

	Random	Systematic	Link
OLS	Normal only	$n_{i} = \sum_{i} r_{i} \beta_{i}$	$E(y_i) = \eta_i$
GLM	Various distribution	$\eta_i = \sum_j x_{ij} \beta_j$	$g(E(y_i)) = \eta_i$

#### Great flexibility

- Various distribution, variance structure
- Prior weight and the credibility of data
- Offset of data



### Where we go from GLM

#### More regression models

- Survival Models (Cox Proportional Hazard)
- Generalized Additive Models (GAM)
- Multilevel/Hierarchical Linear Model(HLM)
- Support vector machine
  - Instead of a linear boundary that are affected by all data points to separate classes, an optimal boundary is selected to maximize the gap between classes
- Neural network / Deep Learning
  - Logistic model is the simplest neural network model



Decision Tree model, (Classification And Regression Tree - CART)
 ✓ Both classification and regression

✓ Non-parametric approach (no requirement on data structure)

CART tree is generated by repeated partitioning of data set
 Data is split into two partitions (binary partition)
 Partitions can also be split into sub-partitions (recursive)
 Until data in end node(leaf) is homogeneous (more or less)

### Results are very intuitive

- ✓ Identify specific groups that deviate in target variable
- ✓ Yet, algorithm is very sophisticated



#### **Recursive Partitioning**

- Take all data points
- Consider all possible values of all variables
- Select the variable/value  $(X=t_1)$  that produces the greatest "separation"
  - $(X=t_1)$  is called a "split".
  - If  $X < t_1$  then send the data to the "left"; otherwise, to the "right"
- Repeat same process on these two "nodes"
  - Result is a "tree"; uses binary splits
- Stop split data until certain criteria are meet

#### Two Core Questions

- How to find split points
  - Which variable among all, at which value or category, what criterion to use
- When to stop splitting
  - Avoid saturated model



#### Splitting Point

- "Separation" defined in many ways; different for regression & classification
- <u>Regression Trees</u>: use sum of squared errors

$$-SSE_p = \sum_i (y_i - \mu)^2$$

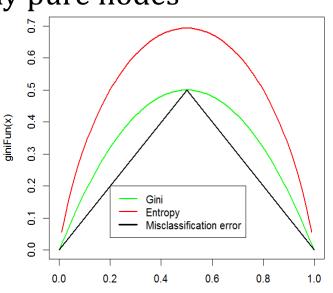
$$-SSE_{c} = \sum_{i} (y_{i}^{L} - \mu^{L})^{2} + \sum_{i} (y_{i}^{R} - \mu^{R})^{2}$$

- Select  $X=t_1$  such that  $\max_{x_i,t}(SSE_P SSE_C)$
- <u>Classification Trees</u>: use measures of purity/impurity
  - Intuition: an ideal tree model would produce completely pure nodes
  - *Gini Index* purity of a node f(p) = p(1 p)

 $f(p) = \sum_i p_i (1 - p_i) = 1 - \sum_i p_i^2$ ,  $p_i = \text{freq of class i}$ 

- *Entropy* - information index f(p) = -plog(p)

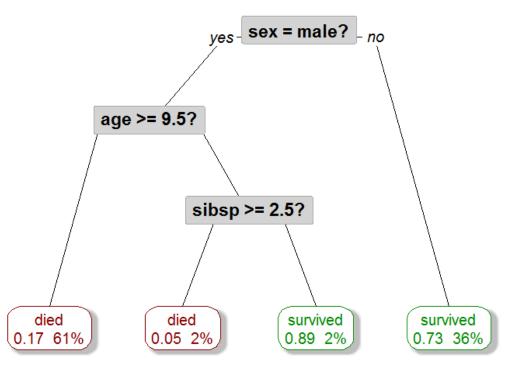
 $f(p) = \sum_i -p_i \log(p_i) = -p \log(p) - (1-p) \log(1-p)$ 



#### Surrogate Splits

- Problem: if missing data on  $x_i$ , we don't know how to assign the object
- Solution: we can use a similar split on another variable that is associated (correlated); we use these (surrogate) splits to assign the object to the class
  - Missing value can be solved in algorithm level



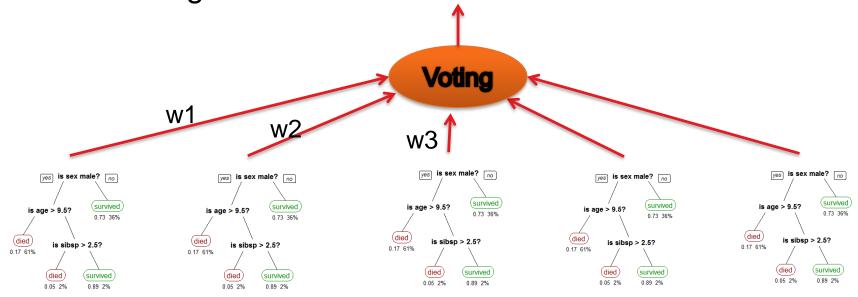




### Where we go from Decision Tree

Decision tree based model

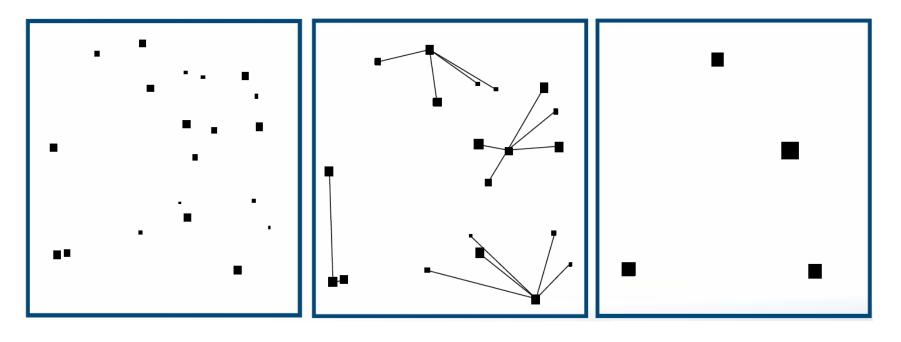
- Random forest
- XG-boost machine
- Gradient Boosting
- Ada Boosting



### Clustering algorithm



- Find similarities in data according to features in data & group similar objects into clusters
- ✓ Unsurprised (no pre-defined), classification, non-parametric
- ✓ How to measure similarities/dissimilarities, e.g. distance
  - Numeric, categorical, and ordinal variables
- Partitioning (k-means), Hierarchical, Density-based, etc.





#### <u>Algorithm</u>

- Partitioning algorithms K-measn/k-medoids
  - Maintain k clusters with k known; place points into their "nearest" cluster
- Hierarchical (Agglomerative)
  - Objects are more related to nearby objects than to objects farther away; objects are connected by distance; how to define "nearby" object

#### K-Means Algorithm

- 1. Select K points as initial centroids, with a given k
- 2. Repeat
- 3. Form K clusters by assign each points to its nearest centroid
- 4. Re-compute the centroids of each cluster
- 5. Until centroids do not change



# **Data Clustering**

#### Define Distance

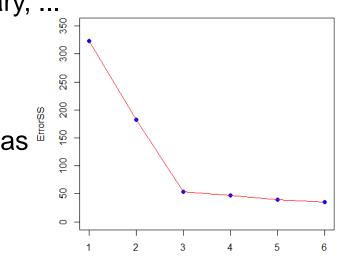
- Euclidean:  $d(x_i, x_j) = (\sum_k (x_{ik} x_{jk})^2)^{1/2}$  (p=2), easy to understand, but not scale invariant
- <u>Manhattan</u>:  $d(x_i, x_j) = \sum_k |x_{ik} x_{jk}|$  (p=1), city-block distance
- <u>Chebychev</u>:  $d(x_i, x_j) = max_k |x_{ik} x_{jk}|$  (p $\rightarrow\infty$ ),
- <u>Minkowski</u>:  $d(x_i, x_j) = (\sum_k (x_{ik} x_{jk})^p)^{1/p}$
- Others like Pearson correlation, Spearman, Canberra, Jaccard, binary, ...

#### Standardization / Normalization

- Values of variables may have different units
- Variable with high variability/range will dominate metric, & lead to bias

### How to determine K

- Business reasons could dictate k
- Try different k, looking at the change in the average distance to centroid, as k increases; error falls rapidly until right k, then changes little



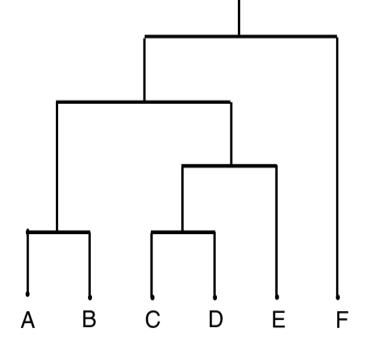


# **Data Clustering**

### Comments on K-Means

- Strength: simple, very efficient, & fast
- Weakness
  - Applicable only when *mean* is defined, (categorical?)
  - Need to know k in advance
  - Unable to handle noisy data & *outliers;* sensitive to outliers
  - Not suitable for clusters with non-convex shapes
  - Maybe sensitive to initialization
- There are variants of *k-means*

#### Hierarchical clustering

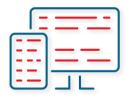


- Bottom up (aglomerative) or top down (divisive/deglomerative) produce a dendrogram
- Important questions how to represent a cluster of more than one point, & how to determine the "nearness" of clusters?
  - Single Link: smallest distance between points
  - Complete Link: largest distance between points
  - Average Link: average distance between points
  - Centroid: distance between centroids



# What is next for Actuary?

- You have solid education background in statistics
- You already have the business knowledge
- Pick up the new skills of data analytics
  - Refresh yourself with the basics of modeling
  - Learn a modeling application / language & practice with examples
  - Attend seminar, conference, training program, etc.
  - Start a project to apply the new skills
  - Link your new skills with your job & practice if possible





### Conclusion

#### Actuary unique position

- Industry knowledge: domain knowledge is key in the predictive modelling process
- Data expertise: data is always the largest issue in data-driven applications



#### **Challenge for actuary**

- Solid math foundation, but need to learn modeling skills and new technology
- Combine the new skills with domain knowledge



#### **Opportunity for actuary**

- Data science is changing the insurance & will revolutionize how we run business
- Actuaries should lead the transforming by becoming data scientist or leading DS



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