



SOCIETY OF  
ACTUARIES®

2019 **ANNUAL  
MEETING**  
& EXHIBIT

October 27-30  
Toronto, Canada

## Session 087: Cashflows: A New Dimension

[SOA Antitrust Compliance Guidelines](#)

[SOA Presentation Disclaimer](#)

# Cashflows: A New Dimension

Michael Carse, FSA EA CERA CFA

Katalin Szeles, FSA FCIA CERA

October 29, 2019



# SOCIETY OF ACTUARIES

## Antitrust Compliance Guidelines

Active participation in the Society of Actuaries is an important aspect of membership. While the positive contributions of professional societies and associations are well-recognized and encouraged, association activities are vulnerable to close antitrust scrutiny. By their very nature, associations bring together industry competitors and other market participants.

The United States antitrust laws aim to protect consumers by preserving the free economy and prohibiting anti-competitive business practices; they promote competition. There are both state and federal antitrust laws, although state antitrust laws closely follow federal law. The Sherman Act, is the primary U.S. antitrust law pertaining to association activities. The Sherman Act prohibits every contract, combination or conspiracy that places an unreasonable restraint on trade. There are, however, some activities that are illegal under all circumstances, such as price fixing, market allocation and collusive bidding.

There is no safe harbor under the antitrust law for professional association activities. Therefore, association meeting participants should refrain from discussing any activity that could potentially be construed as having an anti-competitive effect. Discussions relating to product or service pricing, market allocations, membership restrictions, product standardization or other conditions on trade could arguably be perceived as a restraint on trade and may expose the SOA and its members to antitrust enforcement procedures.

While participating in all SOA in person meetings, webinars, teleconferences or side discussions, you should avoid discussing competitively sensitive information with competitors and follow these guidelines:

- **Do not** discuss prices for services or products or anything else that might affect prices
- **Do not** discuss what you or other entities plan to do in a particular geographic or product markets or with particular customers.
- **Do not** speak on behalf of the SOA or any of its committees unless specifically authorized to do so.
- **Do** leave a meeting where any anticompetitive pricing or market allocation discussion occurs.
- **Do** alert SOA staff and/or legal counsel to any concerning discussions
- **Do** consult with legal counsel before raising any matter or making a statement that may involve competitively sensitive information.

Adherence to these guidelines involves not only avoidance of antitrust violations, but avoidance of behavior which might be so construed. These guidelines only provide an overview of prohibited activities. SOA legal counsel reviews meeting agenda and materials as deemed appropriate and any discussion that departs from the formal agenda should be scrutinized carefully. Antitrust compliance is everyone's responsibility; however, please seek legal counsel if you have any questions or concerns.

# Presentation Disclaimer

*Presentations are intended for educational purposes only and do not replace independent professional judgment. Statements of fact and opinions expressed are those of the participants individually and, unless expressly stated to the contrary, are not the opinion or position of the Society of Actuaries, its cosponsors or its committees. The Society of Actuaries does not endorse or approve, and assumes no responsibility for, the content, accuracy or completeness of the information presented. Attendees should note that the sessions are audio-recorded and may be published in various media, including print, audio and video formats without further notice.*

# Agenda

- Objectives
- Introduction to Liability Cashflows
- New Dimension of Liability Cashflows
- Practical Considerations and Applications

# Objectives

- By the end of this session, attendees will be able to:
  - Explain how introducing a new dimension to liability cashflows can enable better modeling of complex plan design features
  - Describe the most effective way to model different parts of a complex plan from a cashflow perspective
  - Apply the introduced techniques to practical examples to improve accuracy and quality of analysis provided to the plan sponsors

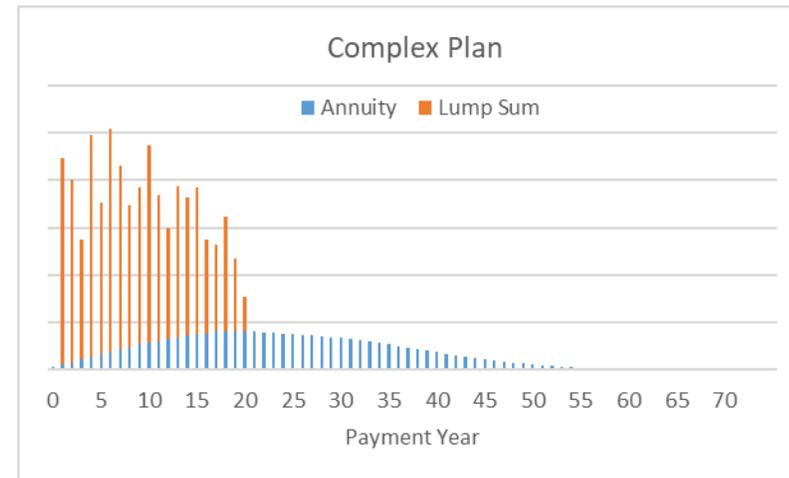
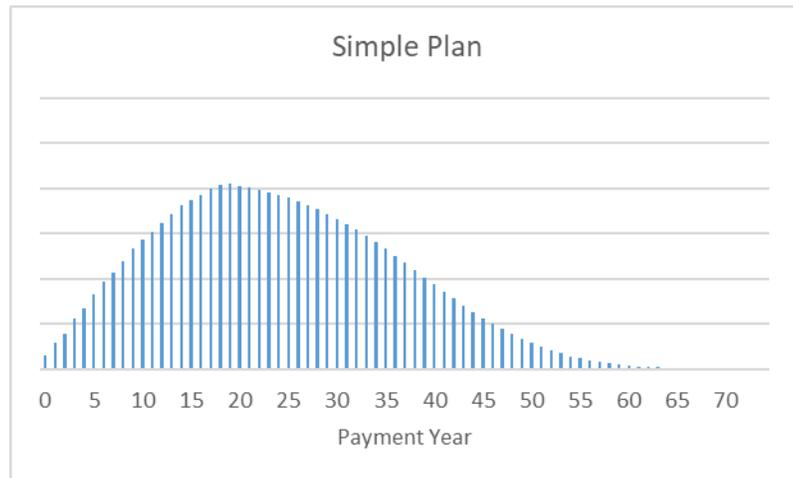
# Introduction to Liability Cashflows

# How are Projected Liability Cashflows Used?

Actuarial valuation software generates projected liability cashflows by payment year

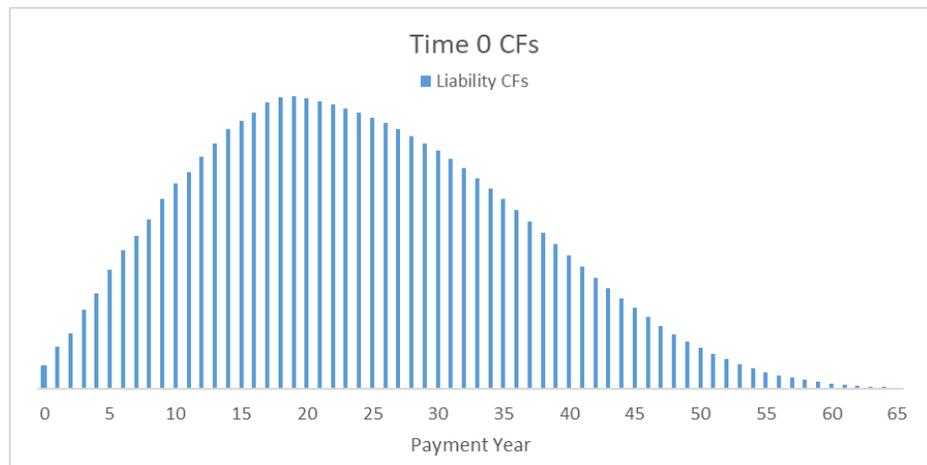
Investment managers use projected cashflows for portfolio decisions (duration, liquidity, etc.)

Portfolio decisions can only be effective if cashflows are a good representation of expected outflows

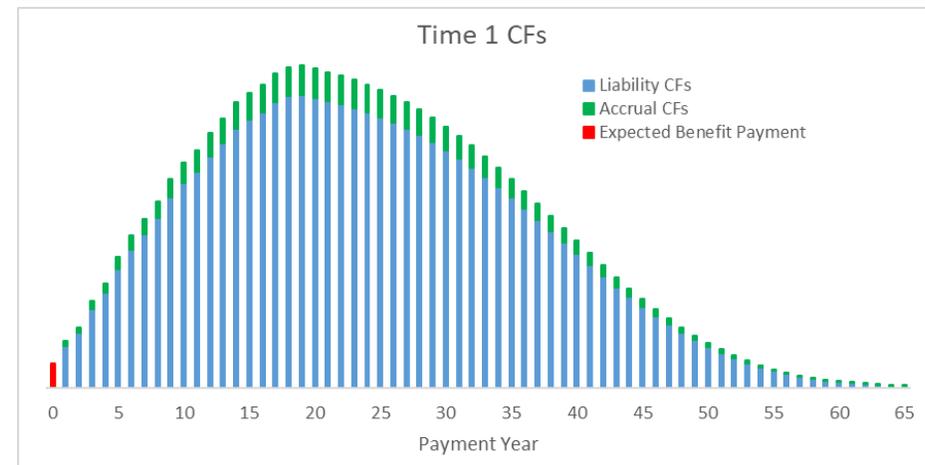


# Traditional vs. Cashflow based Valuation

	Traditional Valuation	Cashflow based Valuation
$AL_0$	PV of accrued benefits	PV of Liability CFs after time 0
$NC_0$	One year's worth of service accruals	PV of accrual CFs
$BP_0$	First year expected liability CF	First year expected liability CF
$AL_1$	$[AL_0 + NC_0] \times (1+i) - BP_{exp,0-1} \times (1+i/2)$	PV of Liability CFs after time 1 incl. adjustment for accruals

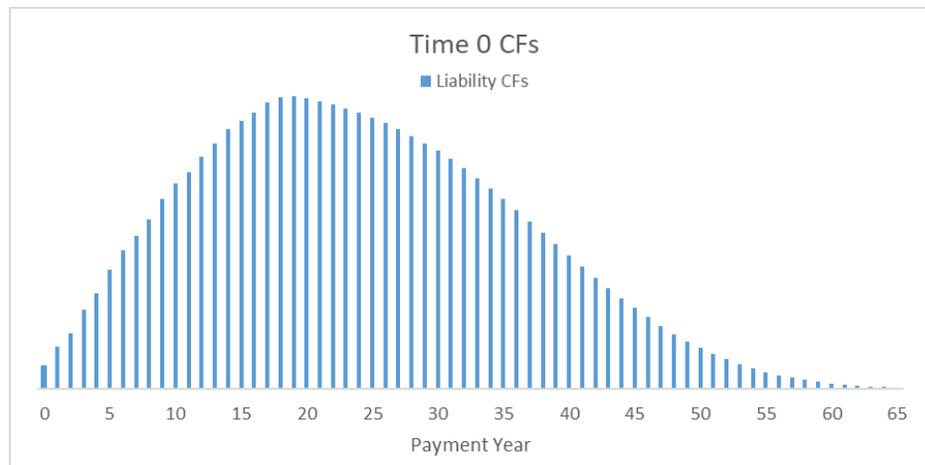


PUC only

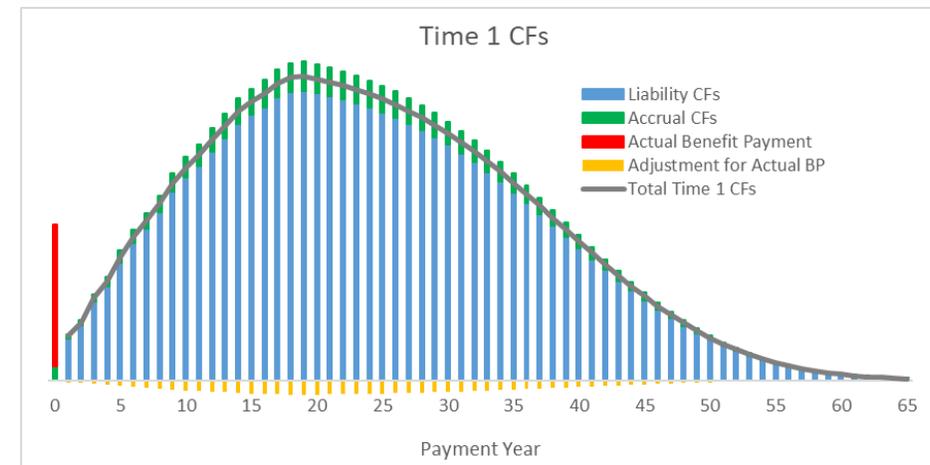


# Traditional vs. Cashflow based Valuation (cont.)

	Traditional Valuation	Cashflow based Valuation
$AL_0$	PV of accrued benefits	PV of Liability CFs after time 0
$NC_0$	One year's worth of service accruals	PV of accrual CFs
$BP_0$	First year <b>actual</b> liability CF	First year <b>actual</b> liability CF
$AL_1$	$[ AL_0 + NC_0 ] \times (1+i) - BP_{act,0-1} \times (1+i/2)$	PV of Liability CFs after time 1 incl. <b>adjustment for</b> accruals and <b>actual BPs</b>



PUC only



# New Dimension of Liability Cashflows

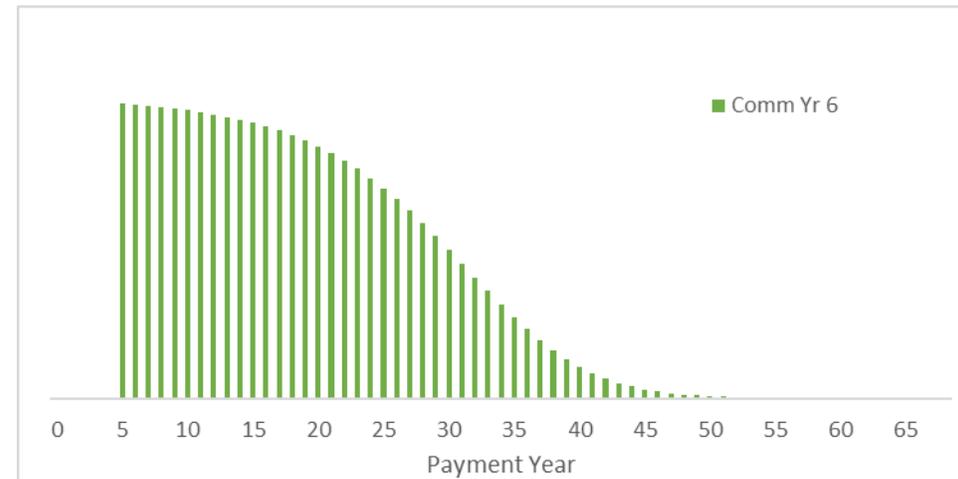
# New Dimension

- By applying actuarial techniques, cashflows by payment year can be:
  - “Rolled forward” with actual benefit payments and service costs
    - sufficient for simple plans
  - Transformed to two dimensions – payment year and commencement year – to capture pre- and post- indexation, and pre- and post- discount rates
    - important for complex plans
- 2D Transformation especially useful for modelling:
  - Cash balance and pension equity plans with interest crediting rates
  - Lump sum paying plans
  - Plans paying COLAs

# Cashflow Example 1

Example 1	
Member status	Active
Age	55
Plan type	Final average
Retirement decrement	100% at age 60
Other decrements	None
Pre-retirement interest crediting	None
Post-retirement indexing	None
Lump sum election	0%

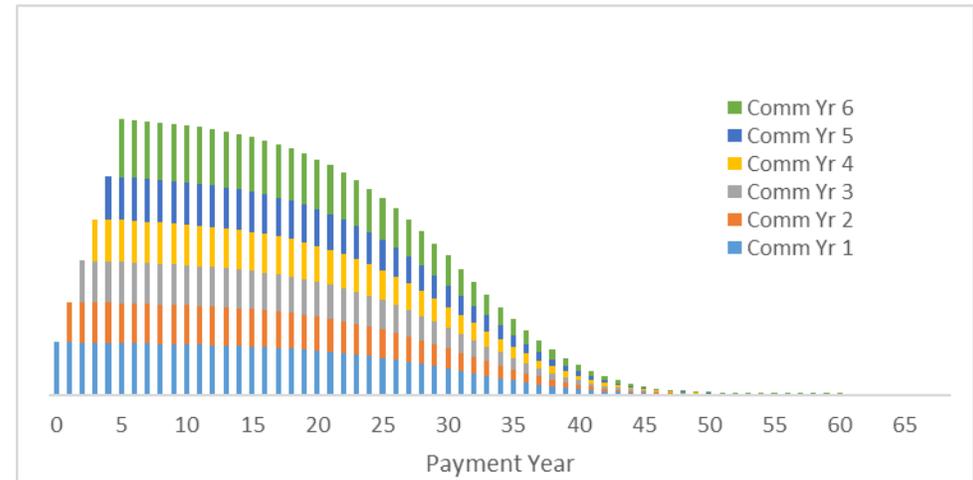
Cashflows		Commencement Year					
Payment Year		Comm Yr 1	Comm Yr 2	Comm Yr 3	Comm Yr 4	Comm Yr 5	Comm Yr 6
1							
2							
3							
4							
5							
6	33,560						33,560
7	33,429						33,429
8	33,284						33,284
9	33,124						33,124
10	32,945						32,945
11	32,745						32,745
12	32,521						32,521
13	32,269						32,269
14	31,983						31,983
15	31,661						31,661



# Cashflow Example 2

Example 2	
Member status	Active
Age	55
Plan type	Final average
Retirement decrement	20% at age 55, 15% at ages 56-59, 100% at 60
Other decrements	None
Pre-retirement interest crediting	None
Post-retirement indexing	None
Lump sum election	0%

Payment Year	Cashflows	Commencement Year					
		Comm Yr 1	Comm Yr 2	Comm Yr 3	Comm Yr 4	Comm Yr 5	Comm Yr 6
1	6,000	6,000					
2	10,616	5,985	4,631				
3	15,330	5,968	4,618	4,744			
4	20,123	5,950	4,604	4,729	4,838		
5	24,993	5,931	4,589	4,714	4,823	4,935	
6	31,616	5,910	4,573	4,697	4,806	4,918	6,712
7	31,492	5,887	4,555	4,679	4,787	4,898	6,686
8	31,356	5,861	4,536	4,659	4,766	4,877	6,657
9	31,205	5,833	4,514	4,636	4,743	4,854	6,625
10	31,037	5,802	4,489	4,611	4,718	4,828	6,589
11	30,848	5,766	4,462	4,583	4,689	4,798	6,549
12	30,637	5,727	4,432	4,552	4,657	4,766	6,504
13	30,399	5,683	4,397	4,517	4,621	4,729	6,454
14	30,131	5,632	4,358	4,477	4,580	4,687	6,397
15	29,827	5,575	4,314	4,432	4,534	4,639	6,332

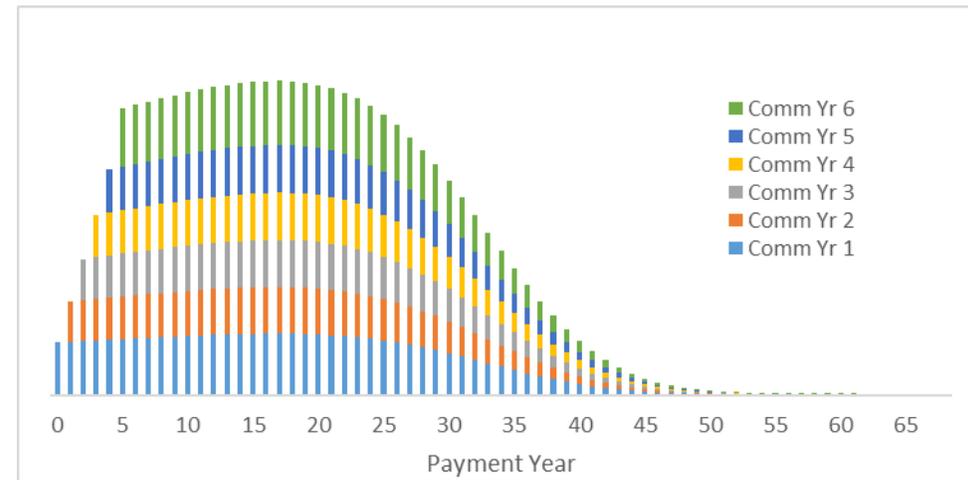


# Cashflow Example 3

Example 3	
Member status	Active
Age	55
Plan type	Final average
Retirement decrement	20% at age 55, 15% at ages 56-59, 100% at 60
Other decrements	None
Pre-retirement interest crediting	None
Post-retirement indexing	80% of CPI*
Lump sum election	0%

\*CPI = 2%

Payment Year	Cashflows	Commencement Year					
		Comm Yr 1	Comm Yr 2	Comm Yr 3	Comm Yr 4	Comm Yr 5	Comm Yr 6
1	6,000	6,000					
2	10,711	6,080	4,631				
3	15,596	6,161	4,692	4,744			
4	20,637	6,240	4,753	4,805	4,838		
5	25,834	6,320	4,813	4,866	4,900	4,935	
6	32,866	6,398	4,873	4,926	4,961	4,996	6,712
7	33,262	6,475	4,932	4,986	5,020	5,057	6,793
8	33,648	6,550	4,989	5,044	5,079	5,115	6,871
9	34,021	6,623	5,044	5,100	5,135	5,172	6,948
10	34,379	6,693	5,097	5,153	5,189	5,226	7,021
11	34,718	6,758	5,147	5,204	5,240	5,278	7,090
12	35,032	6,820	5,194	5,251	5,287	5,326	7,154
13	35,316	6,875	5,236	5,294	5,330	5,369	7,212
14	35,564	6,923	5,273	5,331	5,368	5,406	7,263
15	35,769	6,963	5,303	5,361	5,399	5,438	7,305



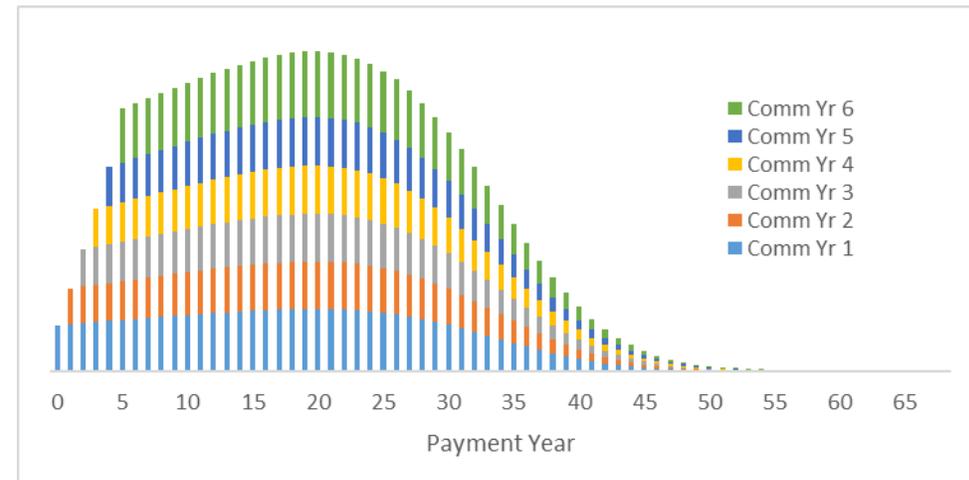
# Cashflow Example 3 – Shock Indexing

## Example 3

Member status	Active
Age	55
Plan type	Final average
Retirement decrement	20% at age 55, 15% at ages 56-59, 100% at 60
Other decrements	None
Pre-retirement interest crediting	None
Post-retirement indexing	80% of CPI*
Lump sum election	0%

\*CPI = 3%

Payment Year	Cashflows	Commencement Year					
		Comm Yr 1	Comm Yr 2	Comm Yr 3	Comm Yr 4	Comm Yr 5	Comm Yr 6
1	6,000	6,000					
2	10,759	6,128	4,631				
3	15,731	6,258	4,729	4,744			
4	20,899	6,389	4,828	4,843	4,838		
5	26,266	6,521	4,928	4,943	4,939	4,935	
6	33,513	6,654	5,028	5,044	5,039	5,036	6,712
7	34,183	6,787	5,129	5,145	5,140	5,136	6,846
8	34,852	6,920	5,229	5,245	5,240	5,237	6,980
9	35,516	7,052	5,329	5,345	5,340	5,337	7,113
10	36,173	7,182	5,427	5,444	5,439	5,435	7,245
11	36,816	7,310	5,524	5,541	5,536	5,532	7,374
12	37,442	7,434	5,618	5,635	5,630	5,626	7,499
13	38,043	7,553	5,708	5,726	5,720	5,716	7,619
14	38,611	7,666	5,793	5,811	5,806	5,802	7,733
15	39,139	7,771	5,872	5,891	5,885	5,881	7,839



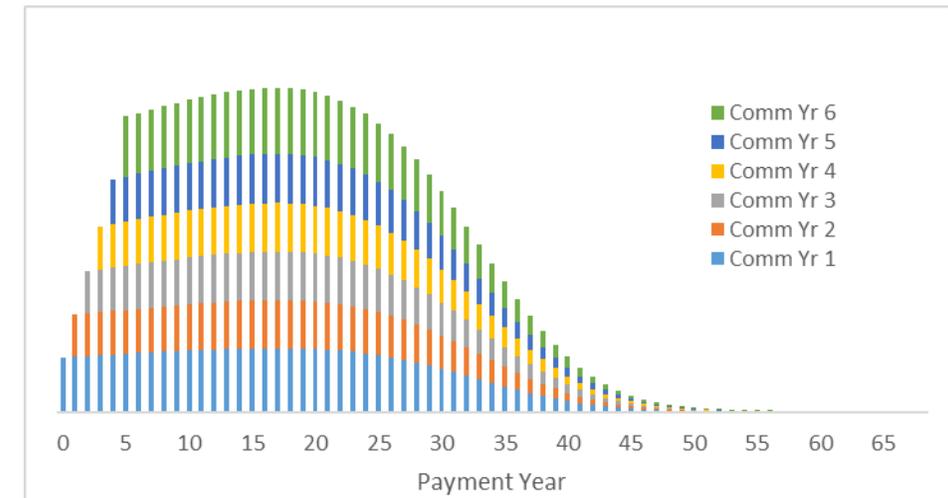
# Cashflow Example 4

Example 4	
Member status	Active
Age	55
Plan type	Cash balance (paid as annuity)
Retirement decrement	20% at age 55, 15% at ages 56-59, 100% at 60
Other decrements	None
Pre-retirement interest crediting	30-year treasury yield*
Post-retirement indexing	80% of CPI**
Lump sum election	0%

\*Interest Crediting Rate (ICR) = 2%

\*\*CPI = 2%

Cashflows		Commencement Year					
Payment Year		Comm Yr 1	Comm Yr 2	Comm Yr 3	Comm Yr 4	Comm Yr 5	Comm Yr 6
1	6,000	6,000					
2	10,659	6,080	4,578				
3	15,468	6,161	4,639	4,669			
4	20,430	6,240	4,699	4,729	4,761		
5	25,544	6,320	4,758	4,789	4,822	4,855	
6	32,462	6,398	4,817	4,849	4,881	4,915	6,601
7	32,852	6,475	4,875	4,907	4,940	4,974	6,680
8	33,234	6,550	4,932	4,964	4,997	5,032	6,758
9	33,603	6,623	4,987	5,019	5,053	5,088	6,833
10	33,956	6,693	5,039	5,072	5,106	5,142	6,905
11	34,290	6,758	5,089	5,122	5,156	5,192	6,973
12	34,601	6,820	5,135	5,168	5,203	5,239	7,036
13	34,881	6,875	5,176	5,210	5,245	5,282	7,093
14	35,126	6,923	5,213	5,247	5,282	5,319	7,143
15	35,328	6,963	5,243	5,277	5,312	5,349	7,184



# Cashflow Example 4 – Shock Interest Credit

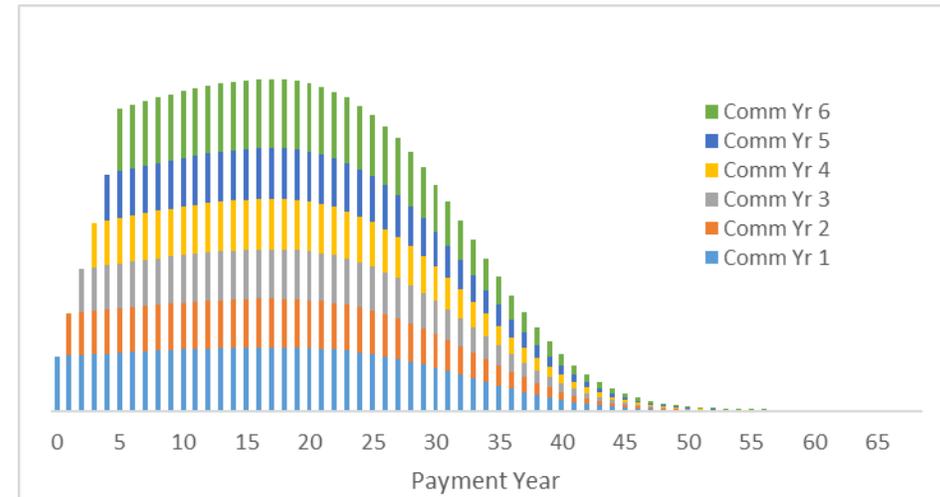
## Example 4

Member status	Active
Age	55
Plan type	Cash balance (paid as annuity)
Retirement decrement	20% at age 55, 15% at ages 56-59, 100% at 60
Other decrements	None
Pre-retirement interest crediting	30-year treasury yield*
Post-retirement indexing	80% of CPI**
Lump sum election	0%

\*Interest Crediting Rate (ICR) = 3%

\*\*CPI = 2%

Cashflows		Commencement Year					
Payment Year		Comm Yr 1	Comm Yr 2	Comm Yr 3	Comm Yr 4	Comm Yr 5	Comm Yr 6
1	6,000	6,000					
2	10,703	6,080	4,623				
3	15,606	6,161	4,684	4,761			
4	20,711	6,240	4,745	4,823	4,903		
5	26,022	6,320	4,805	4,884	4,965	5,048	
6	33,275	6,398	4,865	4,944	5,026	5,111	6,931
7	33,675	6,475	4,923	5,004	5,087	5,172	7,014
8	34,066	6,550	4,980	5,062	5,146	5,232	7,096
9	34,444	6,623	5,036	5,118	5,203	5,290	7,174
10	34,807	6,693	5,089	5,172	5,258	5,346	7,250
11	35,150	6,758	5,139	5,223	5,309	5,399	7,321
12	35,468	6,820	5,185	5,270	5,358	5,448	7,388
13	35,755	6,875	5,227	5,313	5,401	5,492	7,447
14	36,006	6,923	5,264	5,350	5,439	5,530	7,500
15	36,213	6,963	5,294	5,381	5,470	5,562	7,543

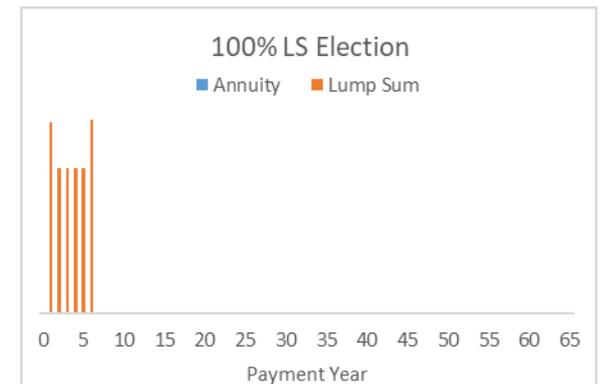
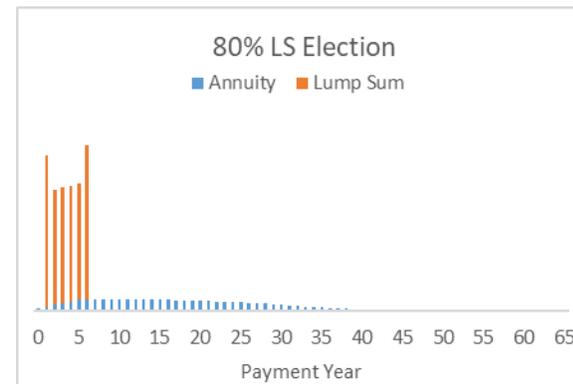
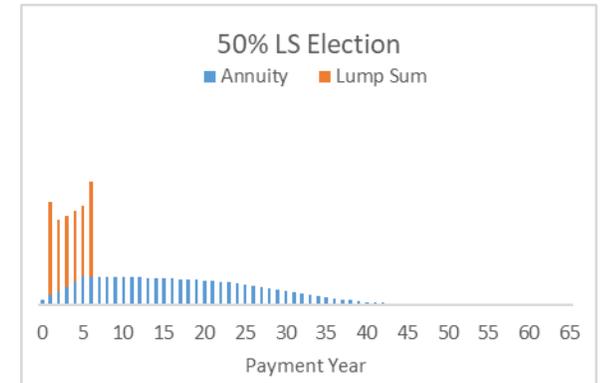
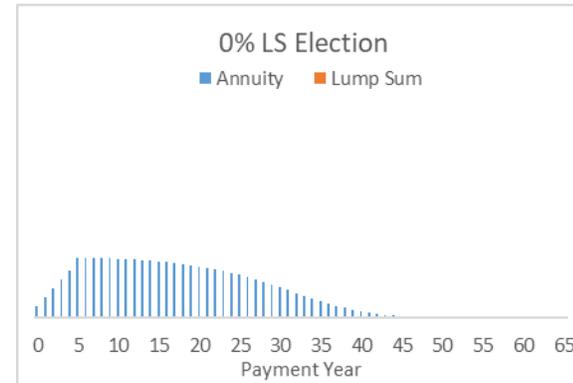


# Cashflow Example 2 – With Lump Sum Election Option

## Example 2

Member status	Active
Age	55
Plan type	Final average
Retirement decrement	20% at age 55, 15% at ages 56-59, 100% at 60
Other decrements	None
Post retirement indexing	None
Lump sum election	<b>0%/50%/80%/100%</b>

Lump sum discount rate can be a flat rate or yield curve based



# Practical Considerations and Applications

# Practical Considerations

Common Issues	Solution
Cashflows outdated	Rollforward cashflows with actual benefit payments and service costs Chopping off first year cashflow is dangerous!
Service cost cashflows not available	Prorate active past service cashflows using (SC/Active Liability) ratio
2D cashflows not available	Apply 1D to 2D annuity cashflow transformation
Complex plan (COLA, crediting rates)	Adjust 2D cashflows to reflect desired indexation and crediting rates
Interest rate sensitive lump sums	Use 1D annuity substitution cashflows to capture correct duration But use “collapsed” 2D cashflows for ALM projections
Plan has multiple benefit structures	Request more granular CFs – split by participant type, plan design type and form of payment; request sensitivity cashflows, if applicable

# 1D to 2D Annuity Cashflow Transformation

		Commencement year			
		1	2	3	...
Payment year	1	$CF_1$			
	2	$CF_2$			
	3	$CF_3$			
	4	$CF_4$			
	...	...			

→

		1	2	3	...
Payment year	1	$CF_{1,1}$	0	0	...
	2	$CF_{1,1} \times I_1 \times p_1$	$CF_{2,2} = CF_2 - CF_{1,2}$	0	...
	3	$CF_{1,2} \times I_2 \times p_2$	$CF_{2,2} \times I_2 \times p_2$	$CF_{3,3} = CF_3 - CF_{1,3} - CF_{2,3}$	...
	4	$CF_{1,3} \times I_3 \times p_3$	$CF_{2,3} \times I_3 \times p_3$	$CF_{3,3} \times I_3 \times p_3$	...
	...	...	...	...	...

$CF_y$  = Expected cashflow paid in year  $y$

$CF_{x,y}$  = Expected cashflow commencing in year  $x$  and paid in year  $y$

$p_x$  = assumed one year survival probability of cashflows paid in year  $x$

$I_y$  = inflationary increase factor in year  $y$

Helps capture LS paying plans, CB plans paying annuities (with fixed conversion rates) and plans paying COLAs

# Collapsing 2D Annuity Cashflows to Lump Sums

		Commencement year				Commencement year					
		1	2	3	...		1	2	3	...	
Payment year	1	$CF_{1,1}$	0	0	0	Payment year	1	$(1 - LS) \times CF_{1,1}$ $+ LS \times LSCF_{1,1}$	0	0	...
	2	$CF_{1,2}$	$CF_{2,2}$	0	0		2	$(1 - LS) \times CF_{1,2}$	$(1 - LS) \times CF_{2,2}$ $+ LS \times LSCF_{2,2}$	0	...
	3	$CF_{1,3}$	$CF_{2,3}$	$CF_{3,3}$	0		3	$(1 - LS) \times CF_{1,3}$	$(1 - LS) \times CF_{2,3}$	$(1 - LS) \times CF_{3,3}$ $+ LS \times LSCF_{3,3}$	...
	4	$CF_{1,4}$	$CF_{2,4}$	$CF_{3,4}$	$CF_{4,4}$		4	$(1 - LS) \times CF_{1,4}$	$(1 - LS) \times CF_{2,4}$	$(1 - LS) \times CF_{3,4}$	...
	...	...	...	...	...		...	...	...	...	...

$CF_{x,y}$  = Expected cashflow commencing in year x and paid in year y

$LS$  = assumed percentage of benefits taken as a lump sum

$LSCF_{i,j}$  = Lump sum cashflow, where  $LSCF_{i,i} = \sum_j CF_{i,j} DF_{i,j}$

$DF_{i,j}$  = Discount factor for cashflow paid in year j back to year i

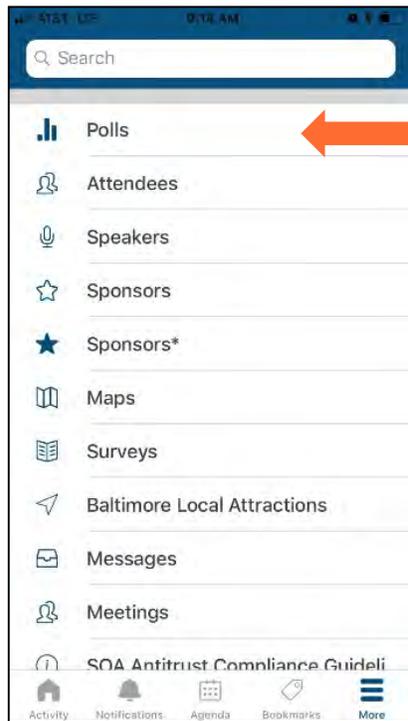
Helps capture interest sensitive lump sum payments.

# Practical Application: Case study

- MK Industries Super Complex Pension Plan
  - Cash balance component (A+B approach)
  - Traditional final salary benefits (some payable as lump sums)
  - Post-retirement COLAs
- 1D cashflows provided for modelling
  - Split by participant type
  - Split by plan design feature (i.e. COLA/non-COLA, CB/Traditional benefit)
  - Split by form of payment (Annuity/LS), where applicable
  - Annuity substitution cashflows provided for traditional lump sum eligible benefits
- Cash balance benefits converted to annuities using fixed conversion rate
- 100% of actives assumed to take traditional benefit as a lump sum

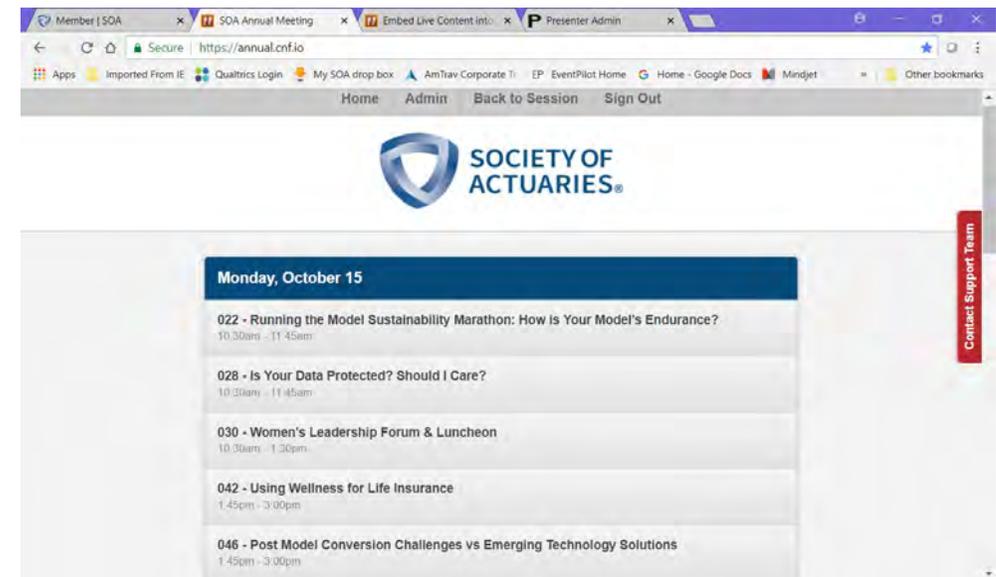
# To Participate, look for Polls in the SOA Event App or visit [annual.cnf.io](https://annual.cnf.io) in your browser

Find The Polls Feature Under **More**  
In The Event App or Under This  
Session in the Agenda



or

Type [annual.cnf.io](https://annual.cnf.io) In Your Browser



## *Live Content Slide*

*When playing as a slideshow, this slide will display live content*

**Poll: We are looking to generate ALM projections as of 12/31/2019, but the 1D cashflow profile provided is as of 12/31/2018. Which of the following adjustments are appropriate?**

## *Live Content Slide*

*When playing as a slideshow, this slide will display live content*

**Poll: We are looking to project cashflows under various CPI scenarios to recommend an appropriate inflation hedge. The cashflows provided have 2% post-retirement CPI embedded in them. What's the best way to adjust active cashflows for this purpose?**

## *Live Content Slide*

*When playing as a slideshow, this slide will display live content*

**Poll: We are looking to project cashflows for the cash balance component of the plan under various ICR assumptions. The annuity cashflows provided have 2% pre-retirement ICR embedded in them. What's the best way to adjust the cashflows for this purpose?**

## *Live Content Slide*

*When playing as a slideshow, this slide will display live content*

**Poll: We are looking to perform ALM projections for the lump sum component of the plan. Both annuity substitution and lump sum cashflows were provided for traditional lump sum eligible benefits. What's the best way to adjust the CFs for this purpose?**

# Modelling extensions

- “Greater of” plan provisions
  - Participant receives max (PV of frozen annuity, Cash balance account)
  - Derive “Real/Nominal” cashflow split to capture ICR exposure
  - Granular cashflow splits can minimize the modelling simplification impact
- Mortality assumptions
  - Analyze impact of changes to base/improvement tables
  - Utilizes 2D cashflow grids – no individual participant data needed
  - “Ratio of Lx” approach

