SOCIETY OF ACTUARIES

EXAM FM   FINANCIAL MATHEMATICS

EXAM FM SAMPLE SOLUTIONS

Financial Economics

June 2014 changes

Questions 1-30 are from the prior version of this document. They have been edited to conform more closely to current question writing style, but are unchanged in content.

Question 31 is the former Question 58 from the interest theory question set.

Questions 32-34 are new.

January 2015 changes

Questions 35-46 are new.

May 2015 changes

Question 32 was modified (and modified again in June)

Questions 47-62 are new.

February 2016 changes: Questions 63-64 are new.

Some of the questions in this study note are taken from past examinations.

These questions are representative of the types of questions that might be asked of candidates sitting for the Financial Mathematics (FM) Exam. These questions are intended to represent the depth of understanding required of candidates. The distribution of questions by topic is not intended to represent the distribution of questions on future exams.

FM-09-16

1.   Solution: D

If the call is at-the-money, the put option with the same cost will have a higher strike price. A purchased collar requires that the put have a lower strike price.

2.   Solution: C

$66.59 - 18.64 = 500 - K\exp(-0.06)$ and so $K = (500 - 66.59 + 18.64)/\exp(-0.06) = 480$.

3.   Solution: D

The accumulated cost of the hedge is $(84.30 - 74.80)\exp(0.06) = 10.09$.

Let x be the market price in one year.

If $x < 0.12$ the put is in the money and the payoff is $10,000(0.12 - x) = 1,200 - 10,000x$. The sale of the jalapenos has a payoff of $10,000x - 1,000$ for a profit of $1,200 - 10,000x + 10,000x - 1,000 - 10.09 = 190$.

From 0.12 to 0.14 neither option has a payoff and the profit is $10,000x - 1,000 - 10.09 = 10,000x - 1,010$. The range is 190 to 390.

If $x > 0.14$ the call is in the money and the payoff is $-10,000(x - 0.14) = 1,400 - 10,000x$. The profit is $1,400 - 10,000x + 10,000x - 1,000 - 10.09 = 390$.

The range is 190 to 390.

4.   Solution: B

The present value of the forward prices is
$1000[10(3.89)/1.06 + 15(4.11)/1.065^2 + 20(4.16)/1.07^3] = 158,968$. Any sequence of payments with that present value is acceptable. All but B have that value.

5.   Solution: E

Consider buying the put and selling the call. Let x be the index price in one year. If $x > 1025$, the payoff is $1025 - x$. After buying the index for x you have $1,025 - 2x$ which is not the goal. It is not necessary to check buying the call and selling the put as that is the only other option. But as a check, if $x > 1025$, the payoff is $x - 1025$ and after buying the stock you have spent 1025. If $x < 1025$, the payoff is again $x - 1025$.

One way to get the cost is to note that the forward price is $1,000(1.05) = 1,050$. You want to pay 25 less and so must spend $25/1.05 = 23.81$ today.

6.   Solution: E

In general, an investor should be compensated for time and risk. A forward contract has no investment, so the extra 5 represents the risk premium. Those who buy the stock expect to earn both the risk premium and the time value of their purchase and thus the expected stock value is greater than $100 + 5 = 105$.

7.   Solution: C

All four of answers A-D are methods of acquiring the stock. Only the prepaid forward has the payment at time 0 and the delivery at time T.

8.   Solution: B

Only straddles use at-the-money options and buying is correct for this speculation.

9.   Solution: D

To see that D does not produce the desired outcome, begin with the case where the stock price is S and is below 90. The payoff is $S + 0 + (110 - S) - 2(100 - S) = 2S - 90$ which is not constant and so cannot produce the given diagram. On the other hand, for example, answer E has a payoff of $S + (90 - S) + 0 - 2(0) = 90$. The cost is $100 + 0.24 + 2.17 - 2(6.80) = 88.81$. With interest it is 93.36. The profit is $90 - 93.36 = -3.36$ which matches the diagram.

10.   Solution: D

Answer A is true because forward contracts have no initial premium.

Answer B is true because both payoffs and profits of long forwards are opposite to short forwards.

Answer C is true because to invest in the stock, one must borrow 100 at $t = 0$, and then pay back $110 = 100(1 + 0.1)$ at $t = 1$, which is like buying a forward at $t = 1$ for 110.

Answer D is false because repeating the calculation shown for Answer C, but with 10% as a continuously compounded rate, the stock investor must now pay back $100\exp(0.1) = 110.52$ at $t = 1$; this is more expensive than buying a forward at $t = 1$ for 110.00.

Answer E is true because the calculation would be the same as shown above for Answer C but now the stock investor gets an additional dividend of 3.00 at $t = 0.5$, which the forward investor does not receive (due to not owning the stock until $t = 1$.

11.   Solution: C

The future value of the cost of the options is 9.12(1.08) = 9.85, 6.22(1.08) = 6.72, and 4.08(1.08) = 4.41 respectively.

If $S < 35$ no call is in the money and the profits are –9.85, –6.72, and –4.41. The condition is not met.

If $35 < S < 40$ the 35-strike call returns $S – 35$ and the profit is $S – 44.85$. For the 45-strike call to have a lower profit than the 35-strike call, we need $–4.41 < S – 44.85$ or $S > 40.44$. This is inconsistent with the assumption.

If $40 < S < 45$ the same condition applies for comparing the 35- and 45-strike calls and so $S > 40.44$ is needed. The 40-strike call has a profit of $S – 40 – 6.72 = S – 46.72$. For the 45-strike to exceed the 40-strike, we need $–4.41 > S – 46.72$ or $S < 42.31$.

There is no need to consider $S > 45$.

12.   Solution: B

Let S be the price of the index in six months.

The put premium has future value (at t = 0.5) of 74.20[1 + (0.04/2)] = 75.68.

The 6-month profit on a long put position is max(1,000 – S, 0) – 75.68.

The 6-month profit on a short put position is 75.68 – max(1,000 – S, 0).

$0 = 75.68 – \max(1{,}000 – S, 0)$.

$75.68 = \max(1{,}000 – S, 0)$.

$75.68 = 1{,}000 – S. \ S = 924.32$.

13.   Solution: D

Buying a call in conjunction with a short position is a form of insurance called a cap. Answers (A) and (B) are incorrect because a floor is the purchase of a put to insure against a long position. Answer (E) is incorrect because writing a covered call is the sale of a call along with a long position in the stock, so that the investor is selling rather than buying insurance.

The profit is the payoff at time 2 less the future value of the initial cost. The stock payoff is –75 and the option payoff is 75 – 60 = 15 for a total of –60. The future value of the initial cost is (–50 + 10)(1.03)(1.03) = –42.44. the profit is –60 – (–42.44) = –17.56.

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14.   Solution: A

Let C be the price for the 40-strike call option. Then, C + 3.35 is the price for the 35-strike call option. Similarly, let P be the price for the 40-strike put option. Then, P – x is the price for the 35-strike put option, where x is the desired quantity. Using put-call parity, the equations for the 35-strike and 40-strike options are, respectively,

$$(C+3.35)+35e^{-0.02}-40=P-x$$
$$C+40e^{-0.02}-40=P.$$

Subtracting the first equation from the second, $5e^{-0.02}-3.35=x, \quad x=1.55.$

15.   Solution: C

The initial cost to establish this position is 5(2.78) – 3(6.13) = –4.49. Thus, you are receiving 4.49 up front. This grows to 4.49exp[0.25(0.08)] = 4.58 after 3 months. Then, if S is the value of the stock at time 0.25, the profit is

5max(S –40,0) – 3max(S – 35,0) + 4.58. The following cases are relevant:

$S<35$: Profit = 0 – 0 + 4.58 = 4.58.

$35<S<40$: Profit = 0 – 3(S – 35) + 4.58 = –3S + 109.58. Minimum of –10.42 is at $S=40$ and maximum of 4.58 is at $S=35$.

$S>40$: Profit is 5(S – 40) – 3(S – 35) + 4.58 = 2S – 90.42. Minimum of –-10.42 is at $S=40$ and maximum if infinity.

Thus the minimum profit is –10.42 for a maximum loss of 10.42 and the maximum profit is infinity.

16.   Solution: D

The straddle consists of buying a 40-strike call and buying a 40-strike put. This costs 2.78 + 1.99 = 4.77 and grows to 4.77exp(0.02) = 4.87 at three months. The strangle consists of buying a 35-strike put and a 45-strike call. This costs 0.44 + 0.97 = 1.41 and grows to 1.41exp(0.02) = 1.44 at three months. Let S be the stock price in three months.

For $S < 40$, the straddle has a profit of $40 - S - 4.87 = 35.13 - S$.

For $S > 40$, the straddle has a profit of $S - 40 - 4.87 = S - 44.87$

For $S < 35$, the strangle has a profit of $35 - S - 1.44 = 33.56 - S$.

For $35 < S < 45$, the strangle has a profit of -1.44.

For $S > 45$, the strangle has a profit of $S - 45 - 1.44 = S - 46.44$.

For $S < 35$ the strangle underperforms the straddle.

For $35 < S < 40$, the strangle outperforms the straddle if $-1.44 > 35.13 - S$ or $S > 36.57$. At this point only Answer D can be correct.

As a check, for $40 < S < 45$, the strangle outperforms the straddle if $-1.44 > S - 44.87$ or $S < 43.43$.

For $S > 45$, the strangle outperforms the straddle if $S - 46.44 > S - 44.87$, which is not possible.

17.   Solution: B

 Strategy I –Yes. It is a bear spread using calls, and bear spreads perform better when the prices of the underlying asset goes down.

 Strategy II – Yes. It is also a bear spread – it just uses puts instead of calls.

 Strategy III – No. It is a box spread, which has no price risk; thus, the payoff is the same (1,000 – 950 = 50), no matter the price of the underlying asset.

18.   Solution: B

First calculate the expected one-year profit without using the forward. This is 0.2(700 + 150 – 750) + 0.5(700 + 170 – 850) + 0.3(700 + 190 – 950) = 20 + 10 – 18 = 12. Next, calculate the expected one-year profit when buying the 1-year forward for 850. This is 1(700 + 170 – 850) = 20. Thus, the expected profit increases by 20 – 12 = 8 as a result of using the forward.

19.   Solution: D

There are 3 cases, one for each row in the probability table.

For all 3 cases, the future value of the put premium is $100\exp(0.06) = 106.18$.

In Case 1, the 1-year profit is $750 - 800 - 106.18 + \max(900 - 750, 0) = -6.18$.

In Case 2, the 1-year profit is $850 - 800 - 106.18 + \max(900 - 850, 0) = -6.18$.

In Case 3, the 1-year profit is $950 - 800 - 106.18 + \max(900 - 950, 0) = 43.82$.

Thus, the expected 1-year profit $= 0.7(-6.18) + 0.3(43.82) = -4.326 + 13.146 = 8.82$.

20.   Solution: B

We need the future value of the current stock price minus the future value of each of the 12 dividends, where the valuation date is time 3. Thus, the forward price is

$$200e^{0.04(3)} - 1.50[e^{0.04(2.75)} + e^{0.04(2.5)}1.01 + \cdots + e^{0.04(0.25)}1.01^{10} + 1.01^{11}]$$
$$= 200e^{0.12} - 1.50e^{0.11}[1 + (e^{-0.01}1.01) + \cdots + (e^{-0.01}1.01)^{10} + (e^{-0.01}1.01)^{11}]$$
$$= 200e^{0.12} - 1.50e^{0.11}\frac{1 - (e^{-0.01}1.01)^{12}}{1 - e^{-0.01}1.01} = 225.50 - 1.67442(11.99672) = 205.41.$$

21.   Solution: E

The fair value of the forward contract is given by $S_0e^{(r-d)T} = 110e^{(0.05-0.02)0.5} = 111.66$.

This is 0.34 less than the observed price. Thus, one could exploit this arbitrage opportunity by selling the observed forward at 112 and buying a synthetic forward at 111.66, making $112 - 111.66 = 0.34$ profit.

22.   Solution: B

First, determine the present value of the forward contracts. On a per ton basis, it is
$1,600/1.05 + 1,700/1.055^2 + 1,800/1.06^3 = 4,562.49$.

Then, solve for the level swap price, x, as follows:

$4,562.49 = x/1.05 + x/1.055^2 + x/1.06^3 = 2.69045x.$

Thus, $x = 4,562.49 / 2.69045 = 1,695.81$.

Thus, the amount he would receive each year is $50(1,695.81) = 84,790.38$.

23.   Solution: E

The notional amount and the future 1-year LIBOR rates (not given) do not factor into the calculation of the swap's fixed rate.

Required quantities are

(1) Zero-coupon bond prices:
$1.04^{-1} = 0.96154, 1.045^{-2} = 0.91573, 1.0525^{-3} = 0.85770, 1.0625^{-4} = 0.78466, 1.075^{-5} = 0.69656.$
(2) 1-year implied forward rates:

$0.04, 1.045^2 / 1.04 - 1 = 0.05002, 1.0525^3 / 1.045^2 = 0.06766,$

$1.0625^4 / 1.0525^3 - 1 = 0.09307, 1.075^5 / 1.0625^4 - 1 = 0.12649.$

The fixed swap rate is:

$$\frac{\begin{aligned}&0.96154(0.04) + 0.9173(0.05002) + 0.85770(0.06766)\\&\quad + 0.78466(0.09307) + 0.69656(0.12649)\end{aligned}}{0.96154 + 0.91573 + 0.85770 + 0.78466 + 0.69656} = 0.07197.$$

The calculation can be done without the implied forward rates as the numerator is 1 – 0.69656 = 0.30344.

24.   Solution: D

(A) is a reason because hedging reduces the risk of loss, which is a primary function of derivatives.

(B) is a reason because derivatives can be used the hedge some risks that could result in bankruptcy.

(C) is a reason because derivatives can provide a lower-cost way to effect a financial transaction.

(D) is not a reason because derivatives are often used to avoid these types of restrictions.

(E) is a reason because an insurance contract can be thought of as a hedge against the risk of loss.

25.   Solution: C

(A) is accurate because both types of individuals are involved in the risk-sharing process.

(B) is accurate because this is the primary reason reinsurance companies exist.

(C) is not accurate because reinsurance companies share risk by issuing rather than investing in catastrophe bonds. They are ceding this excess risk to the bondholder.

(D) is accurate because it is diversifiable risk that is reduced or eliminated when risks are shared.

(E) is accurate because this is a fundamental idea underlying risk management and derivatives.

26.   Solution: B

I is true. The forward seller has unlimited exposure if the underlying asset's price increases.

II is true. The call issuer has unlimited exposure if the underlying asset's price rises.

III is false. The maximum loss on selling a put is FV(put premium) – strike price.

27.   Solution: A

I is true. As the value of the house decreases due to insured damage, the policyholder will be compensated for the loss. Homeowners insurance is a put option.

II is false. Returns from equity-linked CDs are zero if prices decline, but positive if prices rise. Thus, owners of these CDs benefit from rising prices.

III is false. A synthetic forward consists of a long call and a short put, both of which benefit from rising prices (so the net position also benefits as such).

28.   Solution: E

(A) is true. Derivatives are used to shift income, thereby potentially lowering taxes.

(B) is true. As with taxes, the transfer of income lowers the probability of bankruptcy.

(C) is true. Hedging can safeguard reserves, and reduce the need for external financing, which has both explicit (e.g., fees) and implicit (e.g., reputational) costs.

(D) is true. When operating internationally, hedging can reduce exchange rate risk.

(E) is false. A firm that credibly hedges will reduce the riskiness of its cash flows, and will be able to increase debt capacity, which will lead to tax savings, since interest is deductible.

29.   Solution: A

The current price of the stock and the time of future settlement are not relevant, so let both be 1. Then the following payments are required:

Outright purchase, payment at time 0, amount of payment = 1.

Fully leveraged purchase, payment at time 1, amount of payment = $\exp(r)$.

Prepaid forward contract, payment at time 0, amount of payment = $\exp(-d)$.

Forward contract, payment at time 1, amount of payment = $\exp(r-d)$.

Since $r > d > 0$, $\exp(-d) < 1 < \exp(r-d) < \exp(r)$.

The correct ranking is given by (A).

30.   Solution: C

(A) is a distinction. Daily marking to market is done for futures, not forwards.

(B) is a distinction. Futures are more liquid; in fact, if you use the same broker to buy and sell, your position is effectively cancelled.

(C) is not a distinction. Forwards are more customized, and futures are more standardized.

(D) is a distinction. With daily settlement, credit risk is less with futures (v. forwards).

(E) is a distinction. Futures markets, like stock exchanges,have daily price limits.

31.   Solution: E

The transaction costs are 2 (1 for the forward and 1 for the stock)

The price of the forward is therefore $(50 + 2)(1.06) = 55.12$.

32.   Solution: E

The notional value of this short futures position is $1500(20)(250) = 7.5$ million. The initial margin requirement is 5% of 7.5 million, or 375,000, and the maintenance margin requirement is 90% of 375,000, or 337,500. Judy has a short position, so when the index decreases/increases, her margin account would increase/decrease.

At the first marking-to-market, when the index has fallen to 1498, the margin account is:

$375,000 \times \exp(0.04/365) + (1500 - 1498)(20)(250) = 375,041.10 + 10,000 = 385,041.10$.

For Judy not to get a margin call at the second marking-to-market, the value of the index, X, would have to rise so that the account balance decreases to 337,500:

$385,041.10 \times \exp(0.04/365) + (1498 - X)(20)(250) = 337,500$

$X = 1507.52$.

33:     Solution: E

Option I is American-style, and thus, it can be exercised at any time during the 6-month period. Since it is a put, the payoff is greatest when the stock price is smallest (18). The payoff is $20 - 18 = 2$.

Option II is Bermuda-style, and can be exercised at any time during the 2nd 3-month period. Since it is a call, the payoff is greatest when the stock price S is largest (28). The payoff is $28 - 25 = 3$.

Option III is European-style, and thus, it can be exercised only at maturity. Since it is a 30-strike put, the payoff equation is $30 - 26 = 4$.

The ranking is III > II > I.

34.   Solution: E

Since the 2-year forward price is higher than the 1-year forward price, the buyer, relative to the forward prices, overall pays more at the end of the first year but less at the end of the second year. So this means that the buyer pays the swap counterparty at the end of the first year but receives money back from the swap counterparty at the end of the second year. So the buyer lends to the swap counterparty at the 1-year effective forward interest rate, from the end of the first year to the end of the second year, namely 6%.

35.   Solution: C

If the index declined to $45 and the customer exercised the put (buying 100 shares in the market and selling it to the writer for the $50 strike price), the customer would make $500 ($5000 proceeds of sale – $4500 cost = $500). However, this would be offset by the $500 premium paid for the option. The net result would be that the customer would break even.

36.   Solution: D

Expected value if no derivative purchased:

$(0.50)(500.000)(0.6) - (0.5)(300,000) = 0.$

Expected value if derivative purchased:

$(75,000)(0.6) = 45,000$

Change is $45,000 - 0 = 45,000$

37.   Solution: B

When there are discrete dividends, the pricing formula is $S(1 + i) - AV(\text{dividends})$, where S is the current stock price. Thus,

$$75 = S(1.06) - [1.5(1.06)^{0.5} + 1.5 = S(1.06) - 3.0443$$
$$S = 78.0433/1.06 = 73.626.$$

38.   Solution: C

For stocks without dividends and in the absence of transaction costs, the stock's forward price is the future value of its spot price based on the risk-free interest rate; otherwise there would be an arbitrage opportunity. Because the risk-free interest rate is positive, the forward price must be greater than the spot price of 75.

Because these investors are risk-averse (i.e. they prefer not to take risks if the average rate of return is the same) they need to receive on the average a greater return than the risk-free interest rate on the shares they invest in this stock. In other words, they need to receive a risk premium (incentive) for taking on risk. The forward price only includes the risk-free interest rate and not the risk premium, so the forward price is less than the expected value of the future stock price, namely 90.

39.   Solution: E

By definition, one way to use a 3:1 ratio spread is to buy 1 call and sell 3 calls at a different strike price, with the same 1-year maturity. (This can also be done using all puts.)

40.   Solution: C

If F is the forward price, K is the strike price, C is the call option price, P is the put option price, v is the annual discounting factor at the risk-free rate, and t is the number of years, then we have the put-call parity formula $C - P = v^t (F - K)$.

Using the data for each commodity (with C being the call price zinc and K the common strike price), we have

$$700 - 550 = \frac{1}{(1.06)^2}(1400 - K)$$
$$C - 550 = \frac{1}{(1.06)^2}(1600 - K).$$

Now we could solve for K in the top equation and then use this to solve the second equation for C, but a more efficient method is to subtract the top equation from the bottom equation to cancel out K. Therefore,

$$C - 700 = \frac{200}{1.1236} \Rightarrow C = 878.00.$$

41.   Solution: E

The forwards do not have any premium. Due to put-call parity, the net premium of the remaining strategies will increase with an increasing strike price. With a 1% interest rate, the net premium for E will be positive.

42.   Solution: D

Purchasing the stock results in paying K today and receiving S in t years, so the profit at expiration from this transaction is $S - Ke^{rt}$.

Selling the call results in receiving the premium C today and paying max$(0, S - K)$ in t years. Because $S > K$, the profit from this transaction at expiration is $Ce^{rt} - S + K$.

The overall profit is the sum, $Ce^{rt} + K - Ke^{rt} = Ce^{rt} + K(1 - e^{rt})$.

43.   Solution: C

A written collar consists of a short put option and a long call option. The initial cost of the position is –44 – 2.47 + 3.86 = –42.61.

The payoff and profit table is:

	$S_T \leq 40$	$40 < S_T \leq 50$	$S_T > 50$
Short stock	$-S_T$	$-S_T$	$-S_T$
Short Put	$-(40 - S_T)$	0	0
Long Call	0	0	$(S_T - 50)$
Total Payoff	–40	$-S_T$	–50
Total Profit	$-40 + 42.61e^{0.05} = 4.79$	$-S_T + 44.79$	$-50 + 44.79 = -5.21$

As shown in the table, the maximum profit is 4.79.

44.   Solution: E

At expiration the price is 50 and both options are "out-of;the-money" eliminating answers (A) and (B). With a strike price of 45 and a minimum stock price of 46, option A is never in the money, eliminating answer (D). With a strike price of 55, option B will be in the money at the time the stock price is 58, eliminating answer (C) and verifying answer (E).

45.   Solution: C

The change in the futures contract in the three month period is

$$200[Se^{0.75(0.02-0.04)} - 1100e^{1.0(0.02-0.04)}] = -100$$
$$197.022S - 215,643,708 = -100$$
$$S = 1094.01$$

46.   Solution: B

Answer (A) is false because naked writing involves selling, not buying options.

Answers (C) and (D) are false because it is an American option that can be exercised at any time.

Answer (E) is false because being in-the-money means there is a payoff, not necessarily a profit.

47   Solution: B

Writing a covered call requires shorting the call option along with simultaneous ownership in the stock (i.e., the underlying asset).

48.   Solution: E

The payoff for the 45-strike call is $12 = \max(0, S - 45)$, so $12 = S - 45$ and thus $S = 57$.

The payoff for the 135-strike put is $\max(0, 135 - S) = \max(0, 135 - 57) = 78$.

49.   Solution: D

The customer pays 500 to purchase the options. If the option is not in the money, the investor loses the 500. If the option is in the money the investor will have a payoff and thus a loss of less than 500. Hence the maximum possible loss is 500.

50.   Solution: B

The investor received 7 (bought the 70 put for 1 and sold the 80 put for 8). To break even, the investor must lose 7 on the payoff. The purchased put cannot have a negative payoff. However, if the index is at 73 upon expiration, the investor will lose 7 on the 80 put (and have no positive payoff on the 70 put).

51.   Solution: B

First, find the prepaid forward price as

$$F_{0,1}^P = 35 - PV(divs) = 35 - 0.32(e^{-0.04*2/12} + e^{-0.04*8/12}) = 34.37.$$

Next, the forward price is

$$F_{0,1} = F_{0,1}^P e^{rt} = 34.37055 * e^{0.04} = 35.77.$$

52.   Solution: C

Consider the first three answers, which are identical except for the forward price. The short sale proceeds of 100 can be lent at 3%. At time one the investor has 103. If the forward price is less than 103, the investor can buy a share for less than 103 and use that shore to close out the short position, leaving an arbitrage profit. Hence (A) and (B) represent arbitrage opportunities while (C) does.

It is not necessary to evaluate (D) and (E). However, as a check, the stock is purchased for 100.5 and with interest at time one the investor will possess one share of stock and owe 103.565. If the short forward contract requires selling the share for more than 103.565 there will be an arbitrage opportunity. Both (D) and (E) have the forwards priced higher and therefore provide arbitrage opportunities.

53.   Solution: D

If F is the forward price, K is the strike price, c is the call option price, p is the put option price, v is the annual discounting factor due to risk-free interest, and t is the number of years, then we have the put-call parity formula

$$c - p = v^t \left(F - K \right).$$

Using the data for the rice commodity,

$$110 - p = \left(e^{-0.065} \right)^4 (300 - 400) \Rightarrow p = 110 + 100 e^{-0.26} = 187.11. \; .$$

54.   Solution: D

The present value equation is $\dfrac{P}{1+r_1} + \dfrac{P}{(1+r_2)^2} = \dfrac{P_1}{1+r_1} + \dfrac{P_2}{(1+r_2)^2}.$

Multiplying both sides by $(1+r_1)(1+r_2)^2$ yields

$$P\left[(1+r_2)^2 + (1+r_1) \right] = P_1(1+r_2)^2 + P_2(1+r_1)$$

$$P = \frac{P_1(1+r_2)^2 + P_2(1+r_1)}{1+r_1 + (1+r_2)^2}.$$

55.   Solution: A

This type of box spread is a long position in a synthetic forward (long call and short put) and a short position in a synthetic forward at a higher strike price (short call and long put). The payoff is the guaranteed positive difference between the strike prices. With $L > K$, the box spread is equivalent to $c(K) - p(K) - c(L) + p(L)$.

A bull spread using calls is $c(K) - c(L)$ and a bear spread using puts is $p(L) - p(K)$. To reproduce the box spread both spreads must be purchased (long position).

56.   Solution: E

Cash flows like those of a short stock position are created by shorting both a forward and a zero-coupon bond.

57.   Solution: C

All but (C) reduce risk by locking in a given result. Answer (C) involves taking on additional risk.

58.   Solution: E

Derivatives are unlikely to simplify reporting.

59.   Solution: E

The payoff table for the long stock, the long put and the short call is, where S is the stock price at expiration:

	$S <= 40$	$40 < S < 50$	$S >= 50$
Stock	S	S	S
Put	$40 - S$	0	0
Call	0	0	$-(S-50)$
Total	40	S	50

Only Graph E is consistent with this table.

60.   Solution: E

Buying a put at 8.60 and selling a call at 8.80 limits the sale price to the 8.60 -- 8.80 range. Brown also receives a premium from selling the call.

61.   Solution: A

A put option is in-the-money if the current stock price is less than the strike price, at-the-money if these two prices are equal, and out-of-the-money if the current stock price is greater than the strike price.

Note that if the current stock price is less than the strike price 70, then the current stock price must be less than the strike price 80. Since option A is a 70-strike put and option B is an 80-strike put, we conclude that if option A is in-the-money, then option B must be in-the-money.

62.   Solution: E

The future value of the put premium is $7(1.03) = 7.21$. If the asset value falls the profit is max(0, $130 - 60) - 7.21 = 62.79$. If the asset value rises, the profit is max(0, $130 - 125) - 7.21 = -2.21$. The expected profit is $0.5(62.79) + 0.5(-2.21) = 30.29$.

63.   Solution: C

In the second year of the swap contract, Company ABC has the following interest payment outflows:

Existing debt: $2{,}000{,}000 \times (\text{LIBOR} + 0.5\%) = 2{,}000{,}000 \times (4.0\% + 0.5\%) = 90{,}000$.

Swap contract, fixed rate, to the swap counterparty: $2{,}000{,}000 \times 3.0\% = 60{,}000$.

Also, in the second year of the swap contract, ABC has the following interest payment inflow:

Swap contract, variable rate, to the swap counterparty: $2{,}000{,}000 \times \text{LIBOR} = 2{,}000{,}000 \times 4.0\% = 80{,}000$.

Thus, the combined net payment that Company ABC makes is:

$(90{,}000 + 60{,}000) - (80{,}000) = 70{,}000$, which is an outflow.

64.   Solution: A

The reinsurance company pays Libor + 0.50%, which is 1% + 0.50% or 1.50% and receives the swap rate which is the treasury rate plus the swap spread or 2% + 0.20% = 2.20%.

The net payment to be received is therefore:

$(2.20\% - 1.50\%) \times 2{,}000{,}000 = 0.7\% \times 2{,}000{,}000 = 14{,}000$.