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Abstract

The 1974 passage of ERISA halted the evolution of the actuarial pension model. This frozen model was unable to incorporate the emerging science of financial economics, which in turn revealed fundamental flaws in the model. Contrary to the teachings of financial economics, the actuarial pension model anticipates expected outcomes without reflecting the price of risk. It then camouflages the risky distribution of outcomes by various smoothings and amortizations.

The flawed pension model has caused widespread, though rarely recognized, damage to pension plan stakeholders. This paper illustrates the flaws and the injuries they cause.

To protect the pension system and the vitality of our profession, we urge pension actuaries to reexamine and redesign the model. The new model must incorporate the market value paradigm and reporting transparency that is rapidly becoming a worldwide minimum standard in finance.

Introduction

At ERISA’s enactment in 1974, the pension actuarial model was highly developed but still evolving. In the previous two decades, actuaries had adapted the model to handle the migration of plans from insurance companies to trustees and from fixed income investments to equities. Pension actuarial methods and assumptions were well suited to providing smooth contribution budgets for sponsor funding.

The actuarial model was less suited to financial measurement and reporting, and it did not adequately protect the members of plans with weak sponsors. Further, the model had not incorporated the nascent science of financial economics. (Also known as “finance,” financial economics is a branch of microeconomics that comprises two fields often identified as “corporate finance” and “investments”).

The timing of ERISA was inopportune for the continued development of the actuarial model. ERISA froze many aspects of the model into law and critically altered the pension actuarial culture. Subtly but certainly, the focus of pension actuarial creativity turned away from evolving the model to satisfying clients who needed to cope with ERISA.

Over time this new focus became a “game” played by consulting actuaries (trying to achieve client objectives despite, but notionally within, ERISA’s strictures) and regulators and legislators (often reacting clumsily to the “creativity” of some actuaries). The result has been a myriad of overlapping, all but contradictory, rules that have made the operation of defined benefit plans excruciating. At the Enrolled Actuaries meeting, Segal and Manning (2002) summed up the resulting debacle in a presentation entitled “Stop the Insanity,” which expresses the common exasperation of actuaries, sponsors, regulators, and participants.

With the ERISA freeze and the shift of creative focus to the ERISA game, the model had little room, and the practicing actuary had little will, to incorporate important lessons from financial economics. Some elements of financial economics¹ did not conflict with ERISA and the

¹ Especially the efficient frontier of Markowitz (1952) and the Capital Asset Pricing Model of Sharpe (1964), Linter (1965), and Mossin (1966).
existing pension actuarial model. Many pension actuaries have mastered and employed these tools.

Other teachings of financial economics (beginning with Modigliani and Miller (M&M, 1958)) conflicted with ERISA and have not been integrated into the actuarial model. Black and Scholes (1973) provided a sophisticated way to deal with financial options. Merton (1974) applied the option approach to the valuation of corporate securities and Merton (1977) analyzed financial guarantees like those offered by the ERISA-established PBGC. Pension actuaries have never, to our knowledge, used option technology to value options embedded in defined benefit plan liabilities, nor even to value plan liabilities in the context of the financial relationship between defined benefit plans and their sponsors.

Most pertinently, a sequence of work applying financial economics to defined benefit plans arrived during ERISA’s first decade and was ignored by the actuarial profession.2

The lessons of M&M, Black and Scholes, and the defined benefit sequence challenge and threaten the existing actuarial model. Since the mid-1980’s, financial engineers (i.e., those who profitably apply financial economics to the design of securities and transactions) have shown that they can exploit financial systems that ignore the teachings of finance. Because financial engineering is grounded in the world of markets (and the no-arbitrage model of pricing financial assets and liabilities), it can dominate the exploited disciplines.

As other financial professions have adapted to and capitalized on these developments, the response of pension actuaries has been dilatory. Although we have introduced the principles of modern corporate finance and investment into our syllabus, we have yet to test the actuarial pension model against these principles. Such a test would reveal pervasive fault lines in the model. Its lack of transparency hinders and misdirects plan sponsors and investors in their decision-making. Better informed market participants are able to exploit the arbitrage opportunities offered by the actuarial work product. The following problems are illustrative:

- Pension accounting conceals volatility and risk and anticipates unearned risk premiums.
- Public pension plans transfer risk to future generations through flawed funding practices, noneconomic transactions such as pension obligation bonds, and misguided design features like skim funds.
- Pension benefits are mispriced in negotiations and other compensation decisions, to the detriment of taxpayers and shareholders.
- Huge unfunded pension liabilities ("legacy costs") remain in the steel industry and elsewhere.
- Plan participants bear creditor risk that they are unable to evaluate or diversify.
- The assumption selection process unduly influences investment decisions and has an unhealthy connection to executive compensation.

This paper illustrates the impact of financial economics upon the venerable and vulnerable actuarial model. We call upon practicing actuaries to prepare for the inevitable application of financial economics to defined benefit finance (and to recognize several exploitations that have already occurred). The professional response must be to learn the science, recognize where it must be applied, support informed legislation and regulation, and direct our creativity to designing defined benefit structures that build upon the science of finance.

Part I: Some Corporate Finance Principles

In this section, we state several principles that are universally accepted in financial economics and almost as universally violated by the actuarial model.

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**Principle 1: $1 million of bonds has the same value at $1 million of equities.** This is a tautology, of course, and no actuaries would dispute it. Yet the actuarial pension model, by focusing on expected returns while ignoring the market price for risk, implies that higher expected future values can be translated into higher present values. Consider a $1-million portfolio of 10-year zero-coupon Treasuries yielding 5% annually, and a $1-million portfolio of equities expected to return 10% annually. They have different 10-year expected values, $1,629,000 for the Treasuries and $2,594,000 for the equities. Yet, the present values of the returns of the two portfolios, when correctly discounted to reflect risk, are equal, because the value of a portfolio must equal the value of its returns.

The equality of the value of returns of all marketable securities is not an arbitrary quirk of financial economics; it is a fact on which financial transactions such as swaps are based. Swaps are agreements between two parties to exchange the return on two market instruments, and they give powerful insight into the arbitrage pricing that underlies financial economics. Understanding why swaps have a zero value, and why the actuarial model fails to show this fact, would lead pension actuaries far toward understanding the fundamental flaws of their current model.

Suppose a securities dealer offers you the following transaction. (We assume that there are no taxes or other frictions and no credit risk on either side.) Ten years from now, she will pay you the 10-year accumulation of $1,000,000 invested today in the S&P 500 Index; and you will pay her the 10-year accumulation of $1,000,000 invested today in 10-year zero-coupon Treasuries.

How much will you pay up front for this deal? Quite a lot, if you look at your expected net payoff: an expected accumulation of $2,594,000 of equities minus $1,629,000 for the Treasuries. The fair price, though, is zero. If you pay anything more than zero, the dealer can assure a profit as follows:

- a. She pockets your up-front payment.
- b. She borrows $1 million at the Treasury rate, with all interest and principal due in 10 years.
- c. She invests the loan proceeds in the S&P 500. During the next 10 years, she earns the S&P return on her $1-million investment.
- d. At the end of 10 years, she receives your payment of the Treasury accumulation and repays her loan.
- e. She pays you the equity accumulation to fulfill her obligation under the swap.

The dealer has profited by your up-front payment without risking any capital. Therefore, in financial economics terms, the present value of the return on $1 million of equity, minus the present value of the return on $1 million of Treasury bonds, must equal zero. You can not get this answer by applying an actuarial discount rate to the expected payoff.

Another way to see that the correct up-front payment is zero is to note that, as a riskless borrower, you could do the borrow-to-invest-in-equity transaction yourself, without the help of the dealer.

These results can easily be generalized by substituting corporate bonds or any other market portfolio for the equities or the Treasuries.

**Principle 2: A fair trade of a marketed security or portfolio must occur at a market price.** There are many exceptions of course, in which the party buying higher or selling lower than the market price does so voluntarily to gain an advantage not available in a regular market transaction. In the absence of such special circumstances, a trade away from market price should not be acceptable to a party who could have transacted in the public markets.

To illustrate this principle, we consider again the equivalence between a $1-million equity portfolio and a $1-million Treasury portfolio. Only the marginal investor is neutral between

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these two portfolios. Those with greater risk tolerance will prefer the $1-million equity portfolio. They may even prefer, say, $800,000 of equities to $1 million of Treasuries as a long-term holding. Suppose that such an individual inherits a $1-million Treasury portfolio and wants to exchange it for equities. He would have a right to a full $1 million of equities. Although he would regard even a lesser amount as an improvement over the Treasury portfolio, if he gets anything less than $1 million of equities, he is surely being cheated by a counterparty who is enjoying an unwarranted profit.

Note that this principle does not depend on the investor’s risk preferences. Nor does it depend on the efficiency or rationality of market prices; it depends only on their availability.

Principle 3: All parties to market transactions are entitled to full current information on the market prices of the relevant assets and liabilities. Transparent and timely financial reporting is necessary to ensure the application of Principle 2 in the financial markets.

Principle 4: A liability is valued at the price at which a reference security trades in a liquid and deep market. A reference security (or portfolio) has cash flows that match the liability in amount, timing, and probability of payment. This principle follows from the fact that a company’s pension liabilities are similar to debt. Their fair value should be found by discounting at the rates applicable to debt with similar creditworthiness, after factoring in the collateral provided by the pension fund. Suppose that an investor is choosing between two corporations that differ only in that one must pay $1,629,000 to pensioners in ten years while the other must make an identical payment to financial creditors. (We assume that any collateral and covenants afford equal protection to the recipients of the two obligations.) These companies are in the identical financial position and must have the same value.

We begin by illustrating this principle with the pension liability of a sponsor with no default risk. The liability consists of a single pension payment of $1,629,000 due in ten years. Our reference security for this riskless liability is a 10-year zero-coupon Treasury, which is currently priced to return 5% annually. A $1-million portfolio of such Treasuries would mature for $1,629,000 and match the liability. The liability therefore has a value of $1 million. We arrive at the same result, of course, by discounting the pension payment at the 5% market rate of the reference security.

Pension liabilities comprise a series of cash flows rather than a single flow. Theory suggests that we should use zero-coupon securities to discount each cash flow, thus using a full discount rate curve. In practice, we use a reference portfolio that approximates the liability cash flows in amount, timing, and probability of payment. We then discount the entire liability cash flow at the internal rate of return of the reference portfolio, a process that is functionally equivalent to using an entire discount rate curve.

The reference portfolio must reflect the risk of the liabilities. Riskless liabilities, as in our illustration, must be measured with a riskless reference portfolio. Pension liabilities that are subject to default require a reference portfolio of comparable creditworthiness. Note that we use reference portfolios specifically to measure liabilities; we do not put them forth as recommended investments for the pension assets.

The actuarial pension model departs significantly from the finance model when it values plan liabilities using the expected return on plan assets. Suppose that equities are expected to return 10%. Then a $628,000 equity

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4 “Probability of payment” refers to the entire probability distribution of payments, from zero to full payment.
5 The FAS 87 double-A rate may be reasonably close to the correct rate for the well-funded pension liabilities of strong sponsors, but is too low for unsecured retiree medical benefits or supplemental executive retirement plans of weak sponsors.
A portfolio would have an expected 10-year value of $1,629,000, and many pension actuaries would regard such a portfolio as fully funding the plan. The actuarial pension model discounts liabilities at the expected return on the assets held to fund these liabilities; it ignores the risk.

The expected return on assets held to fund a debt does not affect the value of the debt. If a corporation borrows $1 million and invests in its business, its debt at the date of issuance is clearly $1 million. We do not discount the debt at the expected return on general corporate assets, even though the debt proceeds may have purchased those assets and those assets may in turn provide funds for servicing the debt.

Alternatively, suppose that instead of investing the entire $1-million proceeds in the operating business, the company sets aside $628,000 in a “Debt Repayment Fund” invested in equity. It expects this equity to grow sufficiently to meet the debt service schedule. May the company now report that the $628,000 Debt Repayment Fund fully offsets the debt, and the remaining $372,000 of the proceeds represents an increase in net worth? Of course not, no more than the company could persuade its bondholders to exchange their $1 million of bonds for $628,000 of equity.

Changing the words “Debt Repayment Fund” to “Pension Fund” does not alter the financial reality. The valuation of the liability does not depend on the expected return of the assets from which the company expects to meet the liability, whether they are earmarked bonds, equities, or internal investments in the company’s business.

Consider two companies with identical balance sheet strength and identical pension obligations, but different pension asset allocations. These companies do not have different pension liabilities; they have different assets. If one generates higher returns, it does not thereby lower its liability and expense; it raises its assets and revenue. And it does so only after the higher returns have been realized, not when they are merely expected.

Although the expected return on plan assets is not pertinent to the measurement of liabilities, asset allocation can have a second-order effect on liability value. This “collateral effect” derives from the benefit security role played by plan assets when the sponsor is subject to default risk.

For example, if a below-investment-grade sponsor puts up matching Treasury securities as collateral for its pension promise, the promise becomes riskless and valuable. If the same sponsor underfunds the plan or mismatches the assets and liabilities, a junk bond discount rate may appropriately reflect the lower value of the promise. The importance of the collateral effect varies with the creditworthiness of the sponsor – for a very strong sponsor it is minimal, and the value of the liabilities will be high and almost independent of the asset allocation.

To summarize: Financial economics measures a liability by using the discount rate curve embedded in a reference portfolio – a portfolio that matches the liability. Such a portfolio is used because of its similarity to the obligation, not because it is a recommended investment policy. It is incorrect to use the expected return on riskier, non-matching assets to discount the liability payments.

Although we recognize the theoretical and practical difficulties in developing a precise discount rate curve, actuaries should agree that like liabilities must be valued at like rates. We may then focus on selecting discount rates within the relatively narrow range implied by this principle, instead of estimating irrelevant equity risk premiums.

Principle 5: Risks are borne and rewards are earned by individuals, not by institutions. Intergenerational risk transfers often go unnoticed because observers think of the pension fund or the plan sponsor as both the bearer of the risk and the beneficiary of the risk premiums. Public plan risks, though, are borne by taxpayers, not by governments. Private plan risks are borne by shareholders, not by
corporations. Risk preferences are not a property of institutions, and it is not enough for the plans or the sponsors to receive the risk premiums for the risks they run. Those risk premiums rightly belong to the specific individuals who bore the risks.

Part II: Actuarial Violations of Corporate Finance Principles

Actuaries would agree that their practice departs sharply from most of the principles set forth in Part I. Even those actuaries who accept these principles may assert that as a long-term, self-correcting system, the actuarial pension model is sound despite its violations of the corporate finance principles. We now illustrate some of the practical and costly ways in which the actuarial pension model misleads users of the work product.

Violation 1: Transferring risk to future generations. Apart from theoretical issues, what is the practical problem with regarding $628,000 of equities as fully funding the pension liability that we valued at $1 million in Part I? Suppose that Generation 1 (today’s stockholders for a corporate plan, or today’s taxpayers for a public plan) receives $1 million of wage concessions from employees in exchange for the pension promise described in Part I. Following ASOP 27, but violating Principle 4, the liability is valued at only $628,000 under the assumption of equity investment. Gen 1 duly puts up $628,000, which is invested in equities. Ten years from now, Generation 2 will pay any shortfall, or receive any excess, of today’s $628,000 relative to $1 million of Treasuries. Gen 2 can expect the equities to grow to match the Treasuries over time, so its expected payment is zero. To value Gen 2’s position, however, we must adjust the expectation to reflect the negative value of its risk position.

Is this adjustment necessary even if Gen 2 is a generation of financial risk-takers? Yes – let’s even suppose that Gen 2 members are so exuberant about equity investment that they prefer a 10-year holding of $628,000 of equities to $1 million of Treasuries. In the public markets (through a dealer or through personal leverage), they could have gotten the deal described in Principle 1 – $1 million of equities versus $1 million of Treasuries. Under Principle 2, which sets a market value standard for transactions, they have been cheated out of $372,000.

Another way to illustrate the problem is to observe that Gen 2 members should have (or plan to have) personal portfolios with mixes of risky and riskless investments that reflect their personal risk preferences. Their responsibility for the new pension benefits adds risk but not expected return. To restore their optimal investment positions, they should now act to offset that leveraged pension risk by adjusting their personal portfolios.

How can Gen 2 members counteract this pension risk? They can sell $628,000 of equity from their personal portfolios and buy $1 million of the matching Treasuries to offset the gain or loss in the pension fund. Where does Gen 2 get the extra $372,000 needed to carry out this hedge? Sorry – the actuary gave that to Gen 1, who effectively collected $372,000 of future risk premiums on the equity investment without bearing any of the risk. So Gen 2 is either out of pocket $372,000 to eliminate the risk, or is left bearing risk that hedge or arbitrage pricing tells us is valued at $372,000 – the cost of converting to a risk-free position. This result of course follows from the fact that Gen 1 underpaid for its pension promise by $372,000.

The equity investment does not, by itself, cause the intergenerational risk transfer. The problem

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6 Plan participants may also bear risk. For private sector plans, taxpayers and the shareholders of other corporate plan sponsors may also bear risk that is nominally borne by the Pension Benefit Guaranty Corporation.

7 A longer chain of generations makes it more difficult to identify the winners and losers. Gold (2002) analyzes how each generation does unto its successor what its predecessor has done unto it. The first generation is a clear winner, the last a clear loser, and, in a stationary population, the other generations all suffer smaller losses.
lies in anticipating risk premiums to justify funding only $628,000 rather than $1,000,000. Suppose Gen 1 paid in $1,000,000 – the true liability – which was invested in equities. Then Gen 2 would be receiving the excess or paying the shortfall of $1 million of equities relative to $1 million of Treasuries. This position is identical to the swap described in Principle 1 and has a fair value of zero. Gen 2 members can run this risk, knowing that they are being fairly compensated for it. If their risk tolerance is already saturated by their personal portfolios, they can hedge the pension risk by selling $1 million of equities and either buying $1 million of bonds or paying down $1 million of debt. Equity investment is not unfair to subsequent generations, if they receive market compensation for their risk and are able to hedge their risk in the public markets.

Note the importance of distinguishing the two taxpayer generations from the pension fund and its sponsor, under Principle 5. In our illustration, the risk bearers are the Gen 2 taxpayers, not the plan or plan sponsor or Gen 1. Those Gen 2 taxpayers are entitled to any risk premiums earned in respect of the risks they run.

Violation 2: Underpricing pensions in compensation decisions. In the example above, Gen 1 received $1 million of wage concessions in exchange for the $1-million pension promise; it paid only $628,000, passing on a $372,000 cost to Gen 2. More likely, though, the sponsor and union actuaries agreed on an equity rate to value the $1-million pension at only $628,000. Because of this underpricing, Gen 1 exchanged $1 million of pension value for only $628,000 of wage concessions. For these wage concessions, Gen 1 paid $628,000 in pension cost and Gen 2 “paid” $372,000 (by carrying risk that was worth $372,000, the price the market would pay someone to bear that risk, or charge for eliminating it).*

To prevent this underpricing, we must follow Principle 4 and use a discount rate that recognizes pension plans for what they are: obligations that closely resemble debt and should be valued in the same way. This discount rate should be nearly riskless for well-funded plans of solid sponsors.

Violation 3: Actuarial/accounting processes biasing investment decisions. Advocates of a financial economics approach to pension investing are often accused of indifference to the expected risk premiums of equities compared to bonds. In fact, financial economics not only recognizes risk premiums; it demands them, as a reward for bearing market risk. Shareholders expect companies to take risks in pursuit of risk premiums, but the companies may have limits on their capacity for risk. The shareholder appetite for risk can be satisfied in various ways:

- Companies can take risk in their operating businesses – for example, investing in innovations rather than milking existing cash cows;
- Companies can leverage their balance sheets by borrowing money to repurchase stock;
- Companies can use pension plan leverage by investing pension assets in equities instead of hedging their debt-like pension obligations with debt securities.

Risk taken in one area may preclude more profitable risk-taking in another, so companies must be thoughtful about where they take it. Our purpose here is not to explore the pros and cons of risk-taking in the pension plan versus taking risk elsewhere.\(^9\) Rather, we show how the actuarial and accounting processes bias the decision in favor of equity investment by pension funds.

\(^8\) Black (1980) compares pension leverage to balance sheet leverage, and Tepper (1981) compares pension leverage to action by individual shareholders to increase their equity holdings by selling bonds or borrowing. An interesting recent application of the Tepper-Black principle is the decision by Boots PLC, the UK firm, to eliminate its pension risk by moving from equity to bonds, substituting balance sheet leverage through a stock repurchase.
The actuarial model regards the use of an expected return for risky investments as unbiased. By ignoring the price of risk, however, this practice in fact produces a strong bias toward equities. Consider the management of a large plan sponsor that seeks to lower pension cost by shifting $1 billion of fund assets from bonds to equities, which will increase the expected return. Principle 1, however, tells us that trading $1 billion of bonds for $1 billion of equities does not change the true economic cost of the plan: the respective returns must each have the same $1-billion present value. In determining present value, financial economics does not recognize equity risk premiums not yet earned for risks not yet weathered.

But actuarial valuations and FAS 87 do. The shift will reduce pension expense by perhaps $50 million (using a 5% risk premium), and may reduce the required contribution by a similar amount. These rewards are certain and immediate; any failure of outcomes to match expectations will be revealed and dealt with in future years. The certainty and immediacy stand in contrast to other areas in which the company may take risk, where a favorable outcome must be achieved before it shows up in income.

A second advantage to management of taking this pension risk is that it need not attract attention. Increases in the other types of risk are disclosed in advance to interested parties. Changes in asset allocation and modest changes in the expected return on plan assets have, until recently, generally remained below the radar of investors. FAS 87 conceals the impact of pension risk by smoothing earnings and relegating investment performance to a footnote.

A third, and particularly troubling, “advantage” of pension plan risk-taking, is the very personal one that accrues to executives whose pay is linked to corporate earnings and therefore to the return assumption. They can hope for a boost in the value of their stock holdings and options, and they can be certain of a boost in their earnings-linked compensation. These advantages all arise from a transaction that has no economic benefit to shareholders, according to modern corporate finance. Of course, the advantages turn around to stand as firm obstacles to any decrease in the equity holdings of the pension fund. Only an intrepid subordinate addressing a highly principled CFO would recommend a change that cuts the company’s earnings and cash flow and senior management’s bonuses.

Violation 4: Hypothetical actuarial gains concealing real economic losses. The pension obligation bond (POB) is another manifestation of this actuarial error. The POB illustrates how current taxpayers and third parties (incumbent politicians and investment bankers in this case) can profit at the expense of future taxpayers from actuarial violations of finance principles.

Pension Obligation Bonds originated as a tax arbitrage by state or municipal plan sponsors. The sponsor would issue tax-exempt bonds at below-Treasury rates and contribute the proceeds to the pension fund. There they could be invested in Treasuries to lock in the arbitrage gains, or invested in risky assets in the hope of earning the arbitrage gains plus risk premiums.

Tax rule changes in the mid-1980s shut this loophole and removed the tax exemption for municipal bonds whose proceeds were contributed to pension funds. After some time, investment bankers realized that although these public sponsors could no longer arbitrage the tax code, they could still “arbitrage the actuary” by borrowing at taxable rates and investing in risky assets with expected returns that exceeded the borrowing rates.

Absent tax effects and transaction costs, borrowing at Treasury rates to invest in Treasuries inside a pension plan is an economically neutral transaction. Swapping the Treasuries for other marketable securities executives can increase their pay by an increase in the return assumption that is independent of any asset allocation change.
increases risk together with expected return, and leaves the transaction with an economic value of zero.

States and municipalities that borrow to fund their pension plans must now issue taxable bonds at interest rates that are above Treasury rates. Borrowing at above-Treasury rates (and incurring issuance costs) to invest in Treasuries is clearly a negative-value transaction. Per Principle 1, exchanging the Treasury investments for other marketable securities is a valueless swap that does not change the negative economic value. But the actuary assumes a return on the non-Treasury investments that exceeds the sponsor’s borrowing rate. The resulting drop in current and expected future contributions will exceed the sponsor’s debt service cost. Thus the transaction appears to offer an economic benefit, camouflaging further injury to future generations of taxpayers who bear the risks. In short, POBs leverage the transfer of value from Gen 2 to Gen 1.

Violation 5: Concealing risk by smoothing. Many pension calculations smooth out volatility by relying on actuarial asset values and extended amortization of actuarial gains and losses. In Part III of this article, we refer to the proposed ASOP, Actuarial Asset Values for Pension Plan Valuation, and discuss some issues related to the elimination of asset smoothing.

Here we comment on how the actuarial model hinders investors in evaluating pension risk and understanding the value of the company. Many actuaries attempt to justify smoothing by noting that pension funds are very long-term enterprises, best measured by methods that focus on long-term expectations and treat departures from those expectations as short-term phenomena.

Pension plans may be long term, but the shares of their sponsors are traded minute-by-minute in the markets. We would not think of applying such actuarial measurement techniques to the rest of the sponsors’ businesses. How useful would investors find financial reports that were permitted to reflect similar smoothing of operating results: reporting earnings based on expected rather than actual numbers of units sold, and amortizing the differences over future reporting periods? Smoothing misleads investors by disguising not only the current operating results but the historical patterns that would illuminate the business risk. There is no dispute about market value reporting by open-ended mutual funds, which may be quite similar to pension fund holdings. Fair prices must recognize the current value of the business and allocate the rewards of risk-bearing to the shareholders who actually bear the risk, under Principles 2, 3, and 5.

Even for committed long-term investors, the actuarial view can be justified only by the assumption of powerful mean reversion in equity returns, so that a long-term equity commitment will assure the realization of expected risk premiums as patience triumphs over risk. There is no empirical or theoretical evidence that would support such a view. 11

Actuaries should understand the history and recognize the smoothing of assets and other cost elements as a practical convenience, rather than as a principle of actuarial science. In particular, actuaries should never claim that actuarial asset values convey greater truth or fairness than market value with its “unwaranted volatility.” Nothing in their formal training gives actuaries the ability to discern a truer value than that set by a fair and active market. Surely such an ability cannot be embedded in our mechanical asset-smoothing formulas.

Violation 6: Extended Amortization. Financial principles recognize the immediate impact of actuarial gains and losses and liability increases due to plan amendments. Even accepting our existing actuarial funding methodology, however, amortization periods that are long and overlapping present practical problems when applied to frequently amended plans.

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11 Bodie (1995) shows that equity risk is ever-increasing in magnitude (not in annual average) as the horizon lengthens. Wendt (1999) discusses the Bodie demonstration from an actuarial perspective.
Suppose that a plan offers a flat benefit that, by annual amendment, increases 2% every year. The actuarial methodology includes a 6% return assumption, unit credit method, and 30-year amortization of plan changes – common actuarial practice for decades and still acceptable under current standards of practice. Under these conditions, the funding ratio will stabilize at just 70%, forever.\textsuperscript{12} Is this result professionally defensible?

ERISA’s “current liability rules,” adopted in 1987, have mitigated the problem, but its persistence is indicated by the recent publicity given to the steel industry’s legacy costs. Practices that permit such massive funding failures should inspire a self-examination of actuarial standards and of the kind of rules that actuaries have fought for and against.

**Part III: A Call For Change**

We have set forth several theoretical problems and damaging consequences of the existing actuarial pension model. Now we turn to a discussion of the need for change, the obstacles, and the type of reform that would restore the actuarial profession to intellectual leadership in the pension community. We observe that:

- The insights of financial economics have made our science obsolete.
- Other professions, versed in these insights, have moved beyond us in their understanding of pension finance. Their ability to deliver – or extract – greater value in the capital markets makes radical revision of our science a matter of urgency.
- The current process for setting actuarial standards of practice (ASOPs) is dominated by practitioners and protects existing mainstream practice. It often prevents the use of practices that would reflect modern corporate finance.
- This standard-setting process is unlikely to produce changes adequate to the challenges we face. The profession should organize a separate effort to reconstruct an actuarial pension model that is informed by the teachings of financial economics.

**Falling Behind**

In Parts I and II, we have laid out the case for the obsolescence of the actuarial pension model. Pension actuaries were once a force for progress in financial thought. During the 1960s, for example, actuaries led the change from valuing pension assets at book value to partial recognition of market value. Actuaries aspire to recognition as “the leading professionals in the modeling and management of financial risk and contingent events.”\textsuperscript{13}

In the world of pension finance, this aspiration contrasts with the progress made by other professions. The accounting profession, both worldwide (through the International Accounting Standards Board – IASB) and in the US (via FASB), is on track to overturn its core paradigm (historical cost) in favor of a radical revision (fair value) for financial instruments by 2005.\textsuperscript{14} Financial executives understand how to manage the actuarial model to produce desired appearances with no change in the underlying reality. Financial engineers and investment bankers with CFAs, MBAs, or other corporate finance training are learning to manipulate the model to shed a positive light on transactions that are neutral or injurious to the pension plans’ multiple constituencies.

Although modern investment actuaries are as well trained as these other professionals, the actuarial syllabus division has retarded the integration of financial economics into the pension discipline. Pension actuaries are now commonly seen fighting a rear-guard action against risk recognition, transparency, and other advances. We may find it difficult to admit that core actuarial methods and assumptions have now fallen behind those on which other financial professionals rely.

\textsuperscript{12} Bader (1981)

\textsuperscript{13} Society of Actuaries Strategic Plan (2002).

\textsuperscript{14} Defined benefit pension and other post-employment benefit liabilities are identified as financial instruments that will be excluded from the 2005 project. They are likely to be folded in thereafter.
This failure to keep our core discipline up to date often harms those who rely upon us. Some or all of the problems discussed in Part II – underpricing of benefits, questionable asset allocation decisions, intergenerational inequities – have afflicted virtually all pension plans and their sponsors.

These problems usually derive from undervaluing risk rather than from direct draining of funds and are therefore difficult to discern through the actuarial pension lens. For example, traditional actuarial measurement does not reveal the mischief done by POBs and the bankers who promote them. This mischief has therefore not been widely recognized, so far.  

It is true that ERISA and FAS 87, to which ASOPs are naturally tailored, now dictate much pension work. Because actuaries were then the intellectual leaders in pension finance, APB8 (1966) and ERISA (1974) largely adopted the actuarial pension model, and FAS 87 (1985) carried some of the same baggage. With our own model written into the regulatory framework, our profession has both some responsibility for that framework and some influence to exert in guiding its reform.

Regaining Intellectual Leadership

The current standard-setting process is run by active practitioners whose everyday work enmeshes them in existing practice. (In contrast, the Financial Accounting Standards Board is part of a structure that is independent of other business and professional organizations). The actuarial standards structure is a recipe for incrementalism, focused on narrowing the permitted range of current practice. The resulting standards can even act as a bulwark against practices demanded by financial economics. The nature of the process that establishes actuarial standards of practice thwarts radical revision of pension actuarial methods and assumptions. The lessons of corporate finance and the activities of our sister professions, however, make just such radical revision necessary.

The proposed ASOP, Actuarial Asset Values for Pension Plan Valuation, is a case in point, illustrating the incrementalism of our process. It outlines methods, goals, and limitations for nonmarket valuation of assets that trade everyday in liquid markets. The proposal neither questions nor justifies the actuarial departure from traded values except to note that it is permitted by regulation, may serve sponsor objectives (paragraph 3.2.2), and may smooth “the effects of short-term volatility in market value” (paragraph 3.2.1).

The authors have joined with others in submitting a comment to the ASB that reviews the origins of actuarial asset valuation methods, focusing on the Jackson-Hamilton (1968) paper and its excellent discussions. The proposed ASOP provides a timely opportunity for actuaries to begin leading the integration of financial economics into the pension system. We recognize that the ASOP must continue to permit asset smoothing as a plan sponsor expectation that is woven into the regulatory framework. Our major recommendation is that the ASOP define a best practice – using market value for liquid assets and fair value for other assets. Further, we urge the profession to encourage rather than oppose a legislative and regulatory phase-out of nonmarket values for pension assets.

The use of market value raises questions about the resulting volatility in contributions and financial reports. To the extent that sponsors desire contribution stability, we prefer the suggestion of Charles L. Trowbridge in his discussion of Jackson-Hamilton: Value assets at market and apply smoothing directly to the contributions. Doing frankly what we now do indirectly would reduce the artificiality and obfuscation of the current multiple smoothing levels. (It would also require a statutory change.)

But, see Davies (2001).

For example, ASOP 27 would generally rule out the use of a near-riskless rate to discount the well-funded pension liabilities of strong sponsors, where the assets are invested in risky securities.

The use of market value would also increase financial statement volatility. Actuaries should consider the distinction between operating costs and financing costs and their separate sources of volatility. Financial economics and the developing “fair value” paradigm of accounting teach that:

- The operating cost of a defined benefit plan is the value of newly earned benefits.
- The financing cost of the plan is the decrease in accrued benefit surplus, before contributions and newly earned benefits.

Shareholders bear both the operating and financing costs. Each element corresponds closely to the value and the uncertainty of portfolios of publicly traded securities. The volatility of the pension operating cost is unaffected by asset valuation methodology; it relates primarily to the variability of interest rates and is small in comparison to overall corporate operating costs. The volatility of the financing cost is attributable largely to asset-liability mismatches.

Volatility is a property of markets; it is not a disease for which accounting is the cure. The volatility of defined benefit plan funding status and cost is real, and it is generated primarily by the mismatch of assets and liabilities. Asset-liability matching can sharply curtail the volatility of financing gains and losses, and the purchase of deferred annuities can eliminate it. Good accounting will follow the hedging and reflect the reduction or elimination of economic volatility. In any event, the financial reporting should separate the financing gains or losses from the operating earnings.

Conclusion

We urge the profession to a fundamental reform of the actuarial pension model that replaces principles based on history with principles based on science. The new model would rely on market value. It would reject the use of expected returns that ignore the market price of risk. In transition, practice standards could recognize the regrettable necessity of departing from these principles to satisfy plan sponsor expectations in accordance with existing regulation. The profession would take all opportunities to urge the regulatory regime into harmony with the principles it has newly enunciated. Actuaries would become a force to advance rather than retard the emergence of a sound and transparent pension system.

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References


Society of Actuaries Board of Governors, “Society of Actuaries Strategic Plan,” [Board disseminated to membership for discussion but not yet Board approved], 2002.


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The Pension Forum

Discussions

Mr. Thomas Lowman

Back to the Future
Is the cure worse than the ill?

Introduction

I often found myself in agreement with the authors. I would have been in even more agreement if they had replaced the concept of risk free rates with settlement rates. However, I am fearful of the ultimate result of adopting either approach and think more needs to be said on both sides of the issues raised. Some of my comments are my interpretations of what was proposed and where this would lead us.

To make my comments a little less abstract, I have not always used terms like the “risk free rate of return”. While interest rates will change over time I will assume that the risk free rate of return is 4.5% (long term Treasuries are currently just under 5%), that annuity purchase/settlement rates are 6.5% (somewhat lower than 7% FAS discount rates I might use today) and valuation assumptions with equity risk premiums are 8%.

A. Who bears the risk?

Principal 5 (Risks are borne and rewards earned by individuals, not by institutions) seems like a good place to start. I tell my clients that they bear the risks and rewards of an 8% interest assumption. I assume that the plan sponsor takes the long term view of what is best for the company (or government sponsor) and not what might be best for current shareholders/taxpayers. The idea that a shifting group/generation of shareholders/taxpayers exists is often a secondary issue, which may come up when deciding how quickly to amortize unfunded liabilities. By focusing on each year’s (or day’s) group of shareholders paying their fair share of the cost, the authors define the cost as “the value of newly earned benefits” plus the change in any unfunded liability (excluding contributions and newly earned benefits). I believe that this would mean the following:

1. Liabilities today would be valued at a 4.5% interest rate.
2. The traditional unit credit cost method would be used, i.e. no salary scale.
3. All gains and losses would be immediately recognized for expense purposes.
4. The authors’ main theoretical focus is on expense and not funding since a company could elect to have pension debt just like it has any other type of debt. However, the authors’ hope is that liabilities are more conservatively funded and amortization periods shortened.
5. While unfunded liabilities would be based on liabilities at 4.5% and assets at market value, for funding purposes I wonder whether the authors would charge interest on the net unfunded liability based on the rate the plan sponsor pays for borrowing (reflecting each plan sponsor’s individual credit worthiness). This is only a cash-funding question since the expense determination formula appears to require no amortization.

Using the Principal 5 concept, salary increases would be controlled by future shareholders or taxpayers (or their management). This is why I assume that no salary scale would be used (however, automatic post retirement COLAs would be included).

Theoretically, governmental plans could switch to pay-as-you-go expensing since there is no 411(d)(6) protection, i.e. the only benefits “earned” are those already paid. However, contract law and common sense would probably prevail and a case would be made for prefunding (unless we were dealing with Social Security).
Often when a sponsor takes a long-term view it does so at the expense of current shareholders/taxpayers. The authors make a case that the reverse is true with existing pension expense rules (with the possible exception if pay-as-you-go were the correct method for governmental plans).

B. Disclosure vs. Expense vs. Cash Contributions:

I think that it is helpful to compare current practice vs. the authors' proposal in six areas. I put them into the following matrix:

<table>
<thead>
<tr>
<th></th>
<th>Private (ERISA) Plans</th>
<th>Public (Governmental) Plans</th>
</tr>
</thead>
<tbody>
<tr>
<td>Disclosure</td>
<td>1</td>
<td>4</td>
</tr>
<tr>
<td>Cash Funding</td>
<td>2</td>
<td>5</td>
</tr>
<tr>
<td>Expense</td>
<td>3</td>
<td>6</td>
</tr>
</tbody>
</table>

1. Private (ERISA) Plan disclosure

FAS87 produces an ABO that is (in theory) based on a settlement interest rate (e.g. 6.5%). The authors' methodology would appear to have us use 4.5%. Whether you agree with these exact numbers, there is some difference. Why would a company want to disclose a liability larger than the settlement value? One response is that they don't have to if they buy annuities every year. Buying annuities while an employee is still earning benefits creates a concern over efficiency.

2. Private Plan Cash Funding:

The paper talks about redesigning the pension actuarial model. There is some fuzziness between what might happen for funding vs. expense. I have interpreted the paper as stating that the authors want cash cost to be based on 4.5% interest and market values of assets just as expense would be based on these factors. I expect that the authors would like more conservative funding yet would not require immediate funding of any gains and losses.

3. Private Plan Expense:

FAS87 service cost and PBO and interest cost would also appear to change from a 6.5% basis to a 4.5% basis. However, the bigger concern might be with the use of 9% and 10% rates of return on asset assumptions. This would in effect be replaced by actual returns. Actual returns might not be lower but would be volatile.

Benefit improvement costs are currently amortized. This would be replaced by immediate recognition on the profit and loss statement.

The minimum liability concept already accomplishes much of the framework that the authors want. Differences that still exist include that fact that minimum liability does not pass through profit and loss statements and the difference between using a 4.5% rate vs. a 6.5% rate.

4. Public Plan Disclosure:

Compared to private plans, currently there is even less disclosure in governmental plans of the type that the authors wish to see. GASB requires disclosure of funding progress but liabilities are based on funding assumptions (and methods), which average about 8% and include the equity risk premium.

5. Public Plan Cash Funding:

There is no requirement to prefund. Most prefund based on GASB expense rules.

6. Public Plan Expense:

GASB rules accommodated most pre-GASB cash funding practices. In most cases expense is equal to the cash contribution as long as it fits into some broad actuarial standards. These include 30 year and level percentage of pay (open group) amortization of unfunded liabilities. Interest rates include the equity risk premium and currently average about 8%.

C. One Way Flow of Assets:

The flow of assets between the sponsor and the plan is only in one direction. If the plan is 100% funded using a 4.5% interest rate and earns 8%, the gain generally cannot be removed from the plan and transferred back to the sponsor. While the “friction” of tax laws might not be material
in most situations, the concept will limit the sponsor’s willingness to accept the proposed valuation basis.

D. Pension Obligation Bonds:

I am generally not a fan of Pension Obligation Bonds. As the authors say, they have a net economic value of zero. However, under current rules, the degree to which they transfer value from “Gen 2” to “Gen 1” is limited as long as the change in the unfunded liability is amortized.

E. Impact of Changes:

The authors complain of “incrementalism” yet accept adopting market value as a best practice and not a requirement. This tells me that they understand the difficulties associated with the higher cost and increased volatility their model would create. I similarly interpreted a fuzziness in cash funding comments as an understanding of the realities of volatility.

The authors give examples of financial engineers exploiting our discipline. It would seem that if reserves were held at 4.5%, any cash available in the fund would be spent by these engineers to buy annuities at 6.5% and book an immediate gain for current shareholders/taxpayers. To do otherwise would be to take the long-term view of what is best for the sponsor and would violate principal number 5. Their ideas to dampen volatility seem like a “back to the future” concept: investing in fixed income and buying annuities.

My fear is that this would further accelerate the decline in DB plans. Yet I could have said the same thing when it was suggested that pay-as-you-go funding be replaced by pre funding. Since I don’t think that the mutual fund companies will start using future 4.5% rates of return to extol the virtues of DC plans, I think that DB plans will have a real and competitive disadvantage when the employer compares the cost/benefits provided by DB vs. DC plans.

I assume that the same concepts would extend into post retirement medical areas and create higher expense. Post retirement medical does have some differences including: no cash funding, high fuzzy trend rates, less clear benefit protection and possibility of future nationalized health coverage.

F. Where am I?

So where does that leave me (as a Schedule B signing actuary)? I want to hear more. I am an incrementalist on this topic (as I think the authors pragmatically might be but theoretically are not). I suspect that the authors will correct some of my misunderstanding of their position and hope they go more into detail about what they are proposing (e.g. cash vs. expense). If they do, I expect future commentators to be better able to focus their response and concerns.

Some actuaries have told me they think that the Bader/Gold paper is dangerous. Given the timing of the paper (a time when actuarial value of assets are above market value, there are known material investment losses since prior valuation dates, and very low settlement rates) that reaction is heightened. However, in the long term we should remember the Bader Gold paper does not set standards of practice but rather gives us an eloquent argument that others could make and we need to be prepared to develop argument for or against, to either defend our current assumptions or set a new direction for the future.
Introduction

We agree with Messrs. Gold and Bader (the authors) that progress is needed in actuarial science in general and in pension actuarial science in particular. Furthermore, we think that discussing the models and methodologies that underlie our work is of vital importance. Such discussions must take place within the community of practicing actuaries, rather than solely within the academic community. Practicing actuaries understand in detail the problems and frustrations faced by plan sponsors and by the actuarial profession.

However, as Carl Sagan pointed out: “Extraordinary claims demand extraordinary proof.” The implications of the reasoning put forward by the authors are breathtaking in their scope and import. Significant thought, discussion, and especially testing must take place before actuaries can consider making the changes the authors recommend.

In this discussion of the paper, we will:

- Start with a quick check of the conclusions drawn by the authors against current realities;
- Present some simulation data relating to the investment of plan assets in equities;
- Discuss the underlying model used by the authors and how it might not be appropriate for pension plans; and
- Suggest what actuaries, the profession, and the authors should do next.

Quick Check

Conclusions must always be tested against reality. The authors conclude that actuaries should:

- Use risk-free discount rates to value pension plan liabilities;
- Avoid asset smoothing; and
- Avoid long amortization periods (no mention was made of amortizing unfunded liabilities as a level percentage of payroll, but that is presumably bad as well).

Systematically funded public sector pension plans, over the last 30 years, have generally violated the above rules. If the authors were correct, public sector pension plans should be in deep trouble. Our experience is that public sector pension plans are in far better shape today than they were 30 years ago, despite apparently violating the above rules. If public sector pension actuaries had followed the above rules then prior taxpayers would have paid far more for services rendered than current taxpayers are paying now.

The relatively good condition of today’s public pension systems should at least give one some reason to believe that current actuarial funding methodology has not been too far off the mark.

Some Data

The authors invoke the name of science frequently. It is important to recognize that there is only one principle in science: You start with data, you form preliminary conclusions or theories based on the data, and you test your theories with more data. The process of science begins and ends and begins again with data.

So, let’s start with some data. Graph 1 below is a distribution of the employer cost 20 years in the future for a large state retirement plan.
The Pension Forum

The horizontal axis is the cost of the plan in 20 years as a percentage of active member payroll. The vertical axis is the number of simulation trials, out of 5,000 trials, that produced the cost on the horizontal axis.

Under either scenario, the plan actuary’s behavior is the same: He continues to compute liabilities and costs each year based on the assumption that assets will return 8.25% and inflation will be 3.5%. The cost under either investment scenario is the same at time zero. Over the next 20 years, actuarial gains or losses accumulate and change the plan cost. Graph 2 below shows the average plan cost over the next 20 years under the two scenarios.

Two scenarios are shown in Graph 1: The plan assets are fully invested in cash equivalents, and the plan assets are invested 70% in U.S. equities, 30% in fixed income securities.

A similar simulation compared the employer costs with all assets in fixed income securities with the 70%/30% mix. Table 1 below summarizes some results of these simulations.

<table>
<thead>
<tr>
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<th>100% Cash</th>
<th>100% Fixed</th>
<th>70%/30% Mix</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean Employer Cost at 20 Years</td>
<td>34.64%</td>
<td>26.77%</td>
<td>13.19%</td>
</tr>
<tr>
<td>Standard Deviation</td>
<td>5.00%</td>
<td>16.23%</td>
<td>13.38%</td>
</tr>
<tr>
<td>Probability of Higher Cost</td>
<td>53.1%</td>
<td>63.1%</td>
<td></td>
</tr>
</tbody>
</table>

(For the curious, the above plan is the California Public Employees’ Retirement System (CalPERS). The simulation model used was constructed by one of the authors (McCrory) in connection with the Asset/Liability Management Workshop held periodically by the CalPERS Investment Office for the CalPERS Board. Assumptions concerning future returns for the various asset classes were arrived at using a Delphi technique involving the Investment Office and its consultants. Future returns by asset class were produced by an asset simulation model developed by a consulting firm not associated with either of the authors of this discussion.)
Some Conclusions
What conclusions can we draw from the above analysis?

1. Based on the simulations above, there is a very strong case for a large equity component in the investments of any ongoing retirement plan (more will be said later about terminating or capped plans).
   - Investment in equities produces a lower future average employer contribution than fixed income securities;
   - The average employer contribution is level with an investment in equities; and
   - The transfer of risk to future generations that so concerns Messrs. Gold and Bader is very small; in less than one out of five cases will the equity-laden portfolio produce costs higher than a fixed income portfolio.

Therefore, there is a good and substantial set of reasons why the investments of pension plans include large equity portfolios.

2. The risk to the plan sponsor – measured by the likelihood of increased employer costs – drops when fixed income securities are supplemented by equities.

3. Given that the assumed return of 8.25% produces costs that are roughly level on average, it is a reasonable assumption to use in computing the liabilities and long-term cost of the plan.

Alternative Models
The authors of the paper would undoubtedly dispute the conclusions above. The key point we wish to make is that the authors and we differ not because one of us is right and the other wrong, but because we are viewing a pension plan using different mental models.

The model used by the authors of the paper is one of debt: “…a company’s pension liabilities are similar to debt.” In the case of a capped or terminating pension plan, for which payments will end in 20 or 30 years, and whose payments can be predicted accurately, this is not a bad model to use. In fact this is exactly the model used by insurance companies in terminal funding situations. Clearly, it would take a brave plan sponsor to fund payments ending in say, 10 years with common stocks. However, in the case of an ongoing plan, particularly an ongoing government plan, we feel the debt model has serious limitations.

1. The duration is wrong. An ongoing pension plan has pension payments scheduled for as long as 90 years in the future for current members and their beneficiaries, before even considering future new hires. No debt has a term this long.

2. The dynamics are wrong. When inflation increases, pension liabilities increase: The actuary does not immediately change assumptions, but salaries and cost of living adjustments drive up projected benefits, increasing plan liabilities. In contradiction, the value of debt decreases as inflation drives up interest rates.

3. Payments are not determined in advance. Pension payments depend on inflation, salary increases, rates of retirement, death, disability, and termination, personnel and plan administration and on a host of other factors. We have seen cases in which the appointment of a new chief of police doubled disability rates in one of our
plans. Therefore, benefit payments are much more variable than debt.

4. There is no market. Because payments are difficult to determine in advance, there is no market for pension plan liabilities, other than for retirees or for terminating plans. No insurance company is willing to underwrite a system in which future pay increases or administrative changes could increase its payment stream.

5. What the plan sponsor cares about is costs, not liabilities. Any actuary who has presented an actuarial valuation is aware of this. This is particularly true for public sector plans. If you don’t believe that, then try telling a Director of Finance who just budgeted for a 6% of pay pension contribution that her contribution rate needs to increase to 8%.

6. If pension payments are debt, then so are any other contingent payments. By this logic, a $5 million key man life insurance policy would be a $5 million debt, at least until the policy expires. The existence of an insurance company to bear the risk should provoke some thought, and it brings us to the next point...

7. Lastly, and most important, the fund plays a key role of risk reduction. Under the debt model, each year’s payments must be made by assets allocated to that year. Any asset other than the safest – a zero coupon Treasury – runs the risk of not being able to cover the payment due, and a type of insolvency results.

An ongoing pension plan has more flexibility than that. With assets that can cover several tens of years of payments and that are not allocated to any particular member or year, a pension plan can wait out bad markets. Even if sales occasionally occur in depressed markets, they will be compensated for by sales in good markets. The plan is an ongoing, permanent entity that can stand market risk and that will be compensated for the risk it takes.

The mental model used by actuaries in their work is the pension plan as an insurance company. This is natural enough, given our roots. The outlines of this mental model are as follows:

1. The pension plan is regarded as a subsidiary insurance company that provides deferred annuities to employees of the plan sponsor at cost.

2. The role of the plan actuary is to set a reasonable long-term premium for the plan sponsor to pay, usually expressed as a percentage of active payroll. The computation of plan liabilities and the actuarial or smoothed value of plan assets are only tools in the calculation of the premium.

3. The plan sponsor’s obligation is to pay the annual premium. One might argue that the plan sponsor could also have a contingent liability in the event the sponsor or the plan shuts down. We have no objection to recognizing such a liability, but we note that for most ongoing plans it would be zero; they are very well funded with respect to accrued benefits.

4. The plan sponsor’s liability is not the same as the plan’s liability. The plan sponsor’s liability is for contributions due and unpaid, with the possible addition of a contingent shutdown liability. The plan’s liability is a working number used to generate the actuary’s best estimate of a long-term stable premium, nothing more.

5. The trustees of the plan have an interest in ensuring that the plan sponsor’s contributions are as low and stable as possible. Like an insurance company, the plan competes for other uses of the plan...
sponsor’s funds. If required contributions are high or vary excessively, the plan sponsor may seek another arrangement to provide retirement benefits for its employees.

If we recognize the insurance company model as a valid one (though certainly not the only valid model), current actuarial and pension investment practice is seen as natural and appropriate.

1. As shown in the simulation above, investment of plan assets in equities is eminently sensible.

2. Computation of employer costs using assumed rates of return consistent with equities in the portfolio is reasonable and necessary: It is the best way to calculate long-term stable employer contributions.

3. The employer’s risk is variation in the employer contribution to the pension plan. As shown in the above simulation, for at least some plans at least very little of this risk is transferred to future generations.

4. Since stabilization of the premium charged the plan sponsor is desirable, smoothing of plan assets and long amortization periods are understandable practices. However, we agree with the authors that such approaches may not be “best practice”.

From the standpoint of our current mental model, many of the transactions (“violations”) that the authors find so troubling are instead appropriate and correct. We don’t have the time and space to discuss each of the “violations” the authors cite. Let’s look at just one, Violation 3, biasing investment decisions.

The authors claim that reducing the employer contribution based on the expected return on plan assets biases investments in favor of stocks. They are absolutely right: It does, and it should. Stocks are simply a better long-term investment, particularly for an ongoing pension plan with an indefinite time horizon. As pointed out in the simulation example above, the chances are far better than even that the plan sponsor will be better off with lower contributions after investing in stocks.

Now the authors suggest we should ignore this and compute the plan cost using a risk-free set of interest rates regardless of the asset allocation policy. Their rationale is that the rewards of risk should be taken only after they have been realized. There are two points that should be made here:

1. This approach would force the actuary to compute and the plan sponsor to contribute according to a funding pattern that will probably decrease over time as actuarial gains emerge. If anything, the current generation of stakeholders pays more than it should so that future generations can benefit. This is contrary to the ideal of generational equity the authors espouse.

2. The idea that the rewards of risk should only be taken after the risks have been run is a value judgment. It is not a principle of finance, though it may be a moral or religious principle to some.

The example of Boots PLC cited in the author’s footnote is chilling. This company decided to “eliminate its pension risk” by moving from stocks to bonds in its portfolio. Boots may have reduced or eliminated the variability of its pension contribution for its current retirees and some of its current employees, but it did so by virtually guaranteeing itself higher pension contributions than would have been the case with a significant equity portfolio.

**Which Model to Choose?**

When one of us (McCrory) was a very young actuary, he attended a presentation of a paper in which the author asserted that pension plans were a form of deferred compensation. Based on that assertion, the author concluded that all pension plans should be career average plans with full cost of living protection. In reading the paper, it occurred to Mr. McCrory that a conclusion so far from current practice is a symptom of an incorrect or incomplete model.

Pension plans are not deferred compensation, though they have some attributes of deferred compensation. Pension plans are, well, pension
plans, with their own characteristics, history, and practice. Defined benefit pension plans are big enough and important enough to be regarded in their own right.

Pension plans aren’t debt either: They have some characteristics of debt, but they are not debt. If the financial community wishes to regard pensions as debt, this is not an indication of any deep thought or arcane knowledge. Instead, it is just the natural tendency of people to extend concepts with which they are familiar to new situations, even when the fit between the existing concepts and the new situation is imperfect.

What Actuaries Should Do

In our practice we have become too accustomed to presenting discounted expected values as single point estimates of liabilities and costs. We omit telling our clients about the error bars around the numbers we provide. It is not unusual to hear a client refer to their plan as “103% funded” and then make decisions based on that single, precise, but possibly very inaccurate number. Even the authors base their conclusions on the discounting of expected future cash flows to compute liabilities. They take issue mainly with the discount rate.

If we are to be the “leading professionals in the modeling and management of financial risk,” we should improve our models. Specifically:

- Our models should be stochastic, reflecting variability in both assets and benefit payments.
- Where the plan is ongoing, our models should reflect the impact of future new members.

We can use our stochastic models to check our deterministic calculations. Furthermore, we should use our models to inform our clients of the variability in our cost and funding estimates.

We might take a cue from our casualty cousins. Casualty actuaries provide information to clients based on the client’s risk tolerance. For example a worker’s compensation liability might have a 50% confidence or a 90% confidence level that the actual liability is less than that shown by the actuary. Pension actuaries should begin to provide funded status or pension contribution levels with similar confidence levels. At the very least, a frank discussion on the variability in our computations is certainly in order.

What the Profession Should Do

We agree with the authors that our professional practice needs to be improved. Whatever our disagreements with the authors, we commend them for provoking discussion about our basic practices. In our view, the following are some important steps that should be taken by the profession as a whole.

- **Be a light unto ourselves.** We will not “regain intellectual leadership” by following the principles of another profession. Whether the dictates come from financial economics or accounting, they can result in the misapplication of principles developed in another field to pension plans, which have their own unique characteristics. This was discussed above.

- **Adopt more empirical approaches.** Actuaries tend to come from mathematical backgrounds, rather than from science. This means that our reasoning tends to be axiomatic – we reason from principles – rather than empirical – reasoning from experimental data. The authors’ reasoning is an excellent example of this.

The proliferation of cheap computing power means that we can build reasonably accurate open group, stochastic models of our pension plans. Using these models we can experiment with the plans, testing the impact of asset allocation, funding methods, assumptions, legislation, and regulation in seconds. Such models would also enable us to test the impact of the authors’ proposals.

Moreover, stochastic models help us improve our communications with our clients. Our clients know – even if we don’t tell them – that our estimates are uncertain. Seeing the simulation results displayed graphically and
quantifying the degree of uncertainty can aid our clients’ understanding of their plans immeasurably, and make our job communicating results easier in the bargain.

- **Rely on our practicing professionals.** We find it unfortunate that the authors chose to disparage the process of setting actuarial standards. We prefer to have actuarial standards set by practicing actuaries. We feel that men and women who massage the data, do the cost calculations, meet with plan sponsors, and generally try to keep the pension system (what is left of it) alive are in the best position to apply hard-nosed scrutiny to proposed changes.

- **Fight for the pension system.** The authors of the paper are right when they cite the damaging effects of ERISA on the private pension system. Actuarial technique was frozen in place before the advent of cheap computer power. The mind space of consulting actuaries became full of IRS Code section numbers and provisions; application of financial and simulation technologies lagged. Top corporate management opted out of the pension system altogether, inflating their pay instead. Ham-handed government legislation and regulation has increased the cost of running a pension plan and has driven many employers out of the pension system. Savings plans – 401(k) plans and their kin – have replaced defined benefit pension plans; few expect they will prove to be adequate as the baby boom retires.

Only one in five Americans is covered by a defined benefit pension plan. If government and Taft-Hartley members are excluded, the coverage is lower. It may be too late to save what’s left. The profession needs to be very clear about the need for legislative simplification and reform.

We continue to believe defined benefit pension plans are the best and most efficient way to provide retirement income. If the profession agrees with this, then we must communicate this to others.

**What Messrs. Gold and Bader Should Do**

Obviously we are unconvinced by the paper. We acknowledge that we may be mistaken. What could Messrs. Gold and Bader do to convince us? They could present us with some data.

We suggest Messrs. Gold and Bader build a small simulation model of a pension plan and, if necessary, the plan sponsor. This need not be an overly elaborate undertaking, but it should be complete enough to capture the key elements of an ongoing pension plan. Then, using the simulation model they should demonstrate the impact and superiority of the approaches they espouse.

This would be some work; we volunteer to assist them. But in the end, we will have real examples with relevance to real pension plans to consider. That will be a much firmer basis for decision than the small examples presented in the paper.

**Conclusion**

Practices and procedures developed over decades are due some deference; there are reasons for their evolution. The intellectual and institutional genesis of current practices must be carefully analyzed before they are replaced. On the other hand, there is certainly room for improvement in pension actuarial modeling.

Messrs. Gold and Bader have done well to point out to us what they believe are the implications of financial economics on pension actuarial practice. It is up to us to evaluate their claims critically, test them carefully, and adopt those that past muster.
Mr. Zvi Bodie

As a longtime critic of the same actuarial principles and practices that they criticize, I welcome the initiative taken by Bader and Gold. They have clearly articulated the fundamental sources of error in the actuarial model and indicated how they might be corrected. I would add to their list of references some earlier articles from the financial economics literature that might help to further elucidate and support their arguments. I believe that the seminal paper was “What are Corporate Pension Liabilities?” Quarterly Journal of Economics, (August 1982): 435-52. It was written by the economist, Jeremy I. Bulow, and it is reproduced in the collection of papers which I co-edited with Phil Davis, The Foundations of Pension Finance, published by Edward Elgar in January 2001. My own article on this subject is “The ABO, the PBO, and Pension Investment Policy,” Financial Analysts Journal, September/October 1990. It too is reproduced in The Foundations of Pension Finance.

References


http://faculty-gsb.stanford.edu/bulow/articles/what%20are%20corporate%20pension%20liabilities.pdf
Mr. John Ralfe

Response to McCrory-Bartel Discussion of Bader-Gold

1. McCrory-Bartel comment that by moving its pension fund from equities to matching bonds The Boots Company is “virtually guaranteeing itself higher pension contributions than would have been the case with a significant equity portfolio”.

2. As Head of Corporate Finance at The Boots Company and Member of the Pension Fund Investment Committee I would like to respond to this comment.

3. McCrory-Bartel are right, as far as they go, that if Boots Pension Fund holds bonds, not equities and equities outperform bonds, the Company’s cash contributions will be higher. So far, so obvious.

4. We should not forget, of course that regulations require the injection of cash to maintain solvency, which may be at inconvenient times. Boots was also, by good luck of timing, able to lock-in a surplus, selling equities near their peak, which maintains contributions at their current level for the long run.

5. These are mere quibbles. Since the purpose of Boots is to create value for its shareholders, the real question should be “Is shareholder value reduced or increased by moving to matching bonds in the pension fund?”

6. Pension fund asset allocation, equities versus bonds, has no first-order impact on shareholder value. By holding equities in its pension fund Boots is doing nothing that the individual shareholder cannot do directly. The shareholder can thus adjust her own portfolio in response to Boots’ move by selling bonds in her portfolio and buying equities to retain her chosen equity/bond balance.

7. Moving to matching bonds has some second-order advantages, which materially increase shareholder value.

   - Dividend tax credit – Individuals continue to receive a dividend tax credit, which was removed for pension funds in 1997. This means under the UK tax system it is more tax efficient for individuals to hold equities.

   - Increase in gearing – By reducing pension fund risk, Boots has been able to increase risk directly by repurchasing £300m of its own shares, within the same credit rating from Standard & Poor’s and Moody’s. This in turn creates shareholder value by replacing equity with debt.

   - Reducing transaction costs and management time – The transaction costs have also been slashed from about £10m to £0.3m per annum.

   - Reducing agency costs – Increasing transparency allows shareholders to focus on Boots’ operating performance, without any pension distortions.

In concentrating on shareholders we should not forget the 72,000 members of the Pension Plan. Their security has been increased, since the value of Fund assets should always be enough to pay all accrued pensions regardless of movements in financial markets.
Introduction

In their paper entitled “Reinventing Pension Actuarial Science” and in other writings, Mr. Lawrence N. Bader and Mr. Jeremy Gold have done a great service to the actuarial profession by introducing some of the principles of financial economics to the pension arena.

They have challenged actuaries to debate whether our actuarial science should be classified as “flat world,” “round world” or “star trek” science.

In doing so, they suggest rethinking and revising Actuarial Standard of Practice Number 27 ("ASOP27") which establishes a Standard of Practice requiring the recognition of expected rates of return before the related, additional risk has been endured.

Where this writer believes Bader and Gold are strong is their suggested approach to the measurement of assets and liabilities. They suggest that the best practice for the measurement of assets is market value. They suggest that the best measurement of liabilities uses expected rates of return on assets whose probabilities of repayment are comparable to the probabilities of making the desired benefit payments.

Where Bader and Gold might do more, however, is to address the IMPLICATIONS of a financial economics approach to the measurement of pension finances on:

- **Funding Policy** – How much to contribute and when? Failing to recognize the additional expected earnings consistent with additional expected risk would result in expected decreases over time in the employer contribution rates for pension funds whose portfolios accept such risk. The authors deem this approach to be better than giving the benefit of the potential mismatch between the assets and liabilities to the generation that creates it. How do the authors address the goal of intergenerational equity so common in Public Pension Plans?

- **Investment Policy** – How much risk is appropriate? If a plan sponsor can handle the risk of equities in its pension fund, why not? For Public Pension Plans where risk can be spread over multiple generations of taxpayers, why shouldn’t the risk be taken? Note: In spite of their presumed value, tax-efficient, augmented corporate balance sheets, such as those proposed by Irwin Tepper and Fischer Black, have generally not been put into practice.

- **Benefit Policy** – What level and type of benefits should be provided? Do the parties involved in negotiating benefit improvements really want to value benefit improvements without getting the benefit of advance recognition for risk?

- **Accounting/Expense Policy** – At what rate should pension liabilities be recognized? As the world demands greater transparency in the reporting of assets and liabilities, it is unlikely that anything other than a market value/fair value model will prevail. In such a world, how or should one separate and recognize the reasonably uniform rates of benefit accrual inherent in most pension plans? How should one recognize in the values of accrued benefits the usually volatile rates of discount inherent in the markets? How should one deal with the almost always volatile rates of return on the assets supporting the pension liabilities? Even more than today, will accounting rules drive behavior rather than measure it?

This writer personally believes that the financial economics approach espoused by Bader and Gold is a proper methodology for the measurement of actuarial liabilities.

However, it is not clear that such proper measurement should automatically result in changes in more traditional approaches to funding policy, investment policy and/or benefit policy.

Proper measurement may logically produce better information for disclosure purposes and it is likely to be necessary in a world that
implements transparent, market value/fair value accounting rules. However, for accounting/expense policies, it is not clear how more proper measurement can effectively assist policy makers in their goal-setting for pension plans. In fact, could such proper measurement, if demanded by accounting rules, result in those rules becoming drivers, rather than measurers, of pension funding, investment and/or benefit policies?

A more extensive addressing of these issues would be helpful to this writer.
1. Introduction

We thank our commentators for enriching a debate that we believe is vital to the future of the pension actuarial profession. Before responding to their specific comments, we briefly remark on the scope of our article and our response.

The authors have forty years of combined experience in “traditional” pension consulting and are well aware of the virtues of defined benefit plans. We believe, however, that radical change is now necessary in how actuaries measure liabilities and develop plan costs. Such change must be accompanied by difficulties and dangers and compromises. As Mr. Lowman implies, there may be areas where proposed changes will be worse than the disease. To choose between alternatives actuaries must thoroughly understand the disease and any proposed changes.

To this end, we seek to enhance actuaries’ understanding of finance by focusing initially on its principles rather than on the practical effects of integrating finance into the actuarial process. We have taken on the deliberately narrow issue of liability measurement not because we do not understand investments and not because we do not understand and appreciate the complexity and elegance of the pension actuarial model. We have done so because we believe that pension actuaries who want to integrate the lessons of finance and pension actuarial practice need to begin with just such a narrow focus.

Our commentators have remarked well beyond the scope of our paper. They take some implications into the areas of accounting, funding, investment, and benefit design. For the most part, in our response, we continue our narrower focus with the expectation and intent that these expanded topics will be the subject of future research and writing.

2. Issues raised by Mr. Thomas Lowman

We are pleased that Mr. Lowman has provided a wide-ranging and thoughtful discussion. It is likely that he speaks for the perspective of many practicing pension actuaries today.

2.1 Rates: Mr. Lowman uses various rates of return for stocks, bonds and annuities as examples of what might be available in markets today. Our paper uses a 5% Treasury return to measure liabilities underwritten by a pension sponsor with no default risk. We begin there in order to contrast riskless liabilities and the often risky asset mixes that fund them. Other than the U.S. government, no plan sponsor may be properly described as entirely free of default risk. For the more realistic case of a well-funded ERISA plan sponsored by a strong sponsor, we advocate a “near riskless” discount rate.

We discuss the determination of discount rate curves in Principle 4. To respond to Mr. Lowman, we assume here that rate curves are flat and that 4.5% represents the Treasury curve. Consistent with this floor, the strongest corporate sponsors of well-funded DB plans might properly use a triple-A discount of about 5% while weaker sponsors of funded ERISA plans might use double- or single-A rates of 5.5% to 6%. Unfunded plans (e.g., OPEBs or SERPs) of weaker sponsors would be discounted at much higher rates related to the sponsors’ unsecured borrowing costs (e.g., debentures).

Mr. Lowman hypothesizes a 6.5% rate for a closeout annuity purchase. With interest rates at the levels suggested above, we doubt that such a rate would be available in the market. If the insurance company basis were adjusted to match typical FAS 87 demographic assumptions and to remove expense loads, we believe that the discount rate required to reproduce the annuity purchase cost would fall well within the range we suggest above.
2.2 Principals and Agents:
Mr. Lowman takes issue with our Principle 5, that risks are borne and rewards earned by individuals rather than institutions. He describes what he tells his client, the plan sponsor, who “takes the long term view of what is best for the company (or government sponsor) and not what might be best for current shareholders/taxpayers. The idea that a shifting group/generation of shareholders/taxpayers exists is often a secondary issue.” Here he confuses the roles of principal and agent. The managers, regardless of tenure, are the “hired hands,” the agents, of the shareholders (principals) who own the enterprise. Modern finance recognizes that companies and similar institutions “are simply legal fictions which serve as a nexus for a set of contracting relationships among individuals.” (Jensen and Meckling, 1976, p.310). Jensen and Meckling go on to observe that shareholders are that special group of contractors who own the residual claims on the assets and who have the right to sell these claims without the permission of other contracting individuals.

To the extent that it is possible to say “what is best for the company,” today’s shareholders are “the company.” Managers must of course accommodate themselves to the rules and mores of society but, as managers, they have no higher duty than to act as loyal agents seeking to protect and grow shareholder value.

Mr. Lowman assumes that a long-term view by management conflicts with the interests of current shareholders. The value of a stock, however, is the value of all its future earnings. When management makes an investment that market participants expect will deliver long-term benefits, it delivers value to current shareholders.

2.3 Pension Obligation Bonds:
Mr. Lowman comments that we state that Pension Obligation Bonds have a net economic value of zero, but he believes that the intergenerational inequity is limited as long as the unfunded liability change is amortized. Although we begin our comments regarding POBs with a hypothetically neutral economic example (where the sponsor is able to borrow at Treasury rates), we quickly observe that any borrowing at rates above Treasuries leads to negative value. POBs are issued because they lower the actuarial cost of Gen 1. Because their total economic value is negative, Gen 1’s lower cost must raise the risk-adjusted cost of subsequent generations.

2.4 Actuarial Standards of Practice: Mr. Lowman refers to our criticism of incrementalism in actuarial standards and then points to our own incremental approach to the proposed ASOP in re actuarial asset valuation methods (see “Selection of Asset Valuation Methods” in this Pension Forum). We are concerned that the standard-setting process admits only incremental improvements, even when the times may require radical revision. We point to the accounting profession, which is now considering a radical revision of its core “historic cost” paradigm. Nonetheless, we must make do with what is available. Today that means that recommendations we make to the ASB may be incremental. Note, however, that our preferred standard for the profession would eschew all asset values other than market. When compromise is necessary, we prefer to aim at the best possible future standard, compromising only on the timing of its adoption.

2.5 Immunization/annuitization – Back to the Future?: Mr. Lowman labels as a “back to the future” concept our suggestion that sponsors wishing to reduce or eliminate pension volatility do so via immunization or annuity purchase. To the extent that our pension actuarial roots (e.g., Trowbridge, 1952) precede the massive 1960s shift to equities, he’s right. To the extent that annuities and immunized bonds may better serve participants, shareholders, and interested institutions (e.g., the PBGC), should we and those sponsors not analyze the issues afresh rather than dismiss them as backward? The “modern” actuarial answer, using smoothing to conceal the volatility of mismatched pension assets and liabilities, does not appear to us to carry much forward viability.

2.6 Accounting: Mr. Lowman makes several inferences beyond the content of our paper in the area of accounting. We agree with his inferences that a finance-based accounting model would: i) employ the traditional unit credit method without salary scale; ii) define liabilities that resemble the ABO; iii) use actual
rather than expected returns; and iv) immediately recognize gains and losses (McConnell and Reese, 2000).

Financial economics, and the “fair value” accounting standards under consideration by the IASB and FASB, try to measure liabilities based on the market value of similar promises. Promises related to employment may vary with respect to their contractual certainty, and no rule may be applied blindly to all situations. To the extent that automatic post-retirement COLA’s are contractually defined (by, e.g., a pension plan document or statute), Mr. Lowman correctly appraises the proper financial treatment. While contractually determined future salaries might also be included in current liability measures, we believe that the “implicit contract” to offer regular salary increases does not rise to the level necessary for advance recognition. Economics teaches us that, in a free economy, future salaries will depend on competitive market forces.

2.7 Funding: Inferring further beyond our scope, Mr. Lowman says “I have interpreted the paper as stating that the authors want cash cost to be based on 4.5% interest and market values of assets just as expense would be based on these factors. I expect that the authors would like more conservative funding yet would not require immediate funding of any gains and losses.”

Our paper does not support this interpretation. Unlike measurement, where capital markets data and economic principles may be sufficient to reach conclusions, prescriptions for funding must include social judgments. We have not offered such judgments, although we have noted a symptom of funding failure in our Violation 6. The ways in which actuaries have addressed these issues (SOA, 1996 and CIA, 1998) in recent years illustrates the role that judgment must play. As a matter of economics, we note that before ERISA this was a matter to be decided by the promise maker and the beneficiary. With the passage of ERISA, Congress dealt itself into the equation arguing that the protection of the beneficiaries was a societal issue.

3. Issues raised by Messrs. Robert McCrory and John Bartel

Messrs. McCrory and Bartel defend existing pension actuarial practice and equity investment. Their defense is statistical, based on a model that distributes returns on asset portfolios and concludes that a plan will require lower average contributions if the plan invests in assets that offer higher average returns.

The basis of our paper is financial. It draws on the lessons of financial economics to illustrate how markets value cash flows that exhibit certain properties. As McCrory and Bartel indicate, we spend much time working with examples in which defined benefit plan liabilities are deemed to have certain bond-like or debt-like properties. Our treatise is more comprehensive, however, and worthy of a more careful read. We do not, for example, assert that the proper discount for pension liabilities is the riskless rate. We encourage our commentators and readers to look carefully at our discussion of Principle 4.

3.1 Return Distributions, Statistical Visualization, and Science: McCrory and Bartel imply that we ignore the return distributions of various asset classes and the implications thereof for pension investments and thus for funding. Our paper addresses the measurement of liabilities, which is an important first step towards the development of rational funding and investment strategies.

Because much of their discussion deals with funding and investment issues not raised in our article, we respond to their comments that lie within the boundaries of our article.

McCrory and Bartel assert that their statistical approach is science, while the lessons of financial economics are something else. But we would characterize their procedure of generating their own data from their own assumptions as “visualization” or “illustration,” rather than

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18 For an overview of fair value accounting see FASB (2000).

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science. Principles of financial economics begin, as science demands, as falsifiable hypotheses, which are then tested minute-by-minute and day-by-day in the real world of financial markets. In the fifty-year history of financial economics, very few hypotheses have survived. One survivor, so far, is the hypothesis that riskier assets are priced to anticipate higher mean returns. Thus the existence of, and investor demand for, the "equity risk premium" is, we may agree with McCrory and Bartel, a scientifically supported concept.

McCrory and Bartel challenge our asserted Violation 3, biasing investment decisions. They regard this bias as an appropriate reflection of the superior long-term performance of equity. We would recognize such superiority only as it occurs, not in advance. Discussing Principle 3, we state that "In determining present value, financial economics does not recognize equity risk premiums not yet earned for risks not yet weathered." McCrory and Bartel dispute this statement: "[t]he idea that the rewards of risk should only be taken after the risks have been run is a value judgment. It is not a principle of finance, though it may be a moral or religious principle to some."

Fortunately, we can settle this dispute by observing a transaction that illustrates precisely how the market values future risk premiums. Our discussion of Principle 1 describes a swap in which one party will receive the return on a $1-million equity portfolio and pay the return on a $1-million Treasury portfolio — in other words, that party has acquired the stream of risk premiums. We show how, under arbitrage pricing, that equity risk premium stream must have a present value of zero. If McCrory and Bartel wish to test their rejection of this principle scientifically, they may offer this risk premium stream to investors. They will find that no investor, of any moral or religious persuasion, will pay a positive up-front price for it. But if McCrory and Bartel offer to buy this stream for any positive price, they will find many happy sellers.

Of course, actuaries who anticipate risk premiums in pension valuations do not literally value a $1-million equity portfolio more highly than a $1-million Treasury portfolio. They achieve the same result indirectly, however, when they value liabilities financed by equity more cheaply than the same liabilities financed by bonds. In discussing Principle 4, we have shown why the higher expected return of equity is irrelevant to the valuation of equity-financed liabilities.

3.2 Risk Transfer: Elsewhere, McCrory and Bartel simply dismiss our arguments as wrong, rather than engaging and challenging them on their own terms. They state that "The transfer of risk to future generations that so concerns Messrs. Gold and Bader is very small." Financial economics teaches that the value of risk is measured by the market price necessary to dispose of it. McCrory and Bartel wish to substitute the probability of shortfall ("in less than one out of five cases") as a risk measure. Statisticians will recognize that shortfall probability is an "insufficient statistic" that fails to account for the severity of the dollar shortfall and for its disutility (as gauged by a consensus of investors – the very same consensus that demands and necessitates the equity risk premium in the first place).

To repeat in highly simplified form our argument concerning Violation 1, would you prefer to be taxpayer Gen 1 paying a certain $1-million pension cost, or Gen 2 paying an expected $1-million cost, but more if equity performance is worse than expected and less if it is better? Our article refers to Gold (2002), which shows how the fundamental tool of finance, arbitrage pricing, quantifies the value of the risk borne by Gen 2. To assert that Gen 1 and Gen 2 are equally burdened is to dismiss the overwhelming empirical findings of financial economics that people attach a negative value to risk. To dismiss the risk as "small" because it happens "in less than one out of five cases" is an unacceptable position for those who aspire to be "the leading professionals in the modeling and management of financial risk."

Actuaries are frequently troubled by the implications of equity investments combined with liability discount rates that do not include the equity risk premium. McCrory and Bartel voice this concern:
“This approach would force the actuary to compute and the plan sponsor to contribute according to a funding pattern that will probably decrease over time as actuarial gains emerge. If anything, the current generation of stakeholders pays more than it should so that future generations can benefit. This is contrary to the ideal of generational equity the authors espouse.”

Traditional actuarial practice and education emphasize the virtue of level expected costs over time. When multiple generations invest in risky assets, and use the expected returns thereon to discount liabilities, the allocation of expected costs is level but the allocation of risks – and therefore of risk-adjusted costs – is not (Gold, 2000, p. 31). Finance teaches that we cannot combine risky investments, level expected costs, and equal risk burdens across generations. Now that we know that risk and reward are inextricably tied, we may ask the professionally important question: “what is fair?”

3.3 Principals and Agents Redux: McCrory and Bartel observe that “the plan sponsor [by which they mean the agent of the plan sponsor] cares about … costs, not liabilities. Any actuary who has presented an actuarial valuation is aware of this.” Even if we understand this as an effort to define the profession’s responsibility to plan constituents, it is a parochial view which ignores the interests of the plan’s principal owners. Although the agents of the sponsor (the CFO or the City Comptroller) may care about costs, the informed principal should care about the value of the promises made to employees in exchange for services delivered today. The value transferred is the cost of the promise and is not amenable to traditional actuarial manipulation.

3.4 Which Model to Choose: In their section “Which Model to Choose,” McCrory and Bartel observe that “pension plans aren’t debt” and that “pension plans are, well, pension plans.” Here they make a genuinely important contribution to our dialogue by properly limiting the applicability of debt analogies. Pension contracts constitute securities that are not perfectly replicated in the capital markets. For most pension promises that have attained the status of liabilities, however, the debt model provides an excellent approximation. Fortunately, the debt market reflects a wide variety of contingencies similar to those found in pension payments – credit risk, calls, adjustments in amount (floating rates, inflation-indexed Treasury notes), or prepayment risk (mortgages). Thus portfolios of debt-like instruments may accurately measure much of the financial effect that pension obligations have upon their sponsors.

3.5 What the Profession Should Do: McCrory and Bartel advise the actuarial profession not to “follow … the principles of another profession.” We advise actuaries not to dismiss finance as “the principles of another profession” any more than physicists should dismiss mathematics. Financial economics offers actuaries invaluable tools that describe how markets work, how securities are valued, and how corporations finance their activities. Actuaries possess, in abundance, the capacity to understand finance, indeed to advance it, and to apply its principles to our practices.

4. Issues raised by Messrs. Zvi Bodie, John Ralfe, and Robert North

We endorse Mr. Bodie’s recommendation of the Bulow article, which is two decades old but well worth the attention of readers interested in a financial economist’s view of pension liabilities. We thank Mr. Bodie for his own work in the area of pension finance and for his own article citations.

Mr. Ralfe offers a lucid explanation of the Boots PLC pension fund restructuring. His comment shows how far actuaries will have to raise their game to advise executives interested in how pension plans affect shareholder value. Mr. Ralfe understands perfectly well that the Boots reallocation from equity to bonds raises the expected contributions to the pension plan. Pension actuaries must understand equally well why it also raises shareholder value.

Mr. North asks us to address the implications raised by our paper in the areas of pension plan funding, investment, benefit design, and
accounting. We have extended our remarks in these directions in the preceding portion of our response, and we will refer back to those remarks in our response.

Concerning funding, we address Mr. North’s concern about intergenerational equity in the concluding portion of Section 3.2.

Concerning investment policy, Mr. North asks, “If a plan sponsor can handle the risk of equities in its pension fund, why not?” As we explain in Principle 5 and Section 2.2 above, the “plan sponsor” must not be regarded as an independent financial entity with financial interests that are different from (and superior to) the shareholders or taxpayers who bear the burdens of plan sponsorship.

Concerning benefit policy, Mr. North asks, “Do the parties involved in negotiating benefit improvements really want to value benefit changes without getting the benefit of advance recognition for risk?” See Section 3.3: the “agents” (managers, elected officials) involved in negotiations might want to anticipate risk premiums and thus understate the value of benefit increases, but the “principals” who bear the cost and the risk do not.

Concerning accounting, we address only Mr. North’s broad question, emphasized in his conclusion: “... for accounting/expense policies, it is not clear how more proper measurement can effectively assist policy makers ... could such proper measurement, if demanded by accounting rules, result in those rules becoming drivers, rather than measurers, of pension funding, investment and/or benefit policies?” As we discuss in our paper, measurement under current accounting and actuarial principles clearly influences pension policies now, in ways that can be destructive to shareholders or taxpayers. Until we are shown plausible counter-examples, we will continue to believe that better information would produce better policies.

5. Conclusion

We have taken on the deliberately narrow issue of liability measurement because we believe that pension actuaries who want to integrate the lessons of finance and pension actuarial practice need to begin with just such a narrow focus. The existing pension actuarial model (including its somewhat stochastic sister models that are referred to by McCrory and Bartel) began as a budgeting system for smooth employer contributions at a time roughly coincident with the dawn of modern finance. This budgeting system has been extended to serve many purposes other than budgeting and, in doing so, it has come into conflict with other disciplines that address these same purposes including, at least, finance and accounting. The issue of liability measurement is an ideal base to study this conflict. This is particularly true now that the accounting profession has taken more than a few steps in the direction of agreeing with finance.

The comments on our paper suggest to us three critical insights that we hope readers will take from this work:

1. It is erroneous to attribute to “the plan sponsor” financial interests such as the ability to bear risks or the entitlement to rewards. These attributes belong only to those who actually bear the burdens of plan sponsorship – taxpayers/shareholders.

2. Liabilities are measured without regard to the expected return on risky assets that may be used to fund these liabilities.

3. Outside the actuarial profession, the vast majority of thought leaders in the financial community agree with 1. and 2.

Recent events in the capital markets and corporate world make it increasingly difficult for actuaries to maintain that pension plans are so different from all other financial entities that they must be measured and governed by a long-term self-correcting process that obscures the information to which the ultimate “plan sponsors” are entitled. As Mr. Lowman concludes, the profession must seriously engage the teachings of financial economics and either refute their logical and empirical bases or – as we believe – realign pension practice to accord with these teachings.
References


Society of Actuaries, Pension Forum 9, No. 1, September, 1996.

May 15, 2002

Selection of Asset Valuation Methods
Actuarial Standards Board
1100 Seventeenth Street, NW, 7th Floor
Washington, DC 20036-4601

By e-mail: comments@actuary.org

ASB Board and Committee Members:

We are writing to comment on the Proposed Actuarial Standard of Practice – Selection of Asset Valuation Methods for Pension Valuations.

The proposed ASOP gives the ASB an opportunity to make a positive professional statement by endorsing the use of market value (or fair value, for non-traded assets) as the single best measure of pension assets.

We encourage this definition of a best practice standard within a range of acceptable but notably less scientific measures. We recognize that existing codifications (principally, ERISA, FASB, and GASB) and sponsor expectations and preferences demand a wider range of allowable practices. Fortunately, each of these codifications will permit our recommended best practice.

It is useful to review the origins of the actuarial asset valuation methods. The Jackson-Hamilton (1968)20 paper (and its excellent discussions) is a superb starting place, not only for what it includes, but for a sense of its era implicit in its omissions and its unstated presumptions.

We learn from the Jackson-Hamilton paper that:

- The significant and growing allocation of assets to the equity markets had exposed some of the frailties of earlier book value methods:
  - Book and market values necessarily converge for bonds held to maturity, but not for equities.
  - There is no economic reason to distinguish among dividends and realized and unrealized gains. Differentiation among these may lead to manipulative trading strategies.
  - Equities, valued at market, transmitted volatility to plan contributions. Many actuaries deemed much of this volatility to be spurious. Virtually all actuaries and sponsors found such volatility unattractive.

- The prime function of pension actuaries was to create a sponsor contribution budget. Secondary objectives included compliance with accounting and tax regulations and actuarial soundness. Sponsors wanted smoothness on the one hand and sufficient recognition of expected and achieved equity returns to keep costs low. Jackson-Hamilton framed the entire process as a balance of these objectives in classical actuarial fashion: “[T]he choice [of

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method] will depend on the relative weight assigned to the criterion of smoothness of contribution as compared with fit of value to market.”

Conflicts of interest, real or potential, among shareholders, participants, government agencies and other regulators were not yet a significant issue.

ERISA still lay in the future and APB8 was brand new: “Current legislative proposals (e.g., Senate bills introduced by Senator Yarborough and Senator Javits) to impose stricter minimum funding standards on private pension plans and the rigidity in pension costs resulting from a strict application of the rules in Opinion No. 8 by practicing accountants may force employers to explore the possibility of changing some of the actuarial assumptions, the method of funding, and the method of valuing pension fund assets in order to minimize the impact of any required changes.”

Modern financial and investment principles were in their infancy and beyond the scope of the day’s typical pension actuary: “[A]ctuaries in America have usually disclaimed investment expertise and have been prone to leave asset valuation problems to the employer, trustee, or insurance company.”

Nonetheless, Jackson-Hamilton recognized that: “From an investment standpoint at least, it appears that current market value has been fairly well accepted as the only true measure of asset value.” [Emphasis added] This suggests that the actuarial view of specious volatility (hinted at even in today’s proposed ASOP by the phrase “short-term volatility in market value”) was not a dominant view.

Three decades later, we have acquired some greater insights and encumbrances:

- Volatility is a property of markets; it is not a disease for which actuarial methodology is the cure.

- ERISA, SFAS 87, and GASB 25 permit actuarial asset valuation methods to smooth asset values and ultimately to smooth sponsor contributions and reported expenses.

- Sponsors still desire smoothness of expenses and contributions. Although many know that hedging (asset-liability matching) may be used to reduce volatility, they do not wish to reduce expected returns. They generally prefer to take advantage of the permitted actuarial/accounting smoothings.

We may not be unilaterally able to move client sponsors toward a choice between lower expected returns and volatility, but we have sister professions who may be our allies in such a transition. These include MBAs, CFAs, financial engineers, securities analysts and, trailing slightly behind these others, CPAs. Our own well-trained recent Investment FSAs share the skills and disciplines of many of these professions.

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22 Opinion No. 8 of the Accounting Principles Board (1966).
26 Paragraph 3.2.1.
These professions have preceded us in accepting the teachings of financial economics. They may fully repudiate off-market asset values before we even begin. We are in no small danger of being left behind, with a concomitant loss of credibility and stature among policymakers, regulators and investors.

The proposed ASOP has the potential to be a watershed. We can use it as an opportunity to define market value as our best practice and take a leadership position in encouraging legislative and regulatory reform. Alternatively, we can continue to endorse practices that have lost relevance in a financial world sensitized by episodes of opaque and misleading financial disclosure.

We will forward shortly a paper by Lawrence N. Bader and Jeremy Gold.\(^27\) It outlines some greater challenges to pension actuarial technology and to the remaining pieces of ASOP 4, Measuring Pension Obligations. In doing so, it lays out some of the lessons of financial economics that the authors have learned and applies them to our science. ASB members may wish to review the article for a sense of the world from which the specifics of this commentary letter are drawn.

Finally we outline our recommendations specific to the proposed ASOP:

- Define a **best practice** – using market value for liquid assets and fair value for other assets. Identify acceptable departures from this best practice. We note, however, that until the ASB also identifies as a best practice a market-type valuation of liabilities, the use of market value for assets will not necessarily improve the measurement of funding status.

- Remove references to short-term volatility of assets as a motivation for smoothing and acknowledge that the sole reason for non-market asset valuations is to meet sponsor desires for smoothing contributions and expenses. It does not serve pension actuaries well to suggest that a “true” value of assets lies hidden within volatile markets and that actuaries are especially well prepared to find it.

- Remove paragraph 3.2.2 as presently written. Acknowledge sponsor prerogatives under certain regulations and statutes. Further acknowledge the interests of other constituents, including participants, shareholders, lenders, taxpayers, the Pension Benefit Guaranty Corporation, and others who rely upon our professional representations.

- State in the preamble that we would welcome a legislative and regulatory requirement to use market value for pension assets.

- Make a more explicit statement on the use of market value restarts (for example, in paragraph 3.6). It is not uncommon, particularly in the public plan sector with plans subject to GASB, for actuaries to be whipsawed between requests to raise investment return assumptions when interest rates rise (and market value is likely to be below the actuarial asset value) and requests to restart the actuarial asset value at market when market value exceeds the actuarial value (and interest rates are likely to have fallen). Because ASOPs give both latitude and protection to practicing actuaries, we must recognize that excessive latitude may limit the actuary’s ability to resist this kind of double bind.

\(^27\) The paper speaks for its authors and does not necessarily represent the views of the undersigned.
We hope that the evolving Actuarial Standards of Practice will serve to bring about change sooner rather than later. We would very much like to see the actuarial profession lead the reformation of pension finance, rather than be towed in its wake.

SIGNED

Eleven Fellows of the Society of Actuaries

    Lawrence N. Bader
    Jeremy Gold
    H.J. Brownlee
    Richard Daskais
    Arshil Jamal
    David Kass
    Sven Sinclair
    Margaret M. Warner
    (plus three who do not wish their names on this “public” document.)
As a consulting actuary who works with attorneys in matrimonial actions, I am frequently confronted with the problem of computing the account balance in a defined contribution plan where the marriage occurred subsequent to the date of entry into the plan. Typically in this situation, the pre-marital contributions plus investment earnings thereon must be excluded from the value of the participant’s account balance for equitable distribution purposes.

Before embarking on any computations in the above situation, I try to explain to the attorney that there are two ways to compute the value of this marital asset.

In my judgment, the theoretically correct method is to ascertain the actual contributions over the marriage up to the cut-off date and then add investment earnings at the actual rates earned by the plan over the intervening period. Alternatively (and this should give the same result) we can subtract from the account balance at the cut-off date, the account balance at the date of the marriage brought forward to the cut-off date at the actual investment rates earned by the plan in this intervening period (this, of course, assumes loans are disregarded). This approach is simple to describe and understand, but often difficult (or impossible) to accomplish because the approach requires all the account statements between the marriage date and the cut-off date in order to compute the actual earned investment rates. I call this the exact method.

The second method is simple to describe and understand and even easier to carry out and that is to multiply the account balance at the cut-off date by a coverture fraction—the numerator being service between the marriage date and the cut-off date with the denominator being all service while a plan participant as of the cut-off date (if there are loans outstanding, a decision must be made as to which of the parties is responsible for such loans). I call this the pro-rata method.
Having described both methods, the next question from the attorney is “which is more beneficial to my client?” My response is that I don’t know and in any case that is not a concept that enters my computations. I emphasize that I am an expert, not an advocate. If the past statements are available (and often they are), I will use what I consider to be the theoretically correct approach. If not, there is no choice but to use the pro-rata approach.

Recently I tried to look at the mathematics of each method to see how they compare. My simplified analysis is as follows:

Definitions and Notations:
- Salary at date of hire = S
- Years from plan entry to cut-off date = N
- Years from plan entry to marriage = n
- Annual rate of pay raises = R
- Annual rate of investment earnings = R + a
- Rate of contribution-payable in a single amount at the beginning of each plan year = c %

Total accumulated value of contributions at cut-off date

\[
\left\{ \frac{c}{100} \right\} S \left[ (1 + R + a)^N + (1 + R)^2 \left( 1 + R + a \right)^{N-1} + (1 + R)^3 \left( 1 + R + a \right)^{N-2} + \ldots \right]
\]

\[
= \left\{ \frac{c}{100} \right\} S \left[ (1 + R + a)^N - (1 + R)^N \right]
\]

\[
= \left\{ \frac{c}{100} \right\} S \left[ \frac{(1 + R + a)^N - (1 + R)^N}{(1 + R + a) - (1 + R)} \right]
\]

\[
= \left\{ \frac{c}{100} \right\} S \left[ \frac{1 + R + a - (1 + R)^N}{\alpha} \right]
\]
Therefore, on a pro-rata basis, the amount available for equitable distribution purposes =

\[
\left( \frac{N-n}{N} \right) \left( \frac{C}{100} \right) \left( S \right) \left( \frac{1+R+\alpha}{\alpha} \right) \left[ (1+R+\alpha)^N - (1+R)^N \right]
\]

Accumulation of contributions over the marriage

\[
\left( \frac{C}{100} \right) \left( S \right) \left( 1+R \right)^N \left( 1+R+\alpha \right) \left[ \frac{(1+R+\alpha)^N - (1+R)^N}{(1+R+\alpha) - (1+R)} \right]
\]

We have two expressions for the value of this plan for equitable distribution purposes. The question now is how do they relate? Put another way, under what conditions does I exceed (II), (I) equals (II), (I) fall short of (II)?

First note that if \( \alpha = 0 \) and R is a constant, then the two expressions are equal. Proof of this is to take the limit of each as \( \alpha \to 0 \) using L’Hospital’s rule or what is easier, evaluate the two series putting \( \alpha \to 0 \).

Each becomes: \( \left( \frac{N-n}{N} \right) \left( \frac{C}{100} \right) \left( S \right) \left( 1+R \right)^N \).

If \( \alpha > 0 \) and R is a constant, then \( I > II \)

And \( \alpha < 0 \) and R is a constant, then \( I < II \).

Proof is as follows:

\[
I \geq II \quad \text{if} \quad \left( \frac{N-n}{N} \right) \left( \frac{C}{100} \right) \left( S \right) \left( \frac{1+R+\alpha}{\alpha} \right) \left[ (1+R+\alpha)^N - (1+R)^N \right]
\]

\[
\geq \left( \frac{C}{100} \right) \left( S \right) \left( 1+R \right)^N \left( \frac{1+R+\alpha}{\alpha} \right) \left[ (1+R+\alpha)^N - (1+R)^N \right]
\]
The Pension Forum

\[
\frac{1}{N} \left[ \frac{(1 + R + \alpha)^N - (1 + R)^N}{\alpha} \right] > \frac{(1 + R)^{N-n} \left[ (1 + R + \alpha)^{N-n} - (1 + R)^{N-n} \right]}{N-n} \alpha
\]

Note that the left hand side is the arithmetic mean of the following N quantities:

\((1 + R + a)^{N-1}, \ (1 + R + a^2)^{N-2}, \ (1 + R + a^3)^{N-3}, \ (1 + R)^2, \)

\(\ldots, \ (1 + R + a)^1, \ (1 + R)^{N-2}, \ (1 + R)^{N-1}\)

The right hand side is the arithmetic mean of the following \((N-n)\) quantities:

\((1 + R + a)^{N-n}, \ (1 + R)^{N-n}, \ (1 + R + a)^{N-n+1}, \ (1 + R + a)^{N-n+3} \ (1 + R)^{n+2}, \)

\(\ldots, \ (1 + R + a)^{(N-n-1)}, \ (1 + R)^{N-n}, \ (1 + R)^{N-n+1}\)

Note that \((N-n)\) quantities in the right hand side are the last \((N-n)\) quantities in the left hand side. What are left over are the first \(n\) quantities in the left hand side.

These are: \((1 + R + a)^{N-1}, \ (1 + R + a^2)^{N-2}, \ (1 + R), \ \ldots, \ (1 + R)^n, \ (1 + R + a)^{n+1}\)

Now if \(a > 0\) these quantities will produce a larger arithmetic mean on the left hand side than the right hand side with the converse if \(a < 0\).

The conclusion is that if \(a > 0\) then \(I > II\).

And if \(a < 0\) then \(I < II\).
Two examples will illustrate this:

<table>
<thead>
<tr>
<th></th>
<th>Example A</th>
<th>Example B</th>
</tr>
</thead>
<tbody>
<tr>
<td>S</td>
<td>$40,000</td>
<td>$40,000</td>
</tr>
<tr>
<td>N</td>
<td>9</td>
<td>9</td>
</tr>
<tr>
<td>n</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>R</td>
<td>4%</td>
<td>4%</td>
</tr>
<tr>
<td>(\alpha)</td>
<td>3%</td>
<td>-2%</td>
</tr>
<tr>
<td>c</td>
<td>15%</td>
<td>15%</td>
</tr>
</tbody>
</table>

Expression I (Pro-Rata) $69,098.98 $51,787.99.
Expression II (Exact) $67,089.31 $53,265.42

Of course \(R\) is never a constant from year to year, and \(\alpha\) can vary quite wildly.

Here is a better proof showing that the Pro-Rata Method gives a larger value than the exact method if \(\alpha > 0\) and vice-versa.

Pro-Rata gives

\[
\left(\frac{N-n}{N}\right) \left(\frac{c}{100}\right) \sum \left(\frac{1+R+\alpha}{\alpha}\right)^y - \left(1+R\right)^y
\]

...I
We want to show that for $a > 0$, $I > II$.

Define $f(a)$ as:

$$f(a) = \frac{N-n}{n} \left[ (1+R+\alpha)^n - (1+R)^n \right] - (1+R)^n \left[ (1+R+\alpha)^{N-n} - (1+R)^{N-n} \right]$$

Therefore, $f'(a) = 0$ if $a = 0$

$$f''(a) = (N-n)(N-1)(1+R+\alpha)^{N-3} - (N-n-1)(1+R)^{N-3}$$

at $a = 0$ 

$$f''(a) = (N-n)(N-1)(1+R)^{N-2} - (N-n-1)(1+R)^{N-2}$$

$$= (N-n)\alpha (1+R)^{N-2}$$

Define $f(a)$ as:

Therefore, $a = 0$ gives a minimum value for $f(a)$ and this minimum is zero.

Therefore, for $a > 0$, $f(a) > 0$ and this tells us that for $a > 0$, the Pro Rata Method gives a larger value than the Exact Method.
Designing an International Pension Program for Mobile Employees

by Lisa Larsen

Providing an equitable level of retirement income to employees worldwide has always been a challenge. The design of retirement programs must consider the company’s philosophy on retirement replacement income and competitive goals in addition to varying tax laws and social security programs of each country.

As companies expand into other countries, the initial employees of the foreign subsidiary are often temporarily recruited from the corporate headquarters. These citizens generally relocate to the foreign location to work anywhere from six months to five years. Expatriate agreements are usually provided that guarantee their home country payroll and benefits. Therefore, there is no interruption in their retirement benefit accumulation due to this international assignment.

As business grows in the new country, employees are hired locally. Most companies establish competitive retirement programs for these local employees based on the laws and social security programs of that particular country in conjunction with what the business can afford to provide.

The retirement situation becomes more complex, however, when employees who had been working abroad on expatriate assignments go on to transfer to other countries, working in multiple countries over the course of their career. Many times the company is unable or unwilling to continue to guarantee the home country benefits or the local laws make it difficult for these employees to continue to participate in their home country plans. In these situations, the typical solution has been for these employees to begin participating in the retirement programs of the foreign subsidiaries in which they are currently working.

As the company develops into a multinational company, with more and more local hires in foreign countries, the local employees may begin transferring from country to country. For example, country to country transfers are becoming increasingly more common throughout the European community. These employees may eventually participate in the retirement programs of two, three or even more countries. Many times the combined benefits from participating in multiple retirement programs results in a very small total replacement income, as compared to participation in a single retirement program, for the same number of years.

Shortfalls from participating in multiple retirement programs occur for the following reasons:

- Corporate programs do not or cannot recognize another country’s service for participation and vesting, or worldwide earnings for benefit accruals.
- Social Security (SS) is not well integrated with the plan in another country.
- There are variations in benefit levels among countries.
- Inappropriate transfer policies are being used for short-term savings.
EDS, A Case Study

EDS, a multinational corporation, found itself in this position in the early 1990’s. Employees with anticipated shortfalls in their retirement benefits were demanding that the company fix the problem. Potential transferees with specialized and valuable skills who were aware of the possible impact on their retirement benefits were refusing to go on assignments to another country. Therefore, EDS was forced to undertake a study to determine the best approach for addressing this problem.

Unfortunately, due to country-specific differences, including tax and legal requirements, there is no simple uniform approach to addressing these shortfalls on a worldwide basis. In addition, the company may have a history of growth by transitions and acquisitions, which has left a legacy of diverse practices, with less of a common benefits philosophy than might be found in multinational companies that have grown organically.

This paper presents a case study using EDS’s experience in designing an international pension program to address retirement shortfalls for internationally mobile employees (IMEs) on a corporate wide basis. Items to be covered include alternative plans considered along the way as well as the final plan design that was approved and implemented.

The goal for EDS was to minimize inequities in retirement benefits due to mobility in the most tax-effective way for both the company and the employee by using existing EDS retirement programs where possible. EDS wanted the plan to be easy to understand, easy to administer and easy to estimate the company’s liability.

EDS first needed to identify the employees groups affected. EDS discovered there were a variety of reasons that an employee may work in more than one country with the company over a career. These reasons included:

- Specialized skill needed temporarily by the company
- New business start-up in another country, requiring an executive to temporarily relocate to establish the business
- Employee interested in working in another country, but staying with the same company
- Employee wants to relocate due to personal reasons

Through analysis, two distinct categories of employees emerged at EDS. The first category was the highly paid executive who was asked to accept a temporary assignment in another country. These executives are typically guaranteed home country benefits and are on a formal expatriate package. For these employees, there is no shortfall at retirement as there is no interruption in benefits earned during their career. The second category is employees who worked in multiple countries with EDS for either professional or personal reasons. These employees are on local benefits, payroll and employment agreements in each country and, because of that were in danger of experiencing a shortfall at retirement (see above, for reasons shortfalls occur).
Identifying the Problem

To understand and address this situation, EDS needed a clear picture of what the benefit at retirement is for a full-career employee as compared to the sum of benefits payable from all retirement programs for these IMEs. A sample population of mobile employees was collected, their retirement benefits analyzed to determine if there were shortfalls, and the possible causes of their shortfalls were determined. A strategy was then developed to minimize the shortfalls.

A representative sample of 69 IMEs was located and their work and retirement history were documented and analyzed. The sample contained 45 U.S. citizens working in other countries and 24 other international employees (in 1993). The average age was 37 with average earnings of approximately US$64,000. They averaged 10 years of service, with an average of five years in the host country and were expected to have between 30-35 years of service by age 65 (normal retirement age). Most of the U.S. citizens were working in Canada or the UK. Most of the other IMEs were working in the UK or Germany.

To determine if there was a shortfall at retirement from being in more than one pension plan for EDS, a ‘target’ benefit was derived to compare the total retirement benefits for mobile employees to that of a similar benefit provided to other full-career EDS employees. EDS developed the ‘target’ by examining the replacement ratios in the various countries where these employees were located and the U.S., where the biggest population of employees is, and determined an average replacement ratio for the company. The replacement ratios determined by country, included company – and country-provided benefits. Using this analysis, it was determined that the retirement income target was approximately 55% of final pay.

Retirement Income Replacement Ratios
EDS then took the sample of people and calculated their projected benefits at retirement (age 65) based on their current work history and assuming they stayed in their current work country, and then compared that with the ‘target’ to determine the possibility of a shortfall in benefits at retirement. Comparing the sample to a 55% target replacement ratio at retirement, 25% of the sample group would not incur a shortfall.

Some of the causes of shortfalls of the remaining 75% of the sample were due to the fact that many of EDS’s individual country retirement programs did not recognize worldwide EDS service and/or earnings for benefit accruals. They only recognized service and earnings during the time the employee was working in that country. So IMEs were treated as if they had terminated EDS when they relocated, and were viewed as a new hire in the country they transferred to, even though they remained continuously employed with EDS. Shortfalls arose from the service-related vesting rules of each EDS pension plan when only the service in that country was recognized. By recognizing all service with EDS for vesting purposes, if a participant leaves a country without being vested, they would grow into the vesting, by continuing to work for EDS. Also shortfalls arose for defined benefit (DB) plans that provided benefits that are related to final average earnings, because the benefit was computed with the earnings at the date of international transfer and was not reflective of subsequent EDS salary increases in the new work country. Amending a final average earnings plan to include worldwide earnings, would allow the participant’s benefit to reflect their most recent years of earnings at retirement, which would most likely be their highest, rather than being treated as a vested termination with a frozen benefit (in most cases). Thus, the employee accrues greater benefits than if they left the company and this can be accomplished in a tax-effective way. By amending current plans to recognize worldwide service and earnings with EDS, where possible, another 45% of our sample group no longer showed a shortfall.
The remaining 30% of the sample showed an anticipated shortfall for a number of reasons and this is the group EDS targeted for the development of an international pension program. The shortfalls for these IMEs may be due to a mismatch of Social Security and EDS retirement plans. Some countries have great SS plans and therefore, the EDS sponsored plan was minimal, as seen with Italy and Germany in the graph above. Other countries, which have little or no SS plans, tend to have richer EDS sponsored plans, as seen with the UK and Australia. So even though the replacement ratio from the EDS plan plus SS plan tended to be between 50 and 60% for a full-career employee in most of the countries, IMEs who transferred from a country with high EDS benefits to a country with low EDS benefits, could experience a shortfall at retirement. Some EDS plans are also integrated with SS, thereby recognizing at least a portion of the benefit that will be provided to a full-career employee under the SS program in that country, this could also cause a shortfall as an employee moves among countries.

EDS further discovered that inappropriate transfer policies were being offered to some employees in attempts to keep them whole and save company money by not providing them with a full expatriate package. For example, some IMEs stayed in their home country plan but were paid according to local salary grids. This caused their benefit accruals to be very sensitive to fluctuations in currency exchange rates. In some cases, they got bigger accruals than they would have gotten if they were working in their home country, but the opposite also happened. That is, after they transferred, their local salary converted to their home country currency plummeted due to exchange rate fluctuations. There were also some inappropriate verbal promises made to some IMEs employees that later could not be substantiated, or required payments to be made outside of the formal plans. A corporate guideline rather than ad hoc program was needed so managers would know how to guide their employees through a cost-effective transfer for both parties without having to rely on individual agreements.

**Alternative Approaches Considered**

Once EDS defined the group of IMEs with possible shortfalls, possible ways of making up the shortfall were studied. Local plan coverage assures that all employees of a country are treated equally. Allowing mobile employees to participate in local plans, where they exist, is a tax-effective idea that is beneficial for employees planning on retiring in that host country because they accrue benefits useful to them in the future. However, gaps may still exist because of work countries without plans and even where there are plans, they may not be there long enough to vest, or may earn very low benefits due to their short service in that country.

Keeping IMEs in their home country plan when they are working in another country can cause legal and tax problems due to their not working in that home country and/or not being on the home country’s payroll. The participant may be taxed on benefits earned and the country may not be able to take a tax deduction on the employee’s accruals. Parent company plan coverage may cause tax or currency exchange control problems. There may also be legal penalties in some countries if coverage is affected with an insurer not registered to transact business in that country.
There are a number of approaches for addressing retirement shortfalls for IMEs being used, but there is no easy solution due to the complexity of legal and tax considerations in each country involved. EDS determined that any plan implemented had to be non-qualified because of the difficulty in designing a plan that would meet the tax qualification requirements of each country. Some companies provide protection on an individual basis, such as through a special agreement, guaranteeing employees a certain level of benefits at retirement or some make plan eligibility based on a case-by-case determination. Others have a pension plan for those that meet the eligibility requirements, such as having completed 10 years of service with the company and having worked in at least three countries and participated in local plans. The eligibility criterion depends on their definition of ‘internationally mobile’ employees. EDS defined an IME as an employee who works in at least two countries and participates in all local plans in those countries.

EDS considered one common pension plan approach referred to as an ‘umbrella plan.’ This plan sets an overall target benefit at retirement, e.g. 55% of earnings that the employee is guaranteed at retirement, offset by actual benefits received by other countries. It sounds good, but is hard to administer because the employee cannot determine what they are going to get from the plan until retirement. Estimates can be very cumbersome to calculate because information must be gathered from multiple plans and care must be taken to ensure that all benefits are estimated to begin at the same time or calculated with some sort of actuarial equivalency while making sure that all estimates use the same assumptions. The person calculating the estimate needs to study and understand each plan to determine the benefits and eligibility conditions to receive the benefit and to gather the earnings information needed from each country. It can be very time consuming to prepare an estimate in-house. If you hire a consultant to do the calculation, it can be expensive. Companies that have this type of plan complain of the administrative burden — so much so, that some have abandoned these plans. It is also difficult to estimate future liabilities of this type of plan.

Another approach to addressing shortfalls is the use a defined contribution (DC) plan. A DC plan can provide for an adequate retirement benefit, plan administration is straightforward, and is easy for the employee to understand. Mobility is not much of a problem because DC balances continue to earn interest through retirement or can be transferred to private interest-bearing accounts. There may be disadvantages for DC plans though in terms of tax issues; the deductibility of contributions and whether they are taxable to the employee when they are made and before the employee is vested. So, the employee may be paying taxes on a benefit they will never receive. An unfunded non-qualified plan could avoid these tax issues. An unfunded non-qualified plan would look similar to a cash balance defined benefit type plan with hypothetical account balances for participants.

EDS chose to use an unfunded defined contribution type program that provides a benefit that is supplemental to other EDS retirement benefits that may have accrued. The contribution rates are based on estimated shortfalls. It also provides for a past service credit as of the effective date of the plan. The company purposely chose not link this plan to any of the other EDS benefits to avoid administrative complexity.
The next question for EDS became which country they should as standard for which to calculate the shortfall. Many plans base the shortfall on the home country or the first work country. This works if the person eventually goes back to that country or if that is where they are planning to retire. At EDS, a person who started out in the UK (a high benefit country) and moved to Australia, would see a shortfall if you compare Australian benefits with UK benefits, but may not show a shortfall if they went to Italy. A person who starts in Australia and moves to Germany, where benefits are higher, may or may not have a shortfall, depending on how long they were working in each country and if they should then move to a third country, say Italy, would you then say there is no shortfall? It depends on all the countries they work in and how long they are there and if those countries recognize worldwide service and earnings. Because of these unknowns, EDS decided the best way to determine the possible shortfall was to base it on the IME’s current work country. That means that at different points in time, the projected shortfall for a mobile employee would be measured by the average company ‘target’ and their current work country and therefore could fluctuate.

International Supplement Retirement Plan Design

EDS set their target retirement ratio to 55% of earnings at retirement. Therefore to determine the supplement needed to minimize the shortfall at retirement, the following equation was used:

EDS Plans + Government-sponsored Programs + X = 55%,

Where X = Supplemental benefit, if required.

The following chart shows an analysis of six of our countries’ retirement benefit replacement ratios.

<table>
<thead>
<tr>
<th>Income Replacement Ratio at Retirement</th>
<th>Australia</th>
<th>Germany</th>
<th>France</th>
<th>Canada</th>
<th>UK</th>
<th>Italy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Termination Indemnity</td>
<td>0%</td>
<td>0%</td>
<td>2%</td>
<td>0%</td>
<td>0%</td>
<td>15%</td>
</tr>
<tr>
<td>Social Security</td>
<td>0%</td>
<td>40%</td>
<td>50%</td>
<td>10%</td>
<td>10%</td>
<td>55%</td>
</tr>
<tr>
<td>Local EDS Plan</td>
<td>45%</td>
<td>11%</td>
<td>0%</td>
<td>43%</td>
<td>57%</td>
<td>0%</td>
</tr>
<tr>
<td>Total</td>
<td>45%</td>
<td>51%</td>
<td>52%</td>
<td>53%</td>
<td>67%</td>
<td>70%</td>
</tr>
</tbody>
</table>

Given these replacement ratios, EDS’s consultants came up with the following annual contribution rates, to bring a full-career EDS employee up to approximately a 55% replacement ratio at retirement. Because the UK and Italy have replacement ratios of over 55%, there are no contributions while an employee is working in one of those countries.
Annual allocations are made to a participant’s account as of the end of the calendar year, based on the sum of their age and service, and the country they are working in. The percentages are applied to their earnings during that period. Interest is credited on their account balance at the end of the year. The interest rate used is equal to the 30-year United States Treasury bond yield rate as published in the *Wall Street Journal* on the first business day in September of each year. Earnings are converted to US$ using the exchange rate found in the *Wall Street Journal* as of the last business day of the year. After 10 years of service with EDS, they are 100% vested in these contributions plus interest.

For eligible employees, a past service allocation was added for years of service prior to January 1, 1997, the plan’s effective date. The past service allocation is equal to the annual allocation percentage (see schedule above) multiplied by their annual earnings for 1996. This is calculated for each eligible year of past service. Vesting of the past service allocation is based on service from January 1, 1997, and is shown in the following table:

<table>
<thead>
<tr>
<th>Years of Service</th>
<th>Vesting</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;1</td>
<td>0%</td>
</tr>
<tr>
<td>1 to &lt;2</td>
<td>20%</td>
</tr>
<tr>
<td>2 to &lt;3</td>
<td>40%</td>
</tr>
<tr>
<td>3 to &lt;4</td>
<td>60%</td>
</tr>
<tr>
<td>4 to &lt;5</td>
<td>80%</td>
</tr>
<tr>
<td>5+</td>
<td>100%</td>
</tr>
</tbody>
</table>

A lump-sum payment of the vested account balance is made when the participant retires or terminates from EDS.

**Special Consideration for US Citizens**

EDS learned that there are special issues for U.S. citizens and residents working abroad. The Internal Revenue Code (IRC) requires U.S. taxpayers to base income on their income from all sources. The only type of funded deferred compensation plan (DB or DC) in which a U.S. tax payer may participate without adverse tax consequences is one that complies with the qualified rules of the Internal Revenue Service (IRS). Coverage under any funded plan, foreign or U.S. based that does not comply with U.S. law, can subject the taxpayer to tax on imputed income arising from contributions to or benefits accruing under the plan. The U.S. tax law does not distinguish between a non-qualified plan in the U.S. and a foreign plan that may be in full compliance with local pension laws.
Most companies do not include U.S. citizens or permanent residents of the U.S. in pension plans for IMEs for the tax reasons noted above. But what about an unfunded non-qualified plan? There are two requirements that must be met for an ERISA exemption (i.e., make it okay to have an unfunded non-qualified plan, not subject to reporting and filing requirements):

1. The plan is for a select group of highly paid executives (EDS could not meet this criteria based on the data received for our population) and
2. Such plan is maintained outside of the U.S. primarily for the benefit of the persons ‘substantially all of whom are nonresident aliens’ (Title I of ERISA, Section 4(b)(4)).

There are no regulations interpreting what it means to have a plan maintained outside of the U.S., but most legal opinion says that this refers to where the employee works, not where it’s administered or where the records are kept.

The number of U.S. citizens allowed varies by legal opinions and can go as high as 25%. However, EDS was advised not let any U.S. citizens into the plan, because even if the plan starts out with no U.S. citizens, some of the participants will likely become U.S. citizens at some point and that number needs to be monitored.

One possible solution is to include U.S. citizens and residents in the U.S. qualified plan and provide umbrella coverage there, or cover them in a non-qualified plan, if the ERISA exemption requirements can be met. EDS chose to include them in the U.S. qualified DB plan. As long as they meet the eligibility requirements of working in at least two countries and participating in those countries local plans, they are covered in the “umbrella” provision of the U.S. plan. The U.S. plan was amended to recognize all EDS service and earnings in the calculation of a guaranteed benefit level. The U.S. plan was also amended to allow an offset of benefits paid from any other company plan (but never less than the actual pension earned in the plan while working in the U.S.).

Summary

EDS now has about 100 participants in the International Supplemental Retirement Plan, and continues to add more countries to the allocation grid, as people become eligible. There are about 30 “umbrella candidates” identified in the U.S. Retirement Plan so far, but this is still in the beginning stages of implementation. It is a manual process to locate these people and can be slow.

While there is no uniform solution, EDS feels that the approach of minimizing inequities rather than eliminating them has worked well. Overall, EDS is pleased with how things turned out. The design criteria of having a plan whose benefit aligns with the company’s shortfall strategy (minimizing, not guaranteeing no shortfall), is easy to understand. It is easy to estimate retirement benefits and EDS’ liability for participants in the International Supplemental Pension Plan. Administration, while requiring more manual effort than we would like, is not difficult. EDS is implementing a worldwide payroll system, which will make the identification, and tracking of these employees easier. Also planned, is moving more of the administration to the Internet, which will make gathering the data less cumbersome and easier for the employee to receive information on the plan.
The original goal was to minimize retirement shortfalls by maximizing current company-provided retirement plans worldwide. To accomplish this goal, EDS has taken full advantage of the existing retirement plans by amending them where possible to recognize worldwide service and earnings in the calculation of benefits.

For IMEs, other than U.S. citizens and residents subject to U.S. federal income tax the International Supplemental Retirement Plan, an unfunded defined contribution type plan has worked to minimize shortfalls. The benefit from this plan is in addition to benefits payable from all other plans, to bring the total retirement replacement income close to the target replacement ratio of 55%.

For U.S. citizens and residents, EDS amended the U.S. Retirement Plan to recognize all EDS service and earnings for benefit accruals and to permit U.S. Retirement Plan benefits to be offset by other EDS retirement benefits in other countries. The administration of this provision is more difficult than the International Supplemental Retirement Plan, because benefit estimates involve collecting other benefit information from all countries in which the employee has worked. Estimating EDS’ liability is also more difficult, but was determined to be overall the best solution available for this group.
**Turnover Rates and Compensation Levels**

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**Introduction**

In valuing liabilities for defined benefit plans, one of the key decrements is turnover. Traditional turnover tables most often relate to age and service. The traditional model assumes younger, shorter service employees tend to have a higher turnover than older, longer service employees. True enough. A typical table would probably have a 2-year select period and ultimate turnover for each age. In this case, the probability of turnover for a particular age may be one of three decreasing rates. For someone with less than one year of service, we would look up a rate from the 1-year select table. For someone with less than two years of service, we would look up a rate from the 2-year select table. For someone with over two years of service, we would look up a rate from the ultimate table.

While it may be generally recognized that higher paid employees tend to have lower turnover and they also tend to be the older, longer service employees, there is rarely (if ever) any explicit assumption made about the relation between the likelihood of turnover and the level of compensation. Maybe that’s OK, maybe not.

This study will hypothesize that higher paid employees tend to have different and generally lower turnover at all levels of age and service. If that is correct, age/service turnover tables will understate liability for plans that have a traditional defined benefit formula by overstating turnover for younger, shorter service, higher paid employees. In a similar fashion, liability for non-traditional front loaded plans, such as cash balance, will have liabilities overstated. This is particular true if the discount rate is higher than the interest crediting rate (in the case of a cash balance plan).

**General Example**

Consider a bank. What is the probability of turnover for two employees both age 40, both with one year of service? The first employee is a bank teller making $25,000 a year.
The second employee is a high paid executive recently recruited from a competing bank. A traditional age/service turnover table would assign the same probability of turnover to both employees, thus understating the liability for the executive (assuming the higher paid employee has a lower probability of turnover than the teller). In this case, a compensation-based table would more accurately predict turnover and associated liability for each employee. This is a specific example of what may be a more general rule, that for a traditional defined benefit plan, age/service based turnover tables will understate liabilities in cases where the probability of turnover decreases as compensation increases.

Numerical Example

It is true that turnover liability tends to be a relatively small portion of total liability, but a change in the turnover rates could have a significant impact on the projected retirement liability. As turnover rates increase, turnover liability increases, but generally, retirement liability would decrease much more, as fewer people are assumed to reach retirement age. In the test case used for this study, the total present value of benefits in a given year varies as much as 23% depending on which turnover table is being used.

Impact of Compensation

Considering compensation to determine the probability of turnover may be important because higher paid employees also carry the greatest potential liability. Even if compensation based turnover tables are no better predictor of turnover than traditional age/service based tables, they may be a better predictor of actual liability. This is because, by being more accurate with regards to higher paid employees, the overall prediction of liability is likely to be more accurate.

Granted, a union company with very little variance in compensation levels would not benefit from a wage based turnover table. However, there are clearly examples of employee groups that include significant numbers of higher paid, shorter service, younger employees (lawyers, doctors, etc) for whom traditional age/service based tables are clearly not the best predictors.

In many corporate environments, such as law firms, compensation is directly related to job category. That is, partners would be at the high end of the compensation scale, followed by non-partner lawyers, followed by paralegals and finally secretaries and other support staff. In this setting, using job category as a factor in determining turnover would be equivalent to using compensation and perhaps a bit more straight forward as
compensation would need to be adjusted each year for inflation. Compensation would be used explicitly in cases where there are too many titles or the titles are not sufficiently descriptive or consistent.

**Source of Data**

For purposes of studying patterns of turnover, 10 years of data will be analyzed for a medium size bank that could be considered representative of mid-size private companies. The average population for any year is about 3,500 lives for a total exposure of about 35,000 units. As mentioned above, it is expected that patterns would vary depending on the size of the employer and the nature of the business. If it can be shown that compensation is a superior predictor of liability for the sample medium size employer, it is almost certainly a better predictor for some smaller employers with a wide variance in compensation.

**Developing Tables**

The data for this study was initially collected for preparing the annual valuation of the employer’s pension plan. In this case, the cause of each decrement was not always captured. Since retirement becomes a factor only after 55, the study will focus on ages under age 55 so that the impact of retirement will not skew results. Since mortality and disability before age 55 are small, all decrements prior to age 55 will be assumed to be as a result of turnover.

The first step in developing sample turnover tables will be to group data in the 1/1/89 to 1/1/93 valuations. Data will be organized with one record for each active participant for each year. Each record will include the participant’s SSN, service as of the valuation, current pay, current age, valuation year and whether or not the participant was active one year after the valuation date. If not and if the participant is less than age 55 as of the valuation date, the participant will be assumed to have terminated during the year.

From this data, the probability of turnover will be determined by:

1. Age
2. Service
3. Compensation
4. Age/Service – matching ranges to actual data (see discussion below)
5. Age/Compensation
6. Compensation/Service
7. Traditional Age/Service – 3 year select and ultimate

Smoothing techniques will also be applied to the data to create tables without random fluctuations or spikes in the turnover rates. See the attached appendix for copies of the final tables.

**Ranges Used in Tables**

In the best case, every table would have a decrement by every age, service and compensation combination, as applicable. Tables for this study will not for two reasons. Number one, the rate of decrement will not always change as each variable changes. Number two, and perhaps more significant, the amount of data used for this study to develop the tables would not allow significant exposures for each combination of factors to provide statistically significant results.

The age-based table will have decrements by age from 18 (earliest age in the group) to age 55. The service-based table will have decrements by service from 0 to 40. Notice that anyone hired at 18 would only have 37 years of service at age 55.

The compensation-based table will have decrements in increments of $2,500 from 0 to $80,000. A larger band, say $5,000 or $10,000 might miss some termination patterns. Smaller bands would often have insignificant numbers of exposures. Participants making $80,000 or more were all grouped together since the number of exposures would not provide statistically significant results using smaller ranges.

Groupings for 2-factor tables were determined based on results of the 1-factor tables except in the case of table 7, the traditional age/service table which uses the traditional bands.

Grouping used for the 2-factor tables are as follows on page 59:
The compensation/service and age/compensation tables both have 18 cells (three compensation groups times six age groups or three compensation groups times six service groups). The age/service table has 36 cells (6 x 6).

**Other Assumptions**

The basis for any present value calculations will be 8% interest and 1994 Group Annuity Mortality.

The plan will be assumed to be a traditional 5-year final average pay plan with a 2% accrual rate and 5-year cliff vesting. This is an extremely simplified version of the actual plan provisions. Using actual plan provisions would add additional complexity without adding value. Though beyond the scope of this paper, it would be interesting to see results for a cash balance formula.

Since we are considering compensation as a basis for turnover, it is appropriate to make some adjustments for inflation and real wage growth. The salary scale for valuation runs will be assumed to be 4.5%. This includes 2.5% for inflation and 2% for real wage growth. For developing salary based turnover tables, salary before 1993 will be adjusted for inflation to the base year of 1993. So, for example, 1992 compensation will be multiplied by 1.025 to get adjusted 1993 compensation.

In each “valuation,” for purposes of looking up a decrement from a salary-based table, compensation projected forward at 4.5% will be adjusted back to 1993 at 2.5% before looking up the appropriate decrement in a salary based table. Rather than adjusting breakpoints in the table each year, the programming adjusts compensation before looking up values in the applicable table.
Valuation Runs

Data from 1/1/89 to 1/1/93 will be used to develop sample turnover tables. Data as of 1/1/94 to 1/1/97 will be used to run test valuations for various tables. Data as of 1/1/98 will only be used as a basis to determine what employees that were active as of 1/1/97 were still active as of 1/1/98.

Methodology for Validating Hypothesis

Once sample turnover tables have been developed using the 1989 through 1993 data, the next step will be to calculate liabilities with data as of 1/1/94, 1/1/95, 1/1/96 and 1/1/97. The turnover tables that produce the least gains and losses will be considered to be better predictors of future potential liability.

Gain/loss will be determined by comparing the actual liability release from turnover compared to the expected release. Expected liability release will be the sum over all active employees of:

\[ W_x \times (PVB - PVAB) \]

\( W_x \) - the probability of turnover (withdraw) at age x (as of the valuation date)

\( PVB \) – the total present value of projected benefits. Arguable, the Entry Age Normal or Projected Unit Credit accrued liability could have been used. Since the present value of benefits reflects the total impact of future decrements, it was deemed to be the most appropriate basis for the study. \( PVB \) will be calculated for each gain/loss calculation based on the turnover table under consideration. That is, if we are calculating the gain/loss for an age/compensation table, the \( PVB \) will be based on the same table.

\( PVAB \) – the present value of vested accrued benefits. The \( PVAB \) is the present value of the vested accrued benefit that would be paid if the participant terminated during the year.

The actual liability release will be the sum for terminated employees of \( PVB - PVAB \).
Calculating PVB

Traditional valuation programming handles age and age/service tables. It does not handle compensation-based tables. In order to have a consistent source of PVB, programming was set up in Microsoft Access 97 specifically to use any of the developed tables. Data is stored in tables with most of the calculations being done in modules (user defined functions). See Appendix I for a copy of the function used to calculate the PVB.

Present Value of Benefits (using each of 7 turnover tables for 4 valuations)

<table>
<thead>
<tr>
<th>Valuation Date - &gt;</th>
<th>01-Jan-94</th>
<th>01-Jan-95</th>
<th>01-Jan-96</th>
<th>01-Jan-97</th>
<th>Average</th>
</tr>
</thead>
<tbody>
<tr>
<td>PVB1 (age)</td>
<td>107,186,080</td>
<td>105,940,195</td>
<td>120,474,128</td>
<td>130,990,231</td>
<td>117,149,155</td>
</tr>
<tr>
<td>PVB2 (svc)</td>
<td>122,929,670</td>
<td>123,340,200</td>
<td>135,410,457</td>
<td>146,022,118</td>
<td>131,425,611</td>
</tr>
<tr>
<td>PVB3 (comp)</td>
<td>103,518,623</td>
<td>106,020,231</td>
<td>116,237,147</td>
<td>128,432,872</td>
<td>113,352,268</td>
</tr>
<tr>
<td>PVB4 (age/svc)</td>
<td>114,232,607</td>
<td>117,351,580</td>
<td>128,736,316</td>
<td>139,878,297</td>
<td>125,049,775</td>
</tr>
<tr>
<td>PVB5 (age/comp)</td>
<td>122,249,116</td>
<td>122,842,556</td>
<td>134,815,118</td>
<td>145,642,766</td>
<td>130,887,239</td>
</tr>
<tr>
<td>PVB6 (svc/comp)</td>
<td>126,896,182</td>
<td>129,684,511</td>
<td>142,447,094</td>
<td>163,763,861</td>
<td>138,192,917</td>
</tr>
<tr>
<td>PVB7 (trad age/svc)</td>
<td>114,055,571</td>
<td>116,924,512</td>
<td>128,380,654</td>
<td>139,243,762</td>
<td>124,551,226</td>
</tr>
</tbody>
</table>

Gains and Losses

<table>
<thead>
<tr>
<th>Valuation Date - &gt;</th>
<th>01-Jan-94</th>
<th>01-Jan-95</th>
<th>01-Jan-96</th>
<th>01-Jan-97</th>
<th>Average</th>
</tr>
</thead>
<tbody>
<tr>
<td>WD (Gain)/Loss1</td>
<td>2,647,892</td>
<td>631,573</td>
<td>1,935,097</td>
<td>789,319</td>
<td>(1,500,970)</td>
</tr>
<tr>
<td>WD (Gain)/Loss2</td>
<td>2,269,297</td>
<td>285,448</td>
<td>1,858,953</td>
<td>279,537</td>
<td>(1,172,809)</td>
</tr>
<tr>
<td>WD (Gain)/Loss3</td>
<td>2,652,510</td>
<td>774,878</td>
<td>1,955,717</td>
<td>787,548</td>
<td>(1,537,663)</td>
</tr>
<tr>
<td>WD (Gain)/Loss4</td>
<td>1,618,815</td>
<td>637,735</td>
<td>583,217</td>
<td>1,003,351</td>
<td>(140,241)</td>
</tr>
<tr>
<td>WD (Gain)/Loss5</td>
<td>2,033,329</td>
<td>16,609</td>
<td>1,544,107</td>
<td>68,628</td>
<td>(873,000)</td>
</tr>
<tr>
<td>WD (Gain)/Loss6</td>
<td>1,099,221</td>
<td>1,115,147</td>
<td>318,999</td>
<td>1,585,769</td>
<td>116,174</td>
</tr>
<tr>
<td>WD (Gain)/Loss7</td>
<td>2,172,938</td>
<td>245,147</td>
<td>1,700,453</td>
<td>244,932</td>
<td>(1,090,875)</td>
</tr>
</tbody>
</table>

Observations – the single factor tables

The compensation only table produces the lowest PVB. This is a result of the compensation only table overstating the probability of turnover, on average, at higher compensation levels. For example, the probability of turnover for a 50 year old with 20 years of service that makes $45,000 would be 15.34% based on the compensation only table, while the age-table has a probability of turnover of 10% and the service only table has a probability of 7.25%. The two-factor tables result in turnover from 6% to 9.6%, further supporting this conclusion. Said in a different way, the 15.34% ignores the actual
age and service, both of which would indicate a lower expected rate of turnover. The net result, is, on average, the compensation only table overstates turnover and so understates liability.

The single factor age and compensation tables produce similar PVB and nearly identical gains and losses. In terms of minimizing gains and losses, compensation is as good as age, but service is the best predictor. There are probably other groups in which compensation alone would be superior to age alone and others where it would be inferior. This remains to be tested.

**Observations – the 2-factor tables**

At first glance, it might appear from the last column that turnover table 4 based on age and service is the superior option. This is based on an average gain/loss of only (140,241) over the 4-year period. Even more interesting perhaps, the traditional age/service table, which does only a mediocre job of minimizing the gain/loss has an average PVB nearly equal to that based on table 4 (modified age/svc). How could this be? Given PVB are approximately equal and PVAB is the same, the only factor left in the gain/loss calculation is the turnover decrement for each individual for the valuation year. Table7, on average, overstates the probability of turnover in the year following the valuation (thus resulting in a larger liability loss), while understating the probability of turnover in future years in such a way that the PVB for table 7 is approximately equal to that of table 4.

2-factor tables that use compensation as a factor consistently produce higher PVB than tables that do not use compensation as a factor.

Further, the 2 factor tables produce superior results in all cases when compared to the single factor tables. As is consistent with comments concerning the 1-factor tables, two-factor tables that use service produce results that are superior to those that do not use service.

**Conclusions**

Clearly, the level of research involved in this study and related results are far too narrow to make any sweeping generalizations. If anything, more questions are raised than questions answered.
Interestingly, the rates of turnover at compensation levels over $20,000 was not shown to have significant variation. In large part, it is likely that the much higher turnover levels at lower compensation levels is due to part-time employees (of which banks often have many). If that is the case, it might make sense to run a separate valuation for part-time employees (using an appropriate age/service table) and another valuation for other employees.

Perhaps the most significant result from this study is that traditional age/service tables do a poor job of predicting gains and losses. By expanding the service bands, age/service tables could be much better predictors of actual liability.

At very high compensation levels (over $120,000), turnover rates tended to start going up again. However, the amount of data was insufficient to reflect in the turnover table or to make any generalizations.

It seems clear that the study of how compensation and service impact turnover is an area that deserves more attention. At the very least, compensation appears to be a factor in predicting turnover. Both the age/compensation and service/compensation tables produce results that are superior to the age only and service only tables. It is likely that using compensation in other combinations with additional refinements and with other employer groups may be shown to significantly improve the prediction of liability. It is significant that there are only 18 cells in age/compensation and service/compensation tables. With more extensive data, future studies may be able to show more definitive results.

**Impact on Funding**

If a table using compensation as a factor is in fact a better predictor and produces a larger PVB, the funding requirement would naturally increase as well. The extent of the increase would of course be dependent on several variables, like the market value of assets, the asset valuation method, the funding method. In any event, a 10% increase in liability could, for a plan that is currently making contributions, produce a significant contribution increase.

Admittedly, valuation methods such as projected unit credit that focus on the liability accrued to date, will be much less affected by changes in the turnover (as will financial disclosures under FASB which are, of course, based on the projected unit credit method).
**Future action**

If you were inclined to do some valuation runs based on compensation, how would you set up the programming? I would suggest splitting participants into groups by compensation (or job category, as appropriate), making a run for each group using appropriate age/service tables and summing the results. As technology progresses and valuation programming catches up, perhaps compensation bands will eventually become a standard parameter.
### Appendix I – One Factor Turnover Tables

*(Tx = Probability of Turnover)*

<table>
<thead>
<tr>
<th>Age</th>
<th>Service</th>
<th>Tx</th>
<th>Comp</th>
<th>Tx</th>
</tr>
</thead>
<tbody>
<tr>
<td>13</td>
<td>38.00%</td>
<td>0.00</td>
<td>25.00</td>
<td>38.34%</td>
</tr>
<tr>
<td>19</td>
<td>36.05%</td>
<td>1.00</td>
<td>26.48</td>
<td>36.26%</td>
</tr>
<tr>
<td>20</td>
<td>34.89%</td>
<td>2.00</td>
<td>24.80</td>
<td>35.34%</td>
</tr>
<tr>
<td>21</td>
<td>30.87%</td>
<td>3.00</td>
<td>20.95</td>
<td>31.52%</td>
</tr>
<tr>
<td>22</td>
<td>30.16%</td>
<td>4.00</td>
<td>18.57</td>
<td>27.77%</td>
</tr>
<tr>
<td>23</td>
<td>27.37%</td>
<td>6.00</td>
<td>16.12</td>
<td>22.61%</td>
</tr>
<tr>
<td>24</td>
<td>26.37%</td>
<td>6.00</td>
<td>14.16</td>
<td>18.68%</td>
</tr>
<tr>
<td>25</td>
<td>25.44%</td>
<td>7.00</td>
<td>12.98</td>
<td>15.64%</td>
</tr>
<tr>
<td>26</td>
<td>24.13%</td>
<td>8.00</td>
<td>11.78</td>
<td>13.00%</td>
</tr>
<tr>
<td>27</td>
<td>22.73%</td>
<td>9.00</td>
<td>11.28</td>
<td>12.00%</td>
</tr>
<tr>
<td>28</td>
<td>22.14%</td>
<td>10.00</td>
<td>10.88</td>
<td>12.00%</td>
</tr>
<tr>
<td>29</td>
<td>20.19%</td>
<td>11.00</td>
<td>10.50</td>
<td>13.00%</td>
</tr>
<tr>
<td>30</td>
<td>18.06%</td>
<td>12.00</td>
<td>9.93</td>
<td>13.00%</td>
</tr>
<tr>
<td>31</td>
<td>17.13%</td>
<td>13.00</td>
<td>9.24</td>
<td>14.27%</td>
</tr>
<tr>
<td>32</td>
<td>16.21%</td>
<td>14.00</td>
<td>8.79</td>
<td>14.70%</td>
</tr>
<tr>
<td>33</td>
<td>15.40%</td>
<td>15.00</td>
<td>8.34</td>
<td>14.99%</td>
</tr>
<tr>
<td>34</td>
<td>15.02%</td>
<td>16.00</td>
<td>7.71</td>
<td>15.62%</td>
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(Tx = Probability of Turnover)

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Appendix IV - Access Function to Calculate Present Value of Benefits

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' wdcode = 2 svc
' wdcode = 3 comp
' wdcode = 4 age/svc
' wdcode = 5 age/comp
' wdcode = 6 svc/comp
' wdcode = 7 trad age/svc
Dim ValYr As Long
Dim iYr As Long
ValYr = Year(Valdt)
iYr = ValYr 'use iyr in loop
Dim i As Integer
Dim Fctr As Double
Dim SumFctr As Double
Dim wd As Double
Dim ab As Double
Dim tage As Long
Dim tComp As Double
Dim adjComp As Double
Dim tSvc As Double
Dim LSvc As Double 'for lookup age/svc, comp/svc tables
Dim myDB As Database
Dim myRS As Recordset, tck As Double
Dim mSQL As String, Px As Double
Set myDB = CurrentDb
mSQL = "select * from [" & wdTable & "]"
Set myRS = myDB.OpenRecordset(wdTable, dbOpenTable)
myRS.Index = "PrimaryKey"
For i = myJy To 55
    ab = CalcTradAB(tComp, tSvc)

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Select Case WDcode  ‘Evaluate Number.
Case 1
    myRS.Seek "="i  ‘get decrement for age w/d
Case 2
    myRS.Seek "="Mn(37, tSvc \ 1) ‘svc w/d
Case 3
    adjComp = tComp / (1.025 ^ (iYr - 1993))  ‘adjust to base yr 1993
    adjComp = (adjComp / 2500 \ 1) * 2500 ‘round to 2500
    myRS.Seek "="Mn(80000, adjComp) ‘comp w/d
Case 4  ‘by age and comp
    adjComp = tComp / (1.025 ^ (ValYr - 1993))  ‘adjust to base yr 1993
    adjComp = (adjComp / 2500 \ 1) * 2500 ‘round to 2500
    If adjComp < 12500 Then
        adjComp = 0
    Else
        If adjComp >= 20000 Then
            adjComp = 20000
        Else
            adjComp = 12500
        End If
    End If
End If
Select Case i  ‘age
    Case Is <= 22
        tage = 0
    Case 23 To 27
        tage = 23
    Case 28 To 32
        tage = 28
    Case 33 To 37
        tage = 33
    Case 38 To 42
        tage = 38
    Case Is >= 43
        tage = 43
End Select
myRS.Seek "="tage, adjComp ‘comp w/d
Case 5  ‘age/svc decrement
Select Case i  ‘age
    Case Is <= 22
        tage = 0
    Case 23 To 27
        tage = 23
    Case 28 To 32
        tage = 28
    Case 33 To 37
        tage = 33
End Select
myRS.Seek "="tage, adjComp ‘comp w/d
tage = 33
Case 38 To 42
tage = 38
Case Is >= 43
tage = 43
End Select
Select Case tSvc \ 1 ‘svc
Case 0, 1
lSvc = 0
Case 2, 3
lSvc = 2
Case 4, 5
lSvc = 4
Case 6 To 9
lSvc = 6
Case 10 To 15
lSvc = 10
Case Is >= 16
lSvc = 16
End Select
myRS.Seek ‘=’ tage, lSvc
Case 6 ‘ svc/comp decrement
Select Case tSvc \ 1 ‘svc
Case 0, 1
lSvc = 0
Case 2, 3
lSvc = 2
Case 4, 5
lSvc = 4
Case 6 To 9
lSvc = 6
Case 10 To 15
lSvc = 10
Case Is >= 16
lSvc = 16
End Select
adjComp = tComp / (1.025 ^ (iYr - 1993)) ‘adjust to base yr 1993
adjComp = (adjComp / 2500 \ 1) * 2500 ‘round to 2500
If adjComp < 12500 Then
adjComp = 0
Else
If adjComp >= 20000 Then
adjComp = 20000
Else
adjComp = 12500
End If
End If
myRS.Seek ‘=’, lSvc, adjComp
Case 7 'traditional age/svc table
   Select Case i 'age
   Case Is <= 18
tage = 18
   Case 19 To 54
tage = i
   Case Is > 54
tage = 54
   End Select
   Select Case tSvc \\ 1 'svc
   Case 0
   ISvc = 0
   Case 1
   ISvc = 1
   Case 2
   ISvc = 2
   Case Is >= 3
   ISvc = 3
   End Select
   myRS.Seek "=", tage, ISvc
   Case Else   ' Other values.
      '        Exit Function
   End Select

   tComp = Mn(160000, tComp * (1 + myFSS))
tSvc = tSvc + 1
iYr = iYr + 1
If i < 55 Then
   ab = ab * vpct(tSvc)
   wd = myRS!decr * Px
Else
   wd = Px
End If
Ps = Px * (1 - myRS!decr)
Fctr = wd * ab
tck = tck + wd
SumFctr = SumFctr + Fctr
Next i

PVB = SumFctr * Age55AnnFctr / (1.08 ^ (Mx(55, myJy) - myJy))
End Function
**PROCEDURE FOR PREPARING ARTICLES FOR THE PENSION FORUM**

*Pension Section News* is intended as a medium for the timely exchange of ideas and information of interest to pension actuaries. *The Pension Forum* is for the publication of full papers and is issued on an ad hoc basis by the Pension Section.

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